2016 PZ Q & (I) (a) C/N: SET OF COSETS OF N IN G, IE SET OF COSETS Ng, g &G. Normal SN=NS Y & . SHOW THAT IT IS INDEED A GREAT? Patrition or into colets each elt in LAGRANGE: ORDER OF GROUP IS DIVISIBLE BY ORDER OF usadly one cret. ALL SUZGROUPS The onto id id iv. +2 cuts juis out it is closed.  $\sigma_{x} \sigma_{z} = \begin{pmatrix} 01 \\ 10 \end{pmatrix} \begin{pmatrix} 0 - i \\ i & 0 \end{pmatrix} = \begin{pmatrix} i & 0 \\ 0 - i \end{pmatrix} = \sigma_{z} \cdot i$ (b) (c) (d) Ez·i € € €x, €3, €2, ₹3 => SET NOT CLOSED, SO NOT I A GROUP FOR SURE.  $\underline{\sigma_3}\underline{\sigma_x} = \begin{pmatrix} 0 - i \\ i \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} -i \\ 0 \\ i \end{pmatrix} = -i \cdot \underline{\sigma_z}$  $= x = \frac{01}{10} \begin{bmatrix} 10 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 - 1 \\ 10 \end{bmatrix} = -i \cdot 53$  $\frac{O_3O_7}{=1} \begin{pmatrix} 0 - i \\ i \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 0 - 1 \end{pmatrix} = \begin{pmatrix} 0 & i \\ i & 0 \end{pmatrix} = i \cdot \mathcal{Q}_X$  $\mathcal{L}_{23} = \begin{pmatrix} 10 \\ 0-1 \end{pmatrix} \begin{pmatrix} 0 & -1 \\ i & 0 \end{pmatrix} = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix} = -1 \cdot \mathcal{L}_{23}$  $Q \times Q \times = \begin{pmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} = I$  $= \hat{3} = \hat{3} = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} \begin{pmatrix} 0 & -1 \\ i & 0 \end{pmatrix} = -\mathbf{I}$ QZ OZ = (10) (10) = I

IEG > PRESENCE OF DENTITY REQUIREMENT SATISFIED.

201672080  $9_{11}9_{2} \in \{0,1,2,3\}$ Letter one white  $5^{2}$ or the  $5^{2}$   $4^{2}$   $4^{2}$ IN GENERAL  $(i)^{42}\sigma_{g}=i \in ijk \sigma_{k}(i)^{41+4/2}$  $\pm \delta_{ij} I(i)^{q_1+q_2} = t$ in Soft we (+ i + i, j + y)where (+ i + i, j + y)HO, TEG > GROUP IS CLOSED UNDER MULTIPLICATION  $(-\sigma_x)^2 = -\sigma_x | (-\sigma_y)^2 = -\sigma_z | (-\sigma_z)^2 = \sigma_z |$   $(-\sigma_x)^2 = -\sigma_x | (-\sigma_z)^2 = \sigma_z | (-\sigma_z)^2 = -\sigma_z |$   $(-\sigma_x)^2 = -\sigma_x | (-\sigma_z)^2 = \sigma_z |$   $(-\sigma_z)^2 = -\sigma_z | (-\sigma_z)^2 = \sigma_z |$  $(i\sigma)^{1} = -i\sigma_{x}(i\sigma)^{1} = i\sigma_{y}(i\sigma)^{2} = -i\sigma_{z}$  $(-i\sigma)^{-1}=i\sigma_{\chi}(-i\sigma_{\chi})^{2}=-i\sigma_{\chi}u_{\chi}(-i\sigma_{\chi})^{2}=i\sigma_{\chi}u_{\chi}$ > INVERSE PRESENT FOR EVERY gEG PRESENCE OF IDENTITY, CLOSE DIESS, PRES. 27 INVERSES LET | | - | g-1 | = a  $9^{19^{1}(g-1)^{19-1}}=g^{a+1g-1}(g^{-1})^{19-11}=g^{19^{-1}(g-1)^{19-11}}=g^{19^{-1}(g-1)^{19}}=g^{19^{-1}(g-1)^{19}}=g^{19^{-1}(g-1)^{19}}=g^{19^{-1}(g-1)^{19}}=g^{19^{-1}(g-1)^{19}}=g^{19^{-1}(g-1)^{19}}=g^{19^{-1}(g-1)^{19}}=g^{19^{-1}(g-1)^{19}}=g^{19^{-1}(g-1)^{1$  $=g^{q}\left(gg^{-1}\right)\left[g^{-1}\right]$   $=g^{q}\left[g^{-1}\right]=1$   $\int_{0}^{\infty} du \text{ that the order } g^{-1}g^{-1}=1$   $\int_{0}^{\infty} du \text{ that the order } g^{-1}g^{-1}=1$   $\int_{0}^{\infty} du \text{ that the order } g^{-1}g^{-1}=1$   $\int_{0}^{\infty} du \text{ that the order } g^{-1}g^{-1}=1$