

## TOPICS 3

### 1/ FIRST PARAGRAPH

$$\text{RADIATION PRESSURE: } P = \frac{L}{4\pi r^2 c}$$

FORCE FROM RADIATION  
PRESSURE = FORCE FROM  
GRAVITY.

THIS COMES  
FROM:

$$P = \frac{\text{MOMENTUM FLUX}}{\text{IN UNIT TIME}} = \frac{1}{A t}$$

~~E TOTAL~~

$$= \frac{E_{\text{TOTAL}} / t}{4\pi r^2 \cdot t} = \frac{L}{4\pi r^2 c}$$

$$\frac{L}{4\pi r^2 c} \pi a^2 = \frac{4}{3} \pi a^3 S M / r^2 \cdot G$$

$$a = \frac{3}{16} \frac{1}{\pi} \frac{L}{M} \frac{1}{G c S}$$

AS WANTED.

## SECOND PARAGRAPH.

$$\text{CIRCULAR ORBIT} \Rightarrow F_{\text{NET}} = \frac{v^2}{r} M$$

$$F_{\text{NET}} = F_{\text{GRAV}} - F_{\text{RADIATION}}$$

$$F_{\text{NET}} = G \frac{\frac{4}{3}\pi(2a)^3 S M}{r^2} - \frac{L}{4\pi r^2 c} (2a)^2 \pi = \frac{v^2}{r} \frac{4}{3}\pi(2a)^3 S$$

INTRODUCE CONSTANTS:

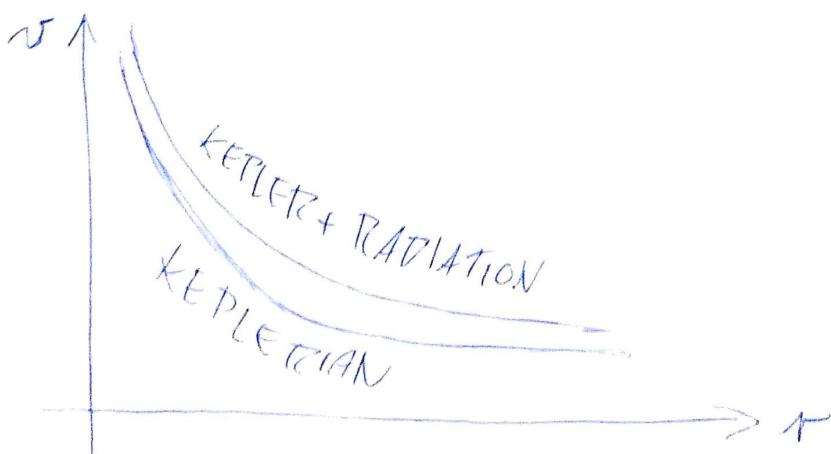
$$G \frac{4}{3}\pi(2a)^3 S M = A > 0 \quad \frac{L}{4\pi r^2 c} (2a)^3 \pi = B > 0$$

$$\frac{4}{3}\pi(2a)^3 S = C > 0$$

$$(A - B) \frac{1}{r^2} = \frac{v^2}{r} C$$

$$v = \sqrt{\frac{1}{C} (A - B) \frac{1}{r}}$$

KEPLERIAN ORBIT:  $B = 0$



# LAST PARAGRAPH

STAR 1

$$M_{\odot}$$

$$L_1 \propto (M_{\odot})^3$$

STAR 2

$$2M_{\odot}$$

$$L_2 \propto (2M_{\odot})^3 = 8 M_{\odot}^3$$

MASS OF ROCKY MATERIAL AROUND STAR 1.

$$= \int_{a_{\text{STAR 1}} \text{ BLOCKOUT}}^{1 \text{ fm}} a^{-3.5} da \cdot \frac{4}{3} \pi a^3 S dN(a)$$

(THIS INTEGRAL IS JUST:

NUMBER OF (THIS BIG OBJECTS) · MASS OF SUCH AN OBJECT SUMMED OVER ALL OBJECT SIZES.

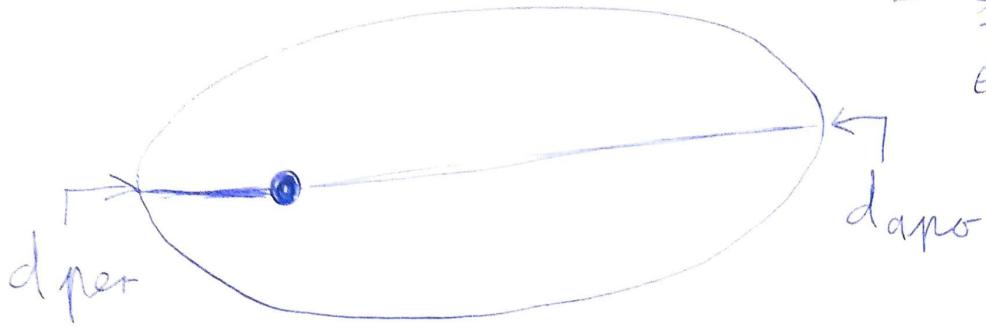
$$\propto \int_{a_{\text{STAR 1}} \text{ BLOCKOUT}}^{1 \text{ fm}} a^{-0.5} da \propto a^{\frac{1}{2}}$$

MASS OF ROCKY MATERIAL AROUND STAR 2

$$= a^{\frac{1}{2}} \Big|_{\text{STAR 2 BLOCKOUT}}^{1 \text{ fm}}$$

$\Rightarrow$  RESULTING MASS IS DOMINATED BY UPPER SIZE, SO NO SIGNIFICANT DIFFERENCE IS EXPECTED.

## 2. FIRST PARAGRAPH



THIS IS  
SUPPOSED  
TO BE AN  
ECLIPSE.

$$T = 2\pi \sqrt{\frac{a^3}{GM}} \Rightarrow \frac{T^2}{4\pi^2} GM = a^3 \Rightarrow a = \left( \frac{GM}{4\pi^2 T^2} \right)^{\frac{1}{3}}$$

$$d_{\text{per}} = a(1-e)$$

$$e = -\frac{d_{\text{per}}}{a} + 1$$

$$= -\frac{d_{\text{per}}}{\left( \frac{GM}{4\pi^2 T^2} \right)^{\frac{1}{3}}} + 1$$

$$= -\frac{10^4 \cdot 1.5 \cdot 10^{11}}{\left( \frac{G \cdot 2 \cdot 10^{30}}{4\pi^2} \left( 2 \cdot 10^7 \cdot 365 \cdot 24 \cdot 60 \cdot 60 \right) \right)^{\frac{1}{3}}} + 1$$

$$\approx \underline{0.89}$$

## SECOND PARAGRAPH



ENERGY CONSERVATION:

$$\frac{1}{2} v_p^2 - \frac{\mu}{d_p} = C$$

ANGULAR MOM CONSERVATION:

$$d_p v_p = d_a v_a$$

$$\frac{1}{2} v_p^2 - \frac{\mu}{d_p} = \frac{1}{2} v_a^2 - \frac{\mu}{d_a}$$

use:  $d_p \ll d_a$ , NEGLECT THIS TERM.

$$\frac{1}{2} v_p^2 - \frac{\mu}{d_p} \approx \frac{1}{2} v_a^2$$

SUB FOR  $v_a$

$$\frac{1}{2} v_p^2 - \frac{\mu}{d_p} \approx \frac{1}{2} \left( \frac{d_p}{d_a} \right) v_p^2$$

$\approx \ll \Rightarrow$  NEGLECT THIS TERM

$$\frac{1}{2} v_p^2 - \frac{\mu}{d_p} \approx 0$$

REARRANGE, RENAME  $d_p$  TO  $T_p$ :

$$v_p \approx \left( \frac{2\mu}{T_p} \right)^{1/2} \text{ AS WANTED.}$$

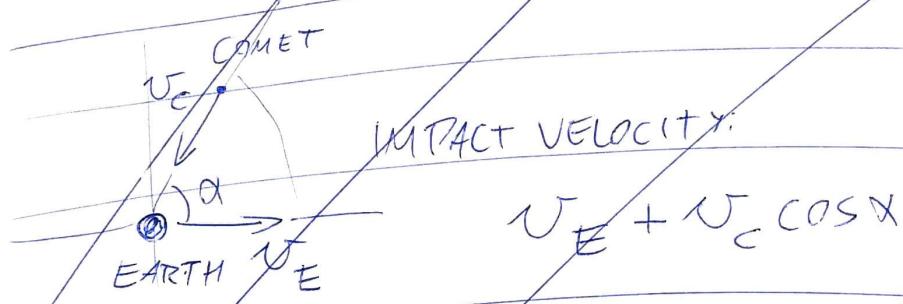
HENCE, ESTIMATE...

$$v_p \approx \left( \frac{2k}{\tau_p} \right)^{1/2}$$

$$\frac{v^2}{r_{\text{EARTH}}} = \frac{\mu}{r_p^3} \Rightarrow v_{\text{EARTH}} = \sqrt{\frac{\mu}{r_p}}$$

~~IF HEAD ON COLLISION WITH OPPOSITE DIRECTION  
OF VELOCITIES:~~

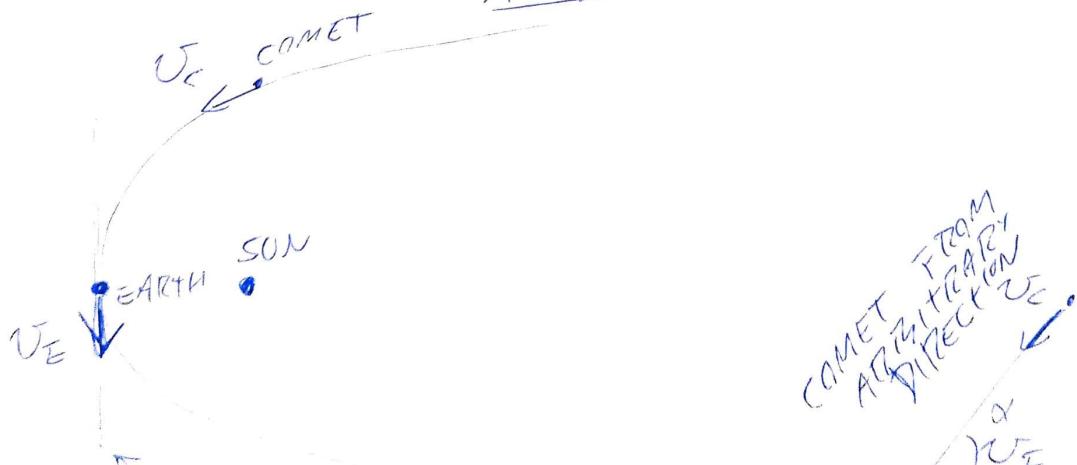
~~MAX IMPACT VELOCITY~~



$$\text{AVERAGE QUANTITY} = \int \text{PROBABILITY DISTRIBUTION OF QUANTITY} \cdot \text{QUANTITY} \cdot dP$$

~~COMETS COME FROM ALL DIRECTIONS~~

ASSUME UNIFORM



TAKE THIS PLANE,  
LOOK FROM  
SIDEWAYS:

$$\text{AVG QUANTITY} = \int_{\text{PROBAB DISTRIB OF QUANTITY}}^{\text{QUANTITY}} dP$$

PROBABILITY OF COMET  
COMING TO EARTH  
WITH ANGLE  $\alpha$   
BETWEEN  $\alpha$  &  $\alpha + d\alpha$

$$\text{IMPACT VELOCITY} = v_E - v_c \cos \alpha$$

$$\text{AVG IMPACT VELOCITY} = \int_0^{2\pi} (v_E - v_c \cos \alpha) \frac{d\alpha}{2\pi} = \cancel{v_{\text{Earth}}} \quad (v_{\text{Earth}} = \sqrt{\frac{N}{\pi}})$$

NO DEPENDENCE ON  
COMET SPEED.

"ONE DISPLACED" ...

$KE = \frac{1}{2} mv^2 = \frac{1}{2} M \frac{\mu}{r}$   
THIS IS SPENT ON HEATING UP THE ATMOSPHERE  
& MAY BE LIFTING SOME PARTS OF IT?

I DON'T SEE HOW I COULD RELATE THIS  
TO ~~EATEN~~ ~~LOGGED~~ MASS OF LOST  
ATMOSPHERE.

# "THE DENSITY OF STATES"

$$T_{\text{NEMESIS}} \approx 2.6 \cdot 10^7 \text{ yrs}$$

$$\hookrightarrow \approx 8.2 \cdot 10^{14} \text{ sec}$$

$$\begin{aligned} & \hookrightarrow 20 \\ & \hookrightarrow 1.6 \cdot 10^{16} \text{ km closer} \\ & \quad \text{some stars} \\ & \quad \text{get in a bit} \\ & \hookrightarrow 500 \text{ pc} \end{aligned}$$

I DON'T SEE HOW TO CALCULATE FREQUENCY  
OF ENCOUNTERS BUT HYPOTHESIS DOES NOT  
SEEM PLAUSIBLE.

3



$$\frac{(F_c - F_e)}{m} = GM \left( \frac{1}{r^2} - \frac{1}{(r + 2R_p)^2} \right)$$

NOTE THAT:

$$(r + 2R_p)^{-2} = \left( r \left( 1 + \frac{2R_p}{r} \right) \right)^{-2} = r^{-2} \left( 1 + \frac{2R_p}{r} \right)^{-2}$$

$$\approx r^{-2} \left( 1 - 4 \frac{R_p}{r} \right)$$

SUBSTITUTE:

$$\frac{(F_c - F_e)}{m} = GM \left( \frac{1}{r^2} - \frac{1}{r^2} \left( 1 - 4 \frac{R_p}{r} \right) \right)$$

$$\approx \frac{4GM R_p}{r^3}$$

$$F_c - F_e = F_T$$

$$\frac{F_T}{m} \approx \frac{4GM R_p}{r^3}$$

WHAT IS THE 4 DOING HERE?

LET'S SAY FORCE NEEDED TO BREAK ROCK  
 $\propto$  AREA FACING STAR  $\times$  STRENGTH.

$$\propto \pi R_p^2 \sigma$$

$$F_T \propto \frac{GM_* R_p}{r^3} m = \pi R_p^2 \sigma$$

$$\frac{GM_* R_p}{r^3} \frac{4}{3} \pi R_p^3 \sigma = \pi R_p^2 \sigma$$

$$\frac{GM_*}{r^3} \frac{4}{3} \pi R_p^3 = R_p^{-2}$$

$$R_p \approx \left( \frac{GM_*}{r^3} \frac{4}{3} \pi \right)^{-\frac{1}{2}}$$

~~$\approx G \cdot 0.5 \cdot 6.7 \cdot 10^{-11}$~~

$$\approx \left( \frac{G \cdot 0.5 \cdot 2 \cdot 10^{30}}{(0.2 \cdot 7 \cdot 10^{12})^3} \frac{4}{3} \frac{3000}{100 \cdot 10^6} \right)^{-\frac{1}{2}} \approx 3 \cancel{\text{km}} \approx 3.2 \cdot 10^4 \text{ m}$$

$= R_{MAX}$

L SOLAR RADIES

FORCE PER UNIT MASS  
ON SURFACE:

$$G \frac{\frac{4}{3} \pi R_{MAX}^3}{R_{MAX}^2} = \frac{4}{3} \pi G J R_{MAX}$$

(BUT IDK WHAT TO DO w/ THIS)

"IF THE LUMINOSITY OF THE WD" ...

$$\begin{aligned} \text{POWER INCOMING} &= \frac{\pi R_{MAX}^2}{4\pi r^2} L \\ &= \frac{R_{MAX}}{4r^2} L \\ &= \frac{(3.2 \cdot 10^9)^2}{4(7 \cdot 10^8)} L \approx 5 \cdot 10^{10} L \approx 1.6 \cdot 10^{-8} L_\odot \\ L_\odot \approx 10^{26} W &\quad \swarrow \quad \searrow \\ \text{WARMING POWER} &\approx 10^{18} W \end{aligned}$$

THE ROCK WOULDN'T  
WITHSTAND THIS  
MUCH HEATING  
FOR LONG.

ON DIMENSIONAL GROUNDS:

POWER IN · TIME TO SUBLIME =  $\Delta H \cdot$  MASS OF ROCK.

$$t = \Delta H \cdot \frac{\frac{4}{3}\pi R_{MAX}^3 S}{P}$$

$$= \Delta H \cdot \frac{\frac{4}{3}\pi (3 \cdot 10^9)^3 3000}{10^{18}}$$

$$\approx 0.5 \Delta H$$

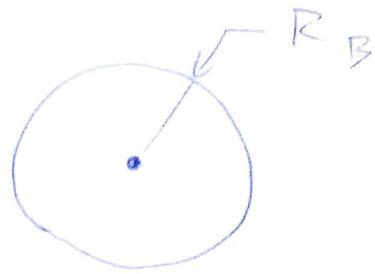
THIS NUMBER SEEMS  
SUSPICIOUSLY SMALL

"A ROCK OF RADIUS  $R > R_{MAX}$ "

PROBABLY HARDLY DOUBLE IF  
GOT PREVIOUS PART WRONG  
SO I'LL GO TO THE NEXT  
PROBLEM.

4.1

$$R_B = \frac{GM}{2c_s^2}$$



WEECHING FLUID  
STEED AT  $R_B$ :  $C_s$

MASS ACCRETING PER UNIT TIME

$$= C_s \underbrace{4\pi R_B^2 S}_{\text{RATE AREA}}$$

$$= C_s 4\pi \left(\frac{GM}{2c_s^2}\right)^2 S = \cancel{\left(\frac{GM}{2c_s^2}\right)^2} + \cancel{\pi} \frac{G^2 M^2}{C_s^3} S$$

CHECK DIMENSIONS:

$$\frac{m}{s^2} \cdot m^2 \frac{kg}{m^3} = \frac{kg}{s^2} \Rightarrow \text{OK}$$

~~THE EQUATION~~

$$\frac{dM}{dt} = \pi \frac{G^2 M^2}{C_s^3} S = \frac{\pi G^2 S}{C_s^3} M^2$$

~~THE EQUATION~~

$$\frac{dM}{M^2} = \frac{\pi G^2 S}{C_0^3} dt$$

$$-M^{-1} = \frac{\pi G^2 S}{C_0^3} t + C_0$$

WE WANT:  $-M(t)^{-1} = -M_0^{-1}$  AT  $t=0$   
 $\Rightarrow C_0 = -M_0^{-1}$

$$-M^{-1} = \underbrace{\frac{\pi G^2 S}{C_0^3} t}_{\text{CHECK DIMENSIONS}} - \frac{1}{M_0}$$

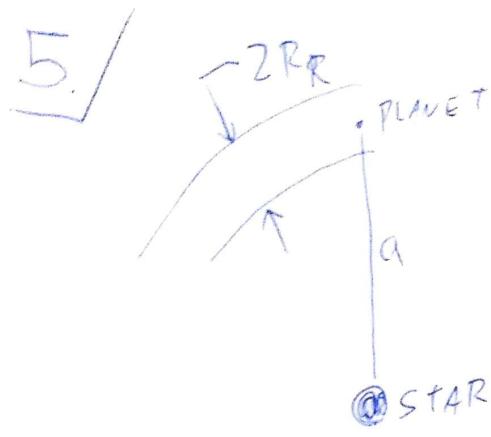
CHECK DIMENSIONS:  $\left(\frac{m^3}{kg\cdot s^2}\right)^2 \frac{kg}{m^3} \left(\frac{m}{s^2}\right)^{-3}$

$$= \frac{m^6 m^{-3} m^3 s^4}{kg\cdot s^4} = \frac{1}{kg} \Rightarrow G_{\text{new}}$$

$$M = \frac{1}{-\frac{\pi G^2 S}{C_0^3} t + \frac{1}{M_0}}$$

SO ILL GET TO  $\infty$  MASS IN VERY  
 FINITE TIME  $\Rightarrow$  THIS IS (RECT) WRONG.

OH, THE PROBLEM ALSO SAYS THIS CANNOT  
 HOLD INDEFINITELY, SO THERE'S HOPE.



ANGULAR MOMENTUM OF DISC:  $M \cancel{d} d \omega$

$$\frac{\omega^2}{a} = \frac{GM}{a^2} \Rightarrow \omega = \sqrt{\frac{GM}{a}}$$

$$L = M_d \underbrace{\sqrt{\frac{GM_*}{a}}}_{\text{ANNULUS}}$$

THIS TURNS INTO ROTATING THE PLANET.

$$L = I \omega = \frac{2}{5} M_{\text{PLANET}} R_{\text{PLANET}}^2 \frac{2\pi}{P_{\text{DAY}}}$$

$M_{\text{PLANET}} \approx M_{\text{ANNULUS}}$  BY END OF ACCRETION.

$$\Rightarrow a \sqrt{\frac{GM_*}{a}} = \frac{2}{5} R_p^2 \frac{2\pi}{P_{\text{DAY}}}$$

$$\frac{5}{2} \sqrt{Na} \frac{1}{R_p^2} \frac{1}{2\pi} = P_{\text{DAY}}^{-1}$$

$$P_{\text{DAY}} = \frac{4\pi}{5} \frac{R_p^2}{\sqrt{Na}} \neq \frac{2}{5} \frac{R_p^2}{\sqrt{Na}}$$

SO I DID SOMETHING WRONG.

USING GIVEN FORMUL

$$T_{\text{DAY}} = \frac{2}{3} \sqrt{\frac{(10 \cdot 6400 \cdot 10^3)^2}{(6.67 \cdot 10^{-30} \cdot 150 \cdot 10^9)^{1/2}}}$$

~~ANS~~ (?)  
= 0.6 SEC

IF THIS IS CORRECT, PLANET ISN'T STABLE.