

# Assignment 1

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	Materials required	Profit/unit	Time required
Collegiate →	3 sq.ft	\$32	45 mins
Minis →	2 sq.ft	\$24	40 mins

⇒ Total materials available = 5000 sq.ft.

⇒ Total available hours of labour/week = Total employees \* No. of hours each employee works/week

$$= 35 \times 40 = 1400 \text{ hours}$$

⇒ Let  $P$  be the total profit

$C$  be the no. of collegiate manufactured

$M$  be the no. of Minis manufactured

$$\therefore \text{Maximize}(P) = 32 * C + 24 * M$$

$$0 \leq C \leq 1000$$

$$0 \leq M \leq 1200$$

\* Material constraints:

$$3C + 2M \leq 5000$$

\* Time constraints:

$$\frac{3C}{4} + \frac{2M}{3} \leq 1400$$

45 mins → hours

$$= \frac{45}{60} = \frac{3}{4} \text{ hr}$$

40 mins → hours

$$= \frac{40}{60} = \frac{2}{3} \text{ hr}$$

① Decision variable

$P$  = Total profit

$C$  = no. of collegiate manufactured

$M$  = no. of Minis manufactured

⑤ Objective function

$$\text{Maximize (P)} = 32 * C + 24 * M$$

subject to

⑥ Constraints

$$3C + 2M \leq 5000 \text{ (material constraints)}$$

$$\frac{3}{4}C + \frac{2}{3}M \leq 1400 \text{ (time constraints)}$$

$$0 \leq C \leq 1000$$

$$0 \leq M \leq 1200$$

{ sales forecast limit for  
colligate & Minis }

(Non-negativity of decision  
variables)

# ① Mathematical Formulation

$$\text{Maximize } (P) = 32 * C + 24 * M \quad (\text{objective function})$$

subject to

$$3C + 2M \leq 5000 \quad (\text{material constraints})$$

$$\frac{3}{4}C + \frac{2}{3}M \leq 1400 \quad (\text{time constraints})$$

$$0 \leq C \leq 1000$$

$$0 \leq M \leq 1200$$

{ sales forecast limit,  
non-negativity of decision variables)

Plant	Excess capacity	Storage space
Plant 1	750 units / day	13,000 sq. ft
Plant 2	900 units / day	12,000 sq. ft
Plant 3	450 units / day	5000 sq. ft

Plant size	Profit/unit	Material/unit	Sales/day
Large	\$420	20 sq. ft	900
Medium	\$360	15 sq. ft	1200
Small	\$300	12 sq. ft	750

et  $N =$  no. of units produced

consider  $N(x, y)$

where  $x = (1, 2, 3) \rightarrow$  Plant number

$y = (L, M, S) \rightarrow$  size of product produced.

eg:  $N_2 M =$  no. of units of medium products produced in plant 2.

Objective function

let  $P =$  profit

$$\text{Maximize } P = 420 (N_1 L + N_2 L + N_3 L) + 360 (N_1 M + N_2 M + N_3 M) + 300 (N_1 S + N_2 S + N_3 S)$$

$N_{1L} \Rightarrow$  no. of units of large product in plant ①

$N_{2L} \Rightarrow$  " " plant ②

$N_{3L} \Rightarrow$  " " plant ③

$N_{1M} \Rightarrow$  no. of units of medium product produced in plant ①

$N_{2M} \Rightarrow$  " " plant ②

$N_{3M} \Rightarrow$  " " plant ③

$N_{1S} \Rightarrow$  no. of units of small product produced in plant ①

$N_{2S} \Rightarrow$  " " plant ②

$N_{3S} \Rightarrow$  " " plant ③

where  $N(x, y) \rightarrow$

$$N_{xy} \geq 0$$

(non-negativity constraints)

## Constraints

### ① Excess capacity constraints

$$\text{Plant ①} \Rightarrow N_{1L} + N_{1M} + N_{1S} \leq 750$$

(for plant 1)

$$\text{Plant ②} \Rightarrow N_{2L} + N_{2M} + N_{2S} \leq 900$$

$$\text{Plant ③} \Rightarrow N_{3L} + N_{3M} + N_{3S} \leq 450$$

### ② Space constraints

$$\text{Plant ①} \Rightarrow 20N_{1L} + 15N_{1M} + 12N_{1S} \leq 13,000$$

$$\text{Plant ②} \Rightarrow 20N_{2L} + 15N_{2M} + 12N_{2S} \leq 12,000$$

$$\text{Plant ③} \Rightarrow 20N_{3L} + 15N_{3M} + 12N_{3S} \leq 5000$$

### ③ Sales as per forecast

$$\text{Plant ①} \Rightarrow N_{1L} + N_{1M} + N_{1S} \leq 900$$

$$\text{Plant ②} \Rightarrow N_{2L} + N_{2M} + N_{2S} \leq 1200$$

$$\text{Plant ③} \Rightarrow N_{3L} + N_{3M} + N_{3S} \leq 750$$

### ④ Percentage of excess capacity to avoid layoffs

$$\text{Plant ①} \Rightarrow \frac{N_{1L} + N_{1M} + N_{1S}}{750} \times 100$$

$$\text{Plant ②} \Rightarrow \frac{N_{2L} + N_{2M} + N_{2S}}{900} \times 100$$

$$\text{Plant ③} \Rightarrow \frac{N_{3L} + N_{3M} + N_{3S}}{450} \times 100$$