

IN EXAMPLE 11.4, LET  $a=0$  AND  $b=\frac{1}{2}$ . FIND  $P$ ,  $P^2$ , AND  $P^3$ . WHAT WOULD  $P^n$  BE? WHAT HAPPENS TO  $P^n$  AS  $n$  TENDS TO INFINITY? INTERPRET THIS RESULT.

$$P = \begin{bmatrix} 1-a & a \\ b & 1-b \end{bmatrix} \quad a=0 \quad b=\frac{1}{2}$$

$$P = \begin{bmatrix} 1 & 0 \\ 0.5 & 0.5 \end{bmatrix} \quad \leftarrow \text{ANSWER}$$

$$P^2 = \begin{bmatrix} 1 & 0 \\ 0.5 & 0.5 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 \\ 0.5 & 0.5 \end{bmatrix} = \begin{bmatrix} (1+0) & (0+0) \\ (0.5+0.25) & (0+0.25) \end{bmatrix}$$

$$P^2 = \begin{bmatrix} 1 & 0 \\ 0.75 & 0.25 \end{bmatrix} \quad \leftarrow \text{ANSWER}$$

$$P^3 = \begin{bmatrix} 1 & 0 \\ 0.5 & 0.5 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 \\ 0.75 & 0.25 \end{bmatrix} = \begin{bmatrix} (1+0) & (0+0) \\ (0.5+0.375) & (0+0.125) \end{bmatrix}$$

$$P^3 = \begin{bmatrix} 1 & 0 \\ 0.875 & 0.125 \end{bmatrix}$$

$\nearrow$   
ANSWER

AS WE CAN SEE, AS  $P^n$  TENDS TO INFINITY,

$$P^n = \begin{bmatrix} 1 & 0 \\ 1-(0.5)^n & (0.5)^n \end{bmatrix} \rightarrow \lim_{n \rightarrow \infty} P^n = \begin{bmatrix} 1 & 0 \\ 1 & 0 \end{bmatrix}$$

$\nearrow$   
ANSWER