


# Modelling the Deterioration of Infrastructures Using Network-Scale Visual Inspections

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MTQ  
Partner

# Definitions

Visual Inspections (VI): Network-scale monitoring technique

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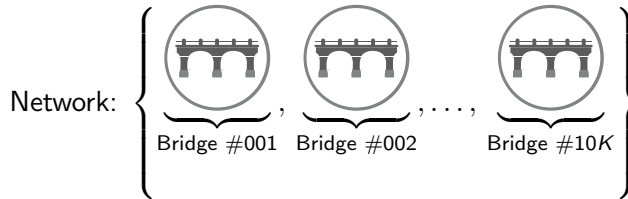
Visual Inspections (VI): Network-scale monitoring technique

Network:

Source: Google images

# Definitions

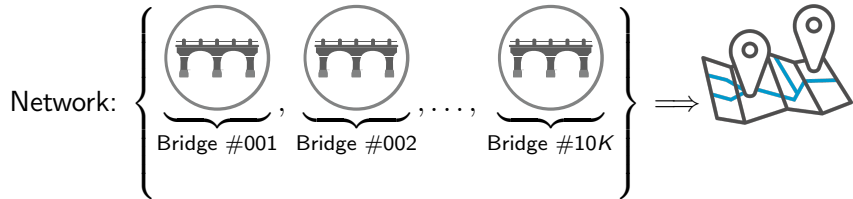
Visual Inspections (VI): Network-scale monitoring technique



Source: Google images

# Definitions

Visual Inspections (VI): Network-scale monitoring technique

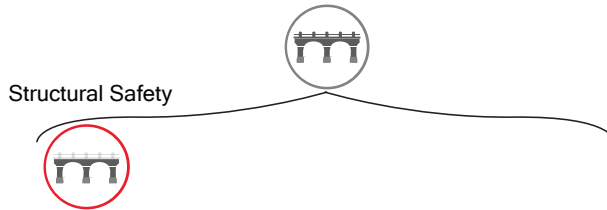


Source: Google images

# Data Hierarchy

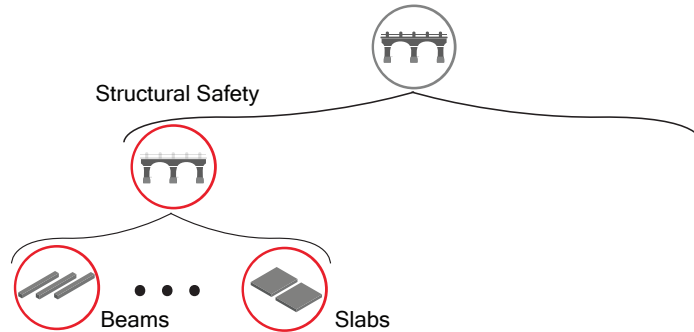


# Data Hierarchy



Source: MTQ, Manual of Inspection

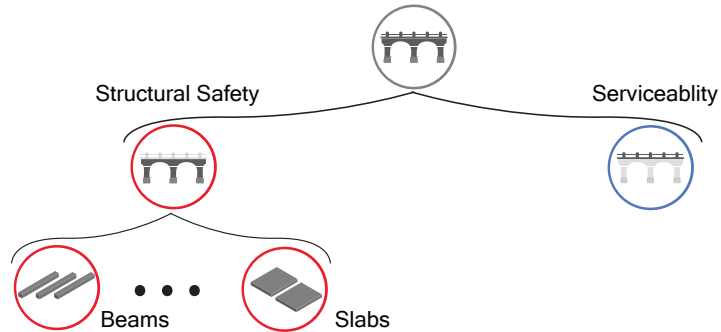
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Source: MTQ, Manual of Inspection

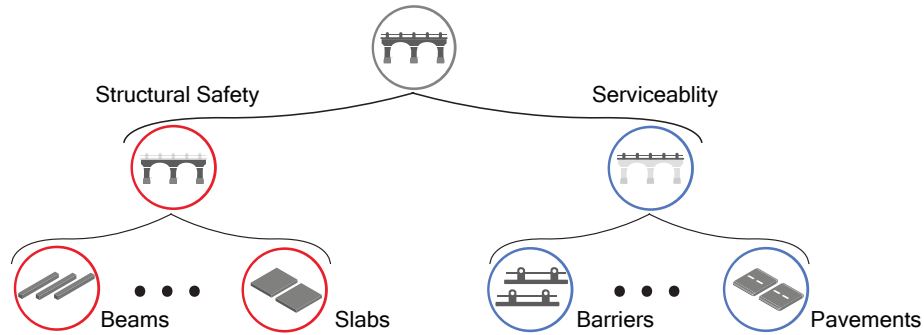


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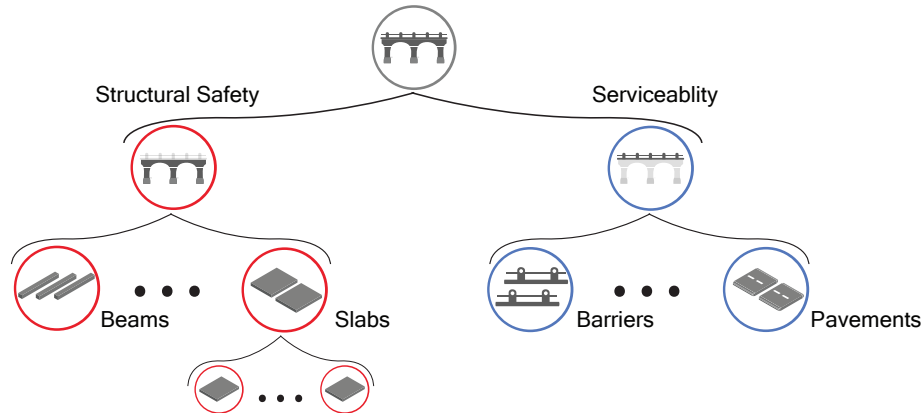
Source: MTQ, Manual of Inspection

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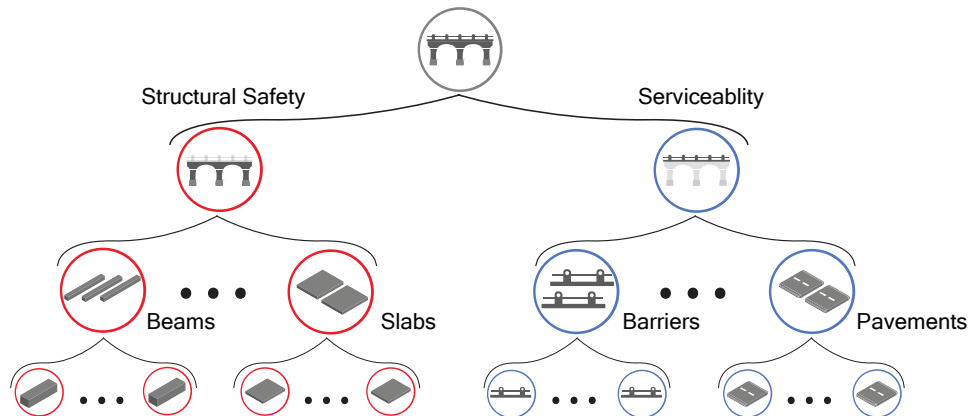
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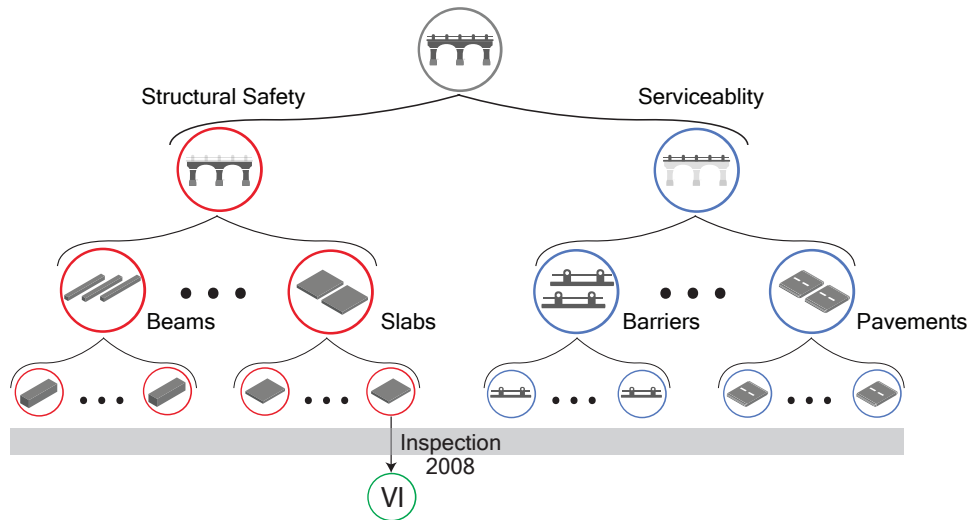
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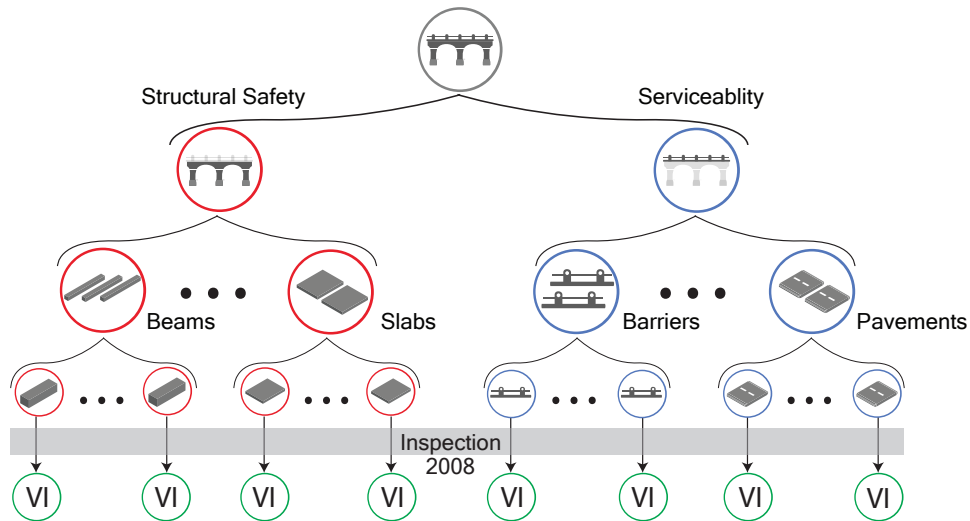
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Source: MTQ, Manual of Inspection

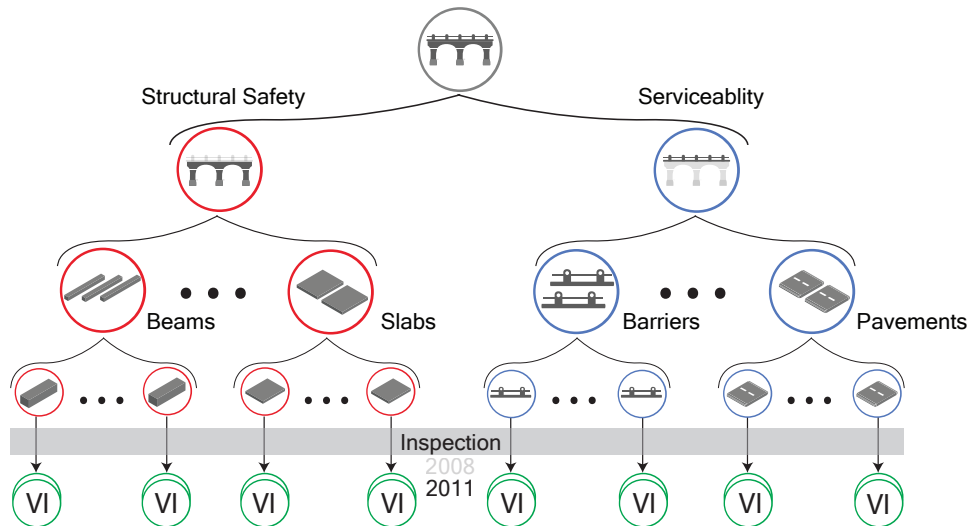
Polytechnique Montréal

# Data Hierarchy



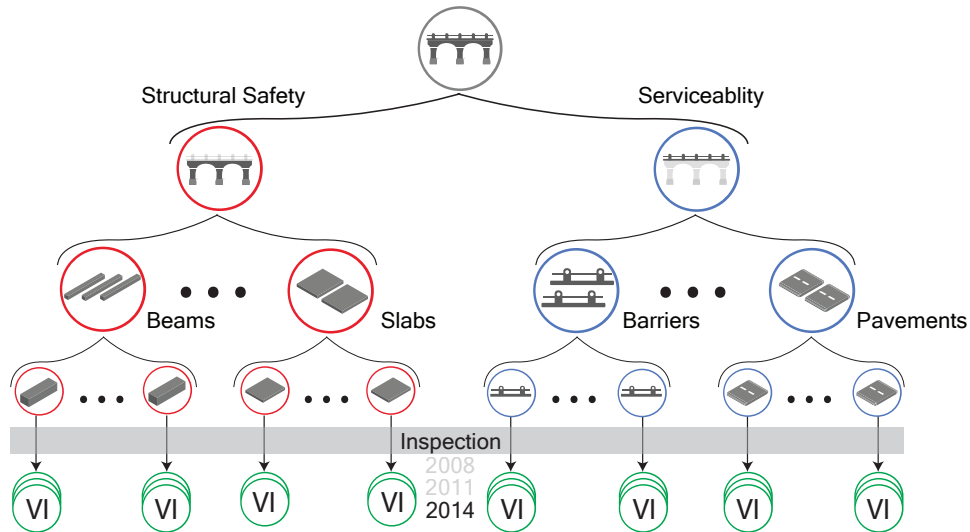
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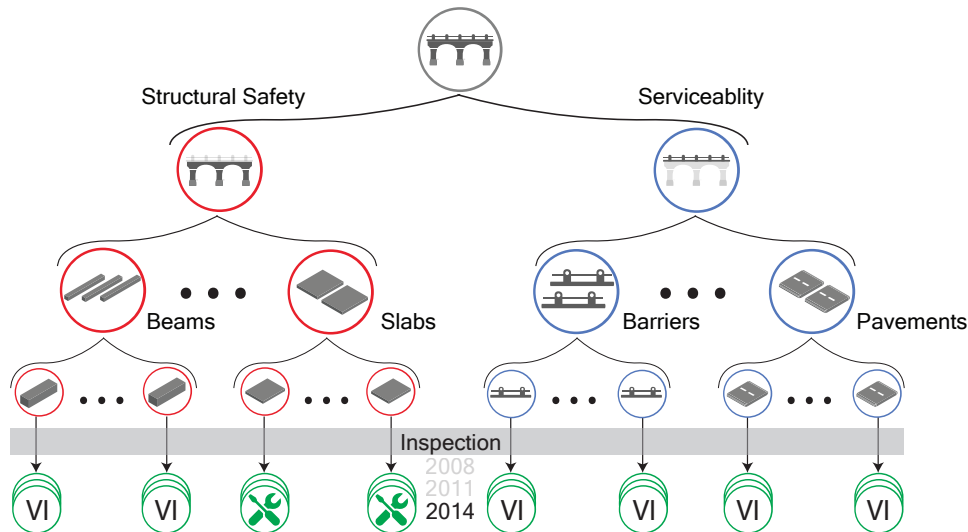
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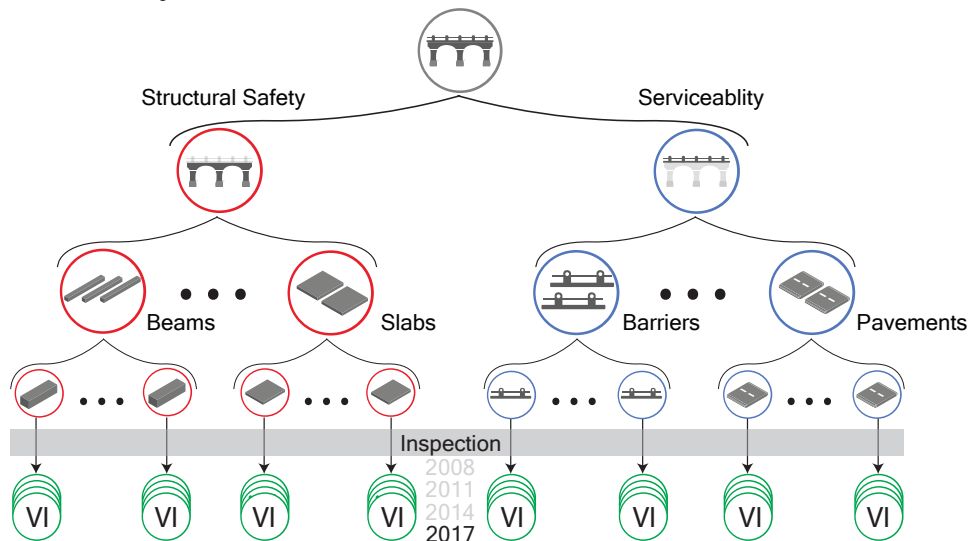


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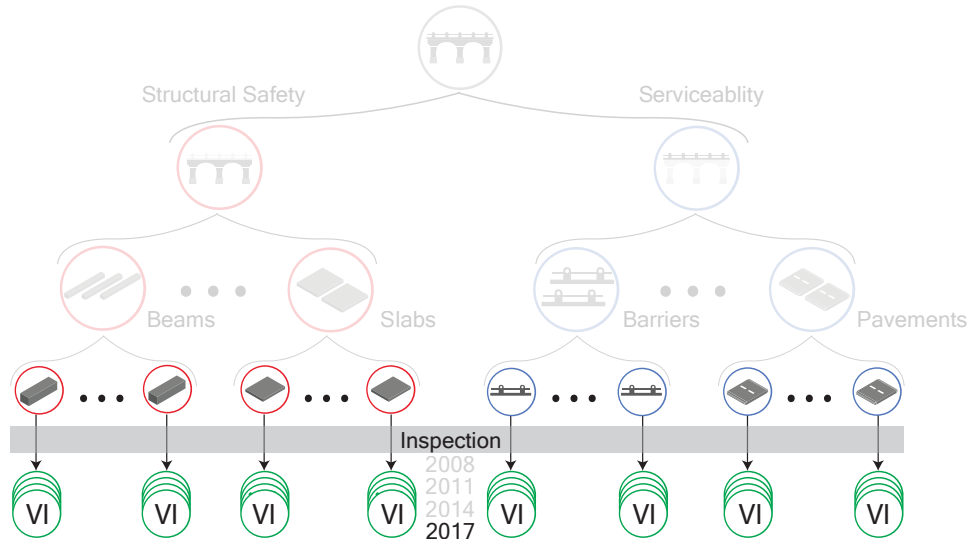
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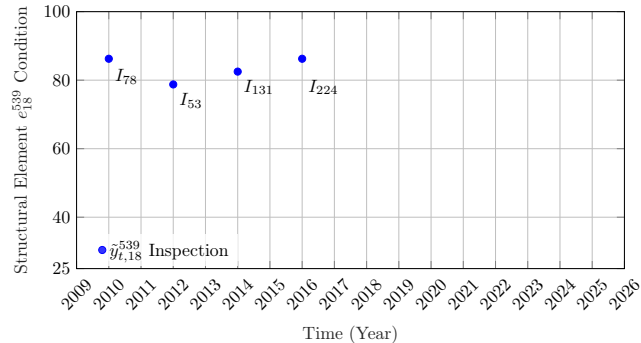
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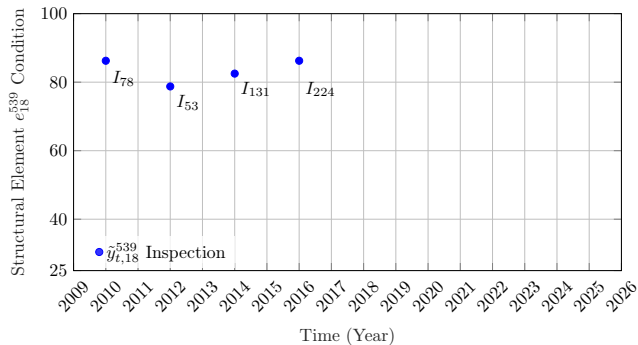
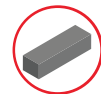


Source: MTQ, Manual of Inspection

# Example of Visual Inspections on a Structural Element

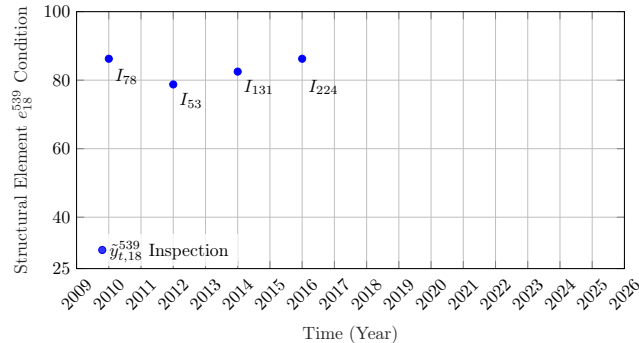


# Example of Visual Inspections on a Structural Element



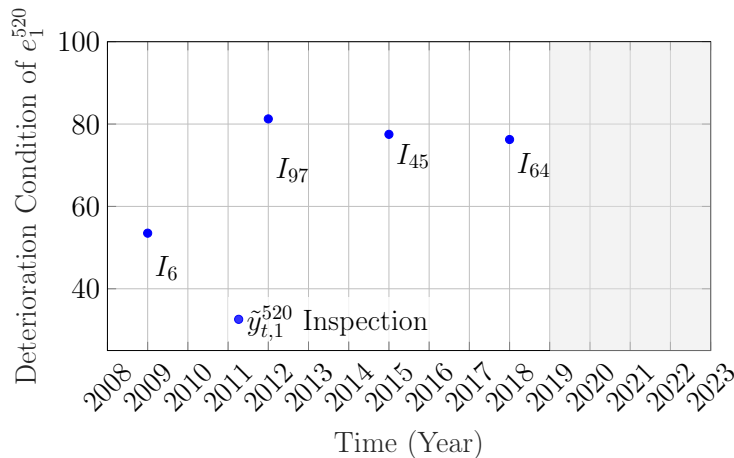
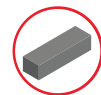
Limited data.

# Example of Visual Inspections on a Structural Element

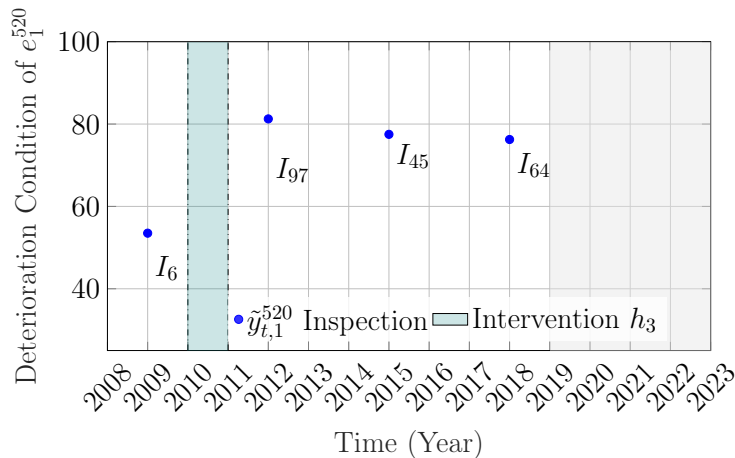


- ✓ Limited data.
- ✓ Subjective (high variability + different inspectors).

# Example of Visual Inspections with an Intervention

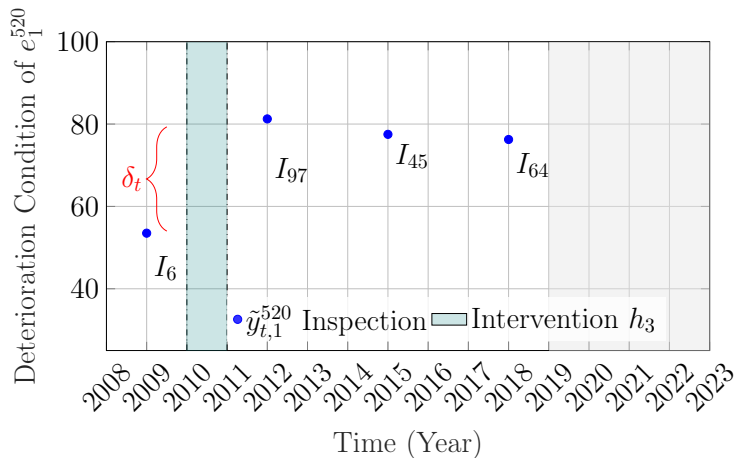


# Example of Visual Inspections with an Intervention





# Example of Visual Inspections with an Intervention



# Objectives

- **Modelling infrastructures deterioration** from network-scale visual inspections.

# Objectives

- ▶ **Modelling infrastructures deterioration** from network-scale visual inspections.
- ▶ Quantifying the **effects of interventions** based on visual inspections.

# Deterioration Behaviour Described by Kinematics

Kinematic Equations

$$x_{t+1} = x_t + \dot{x}_t \Delta t + \frac{1}{2} \ddot{x}_t \Delta t^2 + w \quad (\text{Condition})$$

Source: Hamida and Goulet, 2020

# Deterioration Behaviour Described by Kinematics

Kinematic Equations

$$\begin{aligned}x_{t+1} &= x_t + \dot{x}_t \Delta t + \frac{1}{2} \ddot{x}_t \Delta t^2 + w && \text{(Condition)} \\ \dot{x}_{t+1} &= \dot{x}_t + \ddot{x}_t \Delta t + \dot{w} && \text{(Speed)}\end{aligned}$$

Source: Hamida and Goulet, 2020

# Deterioration Behaviour Described by Kinematics

## Kinematic Equations

$$\begin{array}{lll} x_{t+1} & = & x_t + \dot{x}_t \Delta t + \frac{1}{2} \ddot{x}_t \Delta t^2 + w \quad (\text{Condition}) \\ \dot{x}_{t+1} & = & \dot{x}_t + \ddot{x}_t \Delta t + \dot{w} \quad (\text{Speed}) \\ \ddot{x}_{t+1} & = & \ddot{x}_t + \ddot{w} \quad (\text{Acceleration}) \end{array}$$

Source: Hamida and Goulet, 2020

# Deterioration Behaviour Described by Kinematics

$$\underbrace{\begin{bmatrix} x_t \\ \dot{x}_t \\ \ddot{x}_t \end{bmatrix}}_{\mathbf{x}_t} = \underbrace{\begin{bmatrix} 1 & \Delta t & \frac{\Delta t^2}{2} \\ 0 & 1 & \Delta t \\ 0 & 0 & 1 \end{bmatrix}}_{\mathbf{A}} \cdot \underbrace{\begin{bmatrix} x_{t-1} \\ \dot{x}_{t-1} \\ \ddot{x}_{t-1} \end{bmatrix}}_{\mathbf{x}_{t-1}} + \underbrace{\begin{bmatrix} w_t \\ \dot{w}_t \\ \ddot{w}_t \end{bmatrix}}_{\mathbf{w}_t}$$

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## Method: State-Space Models

Source: Hamida and Goulet, 2020



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## Method: State-Space Models

transition model

$$\mathbf{x}_t = \mathbf{A}\mathbf{x}_{t-1} + \mathbf{w}_t$$

Source: Hamida and Goulet, 2020

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## Method: State-Space Models

transition model

$$\underbrace{\mathbf{x}_t = \mathbf{A}\mathbf{x}_{t-1} + \mathbf{w}_t}_{\text{process error}}, \quad \underbrace{\mathbf{w}_t : \mathbf{W} \sim \mathcal{N}(\mathbf{w}; \mathbf{0}, \mathbf{Q}_t)}_{\text{process error}}$$

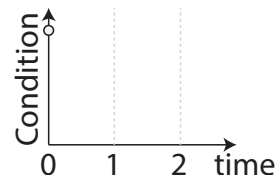
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## Method: State-Space Models

$$\underbrace{\mathbf{x}_t = \mathbf{A}\mathbf{x}_{t-1} + \mathbf{w}_t}_{\text{transition model}}, \underbrace{\mathbf{w}_t : \mathbf{W} \sim \mathcal{N}(\mathbf{w}; \mathbf{0}, \mathbf{Q}_t)}_{\text{process error}}$$



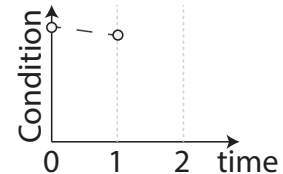
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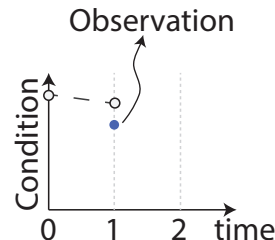
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## Method: State-Space Models

$$\underbrace{x_t = Ax_{t-1} + w_t}_{\text{transition model}}, \underbrace{w_t : W \sim \mathcal{N}(w; 0, Q_t)}_{\text{process error}}$$



Source: Hamida and Goulet, 2020

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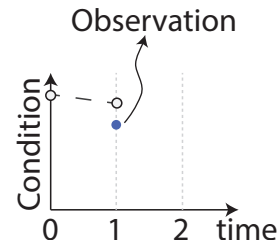
## Method: State-Space Models

transition model

$$\mathbf{x}_t = \mathbf{A}\mathbf{x}_{t-1} + \mathbf{w}_t, \quad \underbrace{\mathbf{w}_t : \mathbf{W} \sim \mathcal{N}(\mathbf{w}; \mathbf{0}, \mathbf{Q}_t)}_{\text{process error}}$$

observation model

$$y_t = \mathbf{C}\mathbf{x}_t + v_t$$



Source: Hamida and Goulet, 2020

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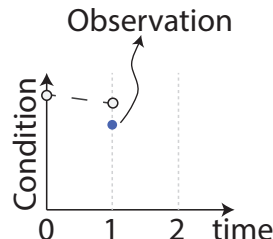
## Method: State-Space Models

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observation model

$$y_t = \mathbf{C}\mathbf{x}_t + v_t, \quad \underbrace{v_t : V \sim \mathcal{N}(v; 0, \sigma_V^2)}_{\text{observation error}}$$



Source: Hamida and Goulet, 2020

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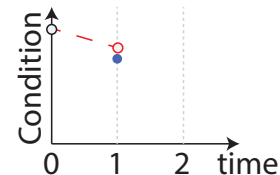
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observation model

$$\underbrace{y_t = \mathbf{C}x_t + v_t}_{\text{observation model}}, \quad \underbrace{v_t : V \sim \mathcal{N}(v; 0, \sigma_V^2)}_{\text{observation error}}$$



Source: Hamida and Goulet, 2020



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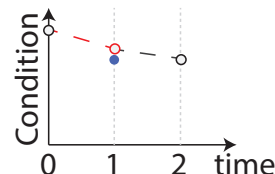
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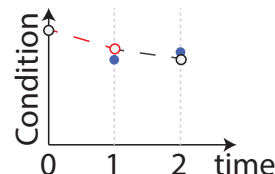
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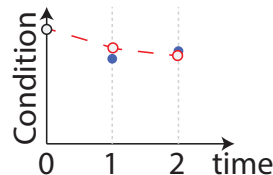
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Source: Hamida and Goulet, 2020

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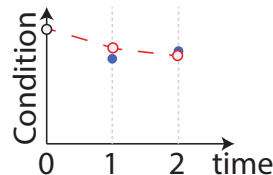
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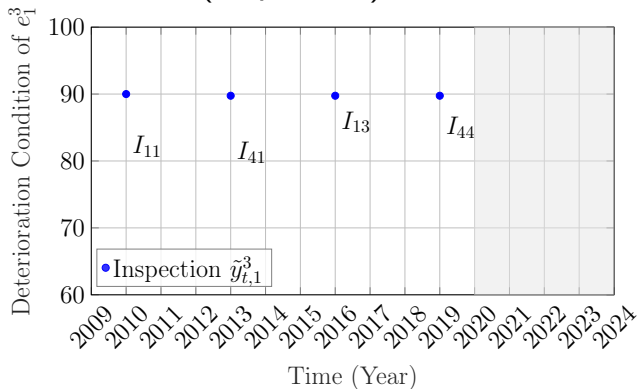
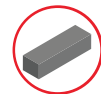


Source: Hamida and Goulet, 2020

# Uncertainty of Observations (Inspectors)



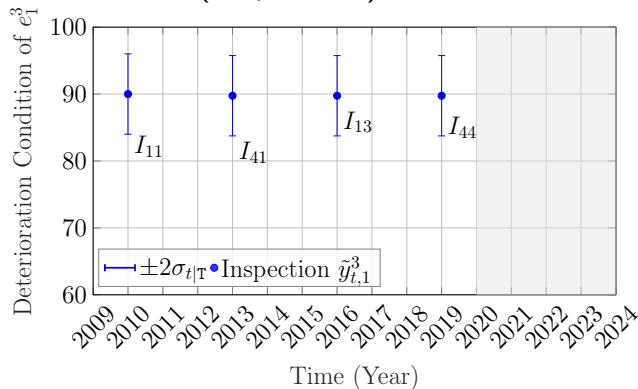
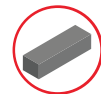
# Uncertainty of Observations (Inspectors)



observation model

$$y_t = \mathbf{C}\mathbf{x}_t + v_t, \quad \underbrace{v_t : V \sim \mathcal{N}(v; 0, \sigma_V^2)}_{\text{observation error}}$$

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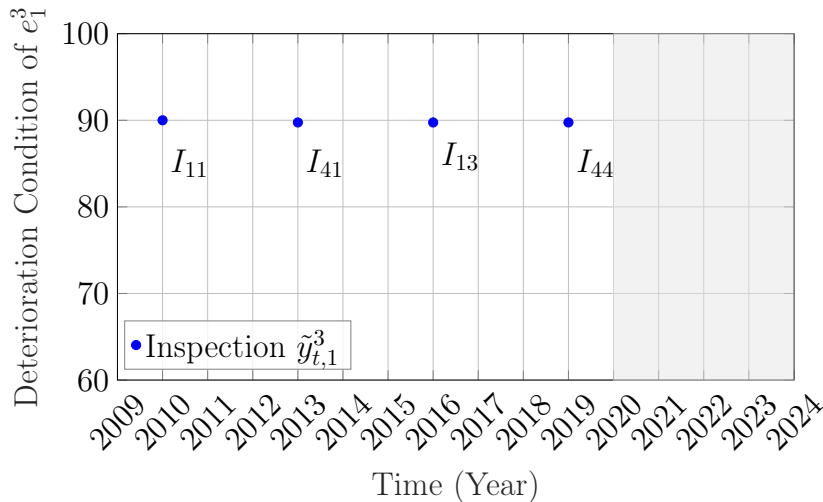
# Uncertainty of Observations (Inspectors)



$$\underbrace{y_t = \mathbf{C}\mathbf{x}_t + v_t}_{\text{observation model}}, \underbrace{v_t : V(l_i) \sim \mathcal{N}(v; \mu_V(l_i), \sigma_V^2(l_i))}_{\text{observation error}}$$

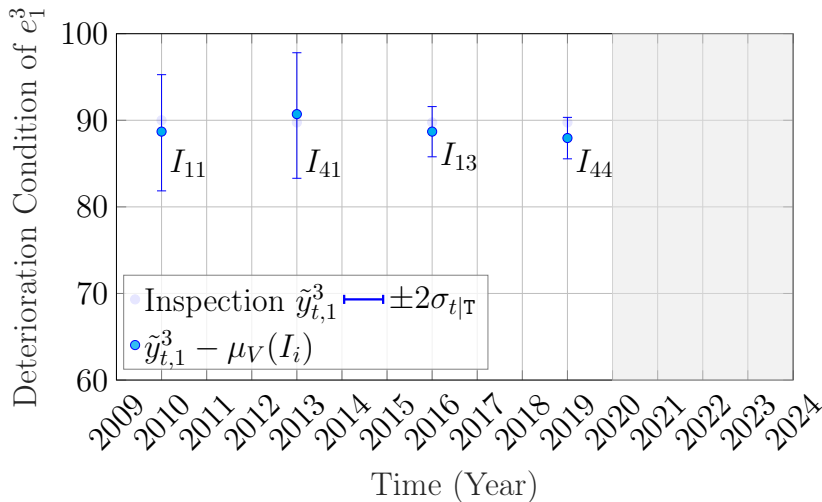


## Example of a Beam Structural Element



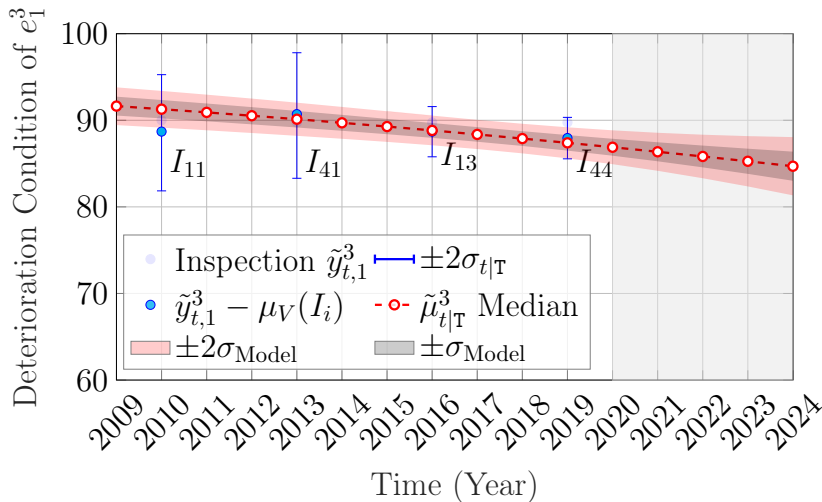
Source: Hamida and Goulet, 2020

## Example of a Beam Structural Element



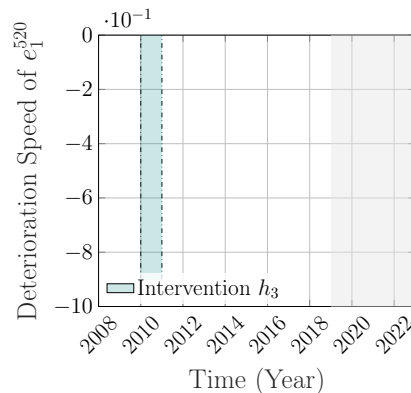
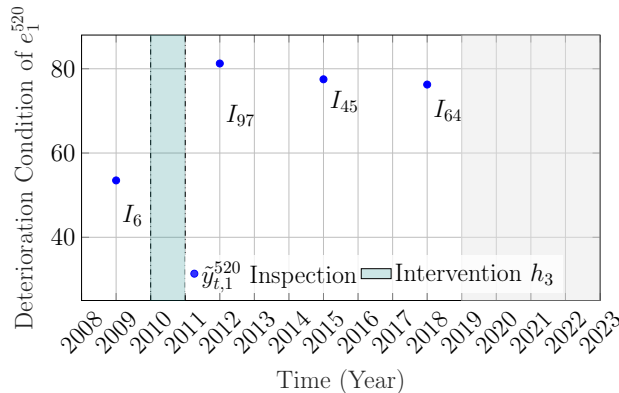
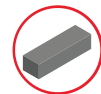
Source: Hamida and Goulet, 2020

## Example of a Beam Structural Element



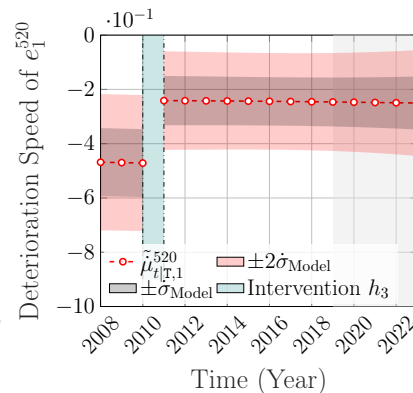
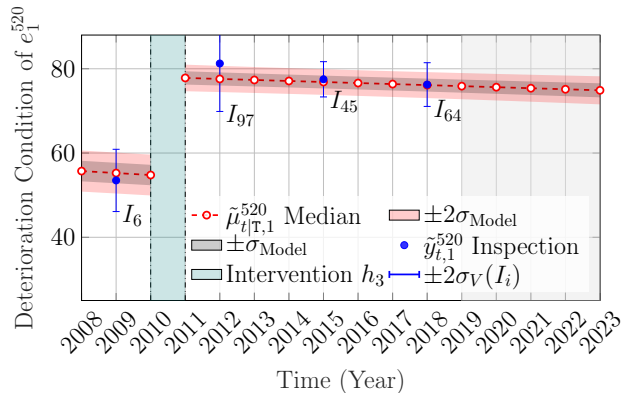
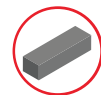
Source: Hamida and Goulet, 2020

# Structural Element Underwent Reparation



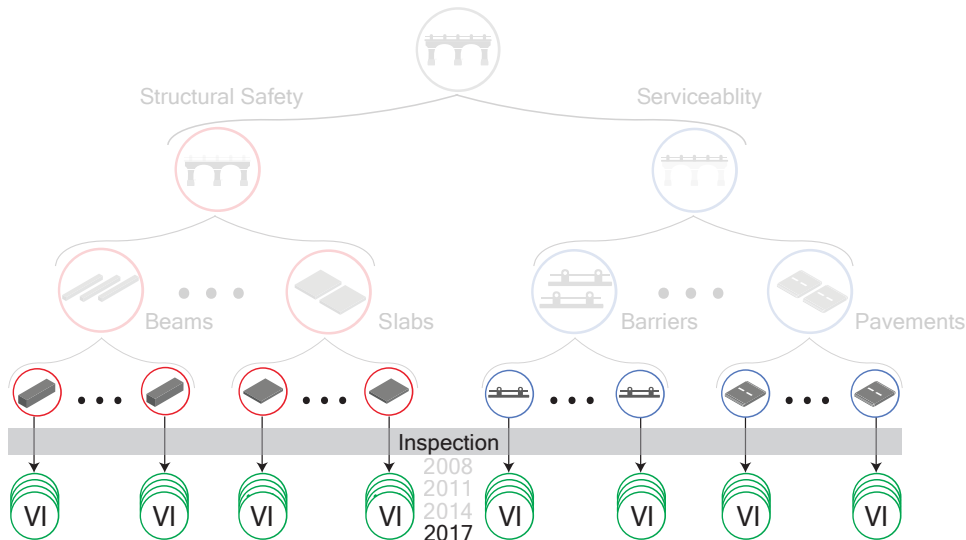
Source: Hamida and Goulet, 2021

# Structural Element Underwent Reparation



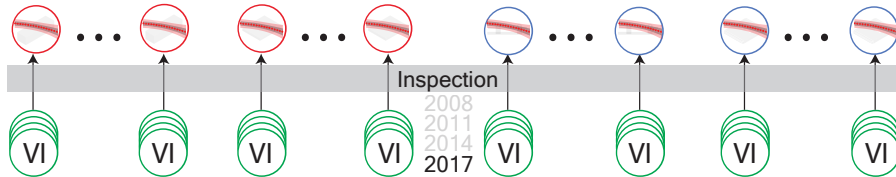
Source: Hamida and Goulet, 2021

# Bridge Components



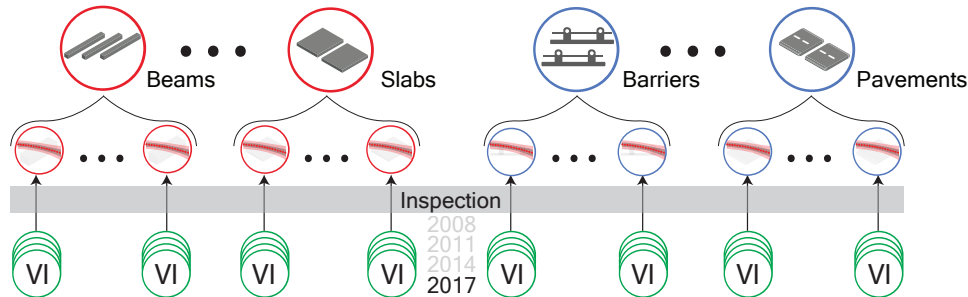
Source: FHWA Manual of Inspection, 2002

# Bridge Components



Source: V. Hamida &amp; J.-A. Goulet, 2022

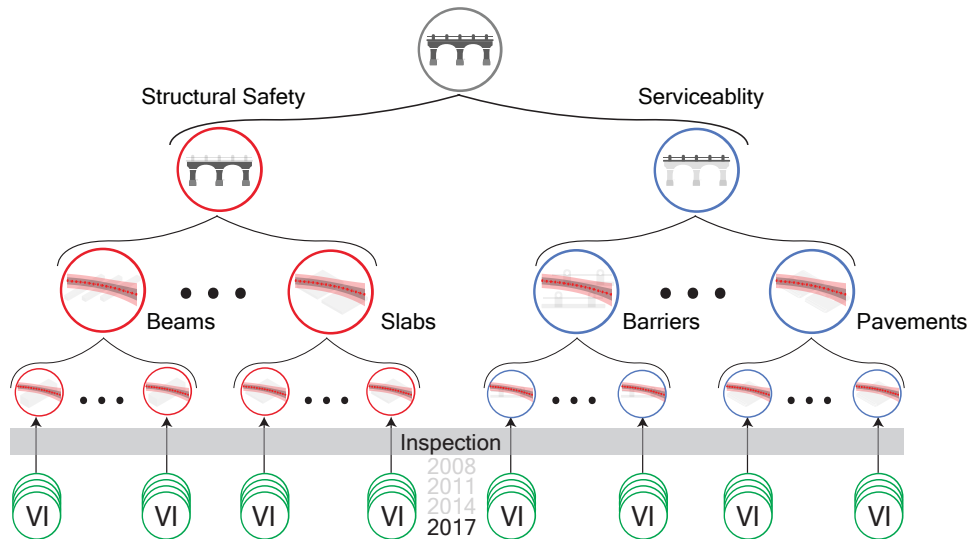
# Bridge Components



Source: FHWA, Manual of Inspection, 2008

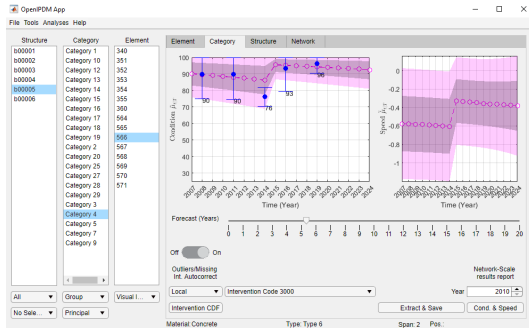


# Bridge Components




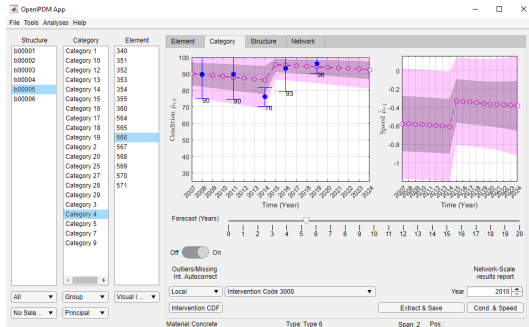
Source: VITQ, Hamida &amp; Goulet, 2022

# OpenIPDM

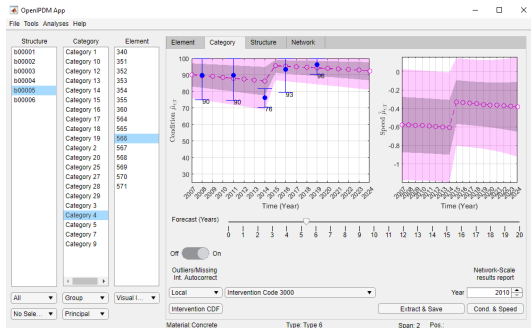



**OpenIPDM**

- Open-source software developed in MATLAB. 

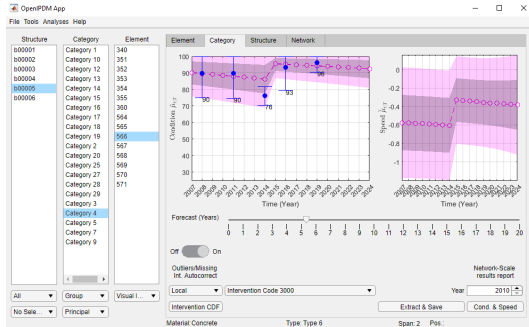



# OpenIPDM



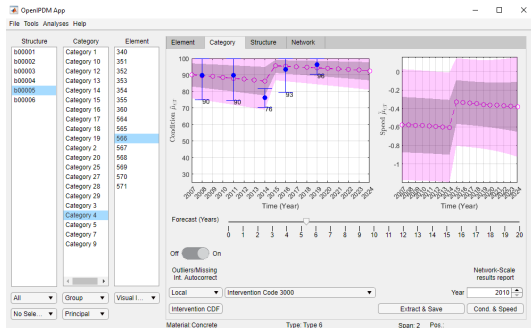
- Open-source software developed in MATLAB. 
- Infrastructures Probabilistic Deterioration Modeling.


# OpenIPDM



- Open-source software developed in MATLAB. 
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- User Interface.

# OpenIPDM



► Open-source software developed in MATLAB. 

► Infrastructures Probabilistic Deterioration Modeling.

► User Interface.

The software **OpenIPDM** is **available**

**online** on  **GitHub**

► <https://github.com/CivML-PolyMtl/OpenIPDM>