

MATHEMATICAL MODELING OF CELL-FREE PROTEIN SYNTHESIS

Presented By: M.A.A. Aqeel
Supervised By: Dr. S.P. Rajapaksha

University of Sri Jayewardenepura

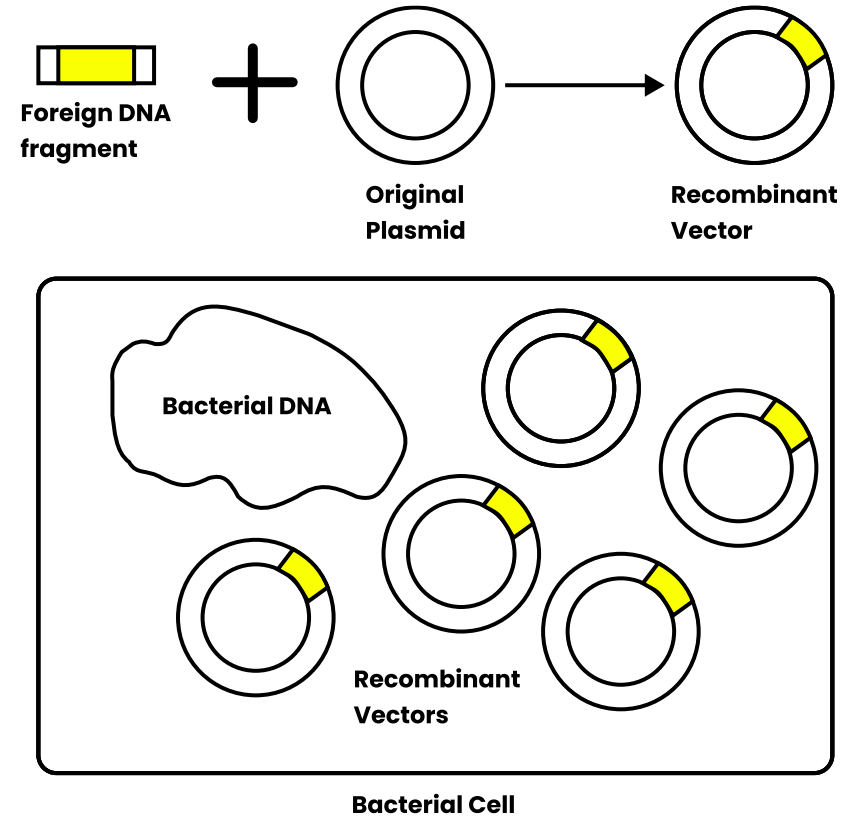


INTRODUCTION

INTRODUCTION TO CELL-FREE PROTEIN SYNTHESIS

Genetic Engineering

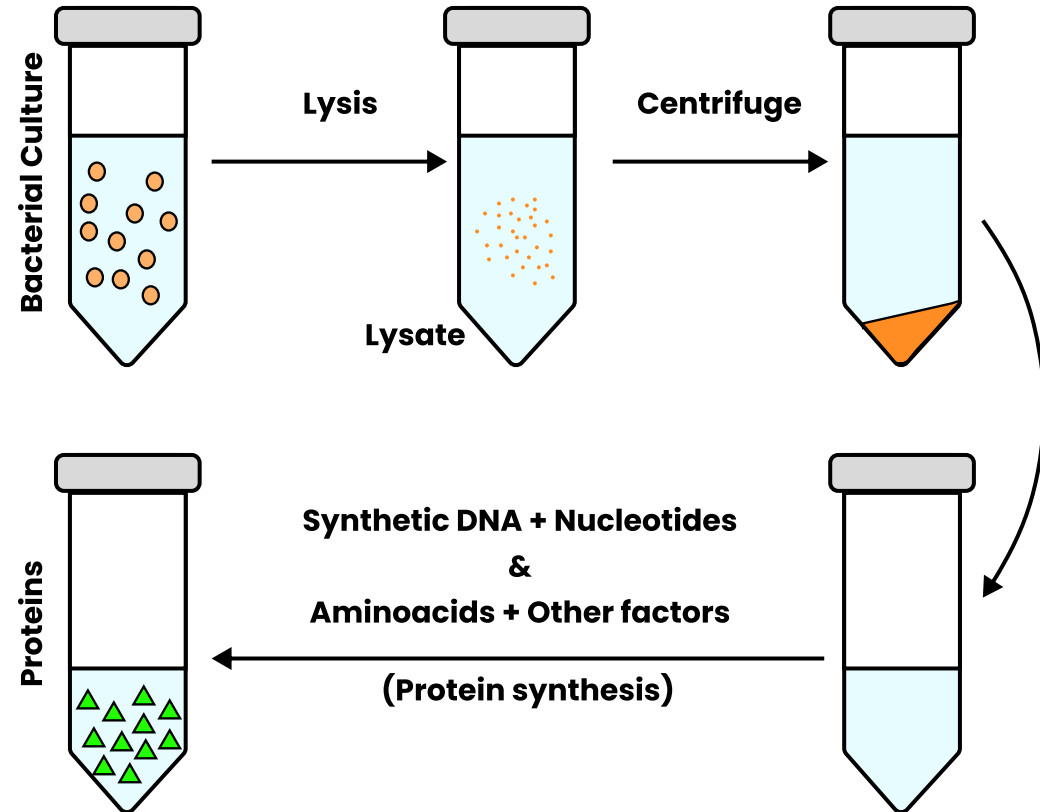
- Most therapeutic proteins are difficult to manufacture with available synthetic capabilities
- Microbial cultures can be utilized through *genetic engineering* to produce such complex molecules
- However, the product yield will be changed according to the nutritional and environmental conditions confronted by cells/culture



INTRODUCTION TO CELL-FREE PROTEIN SYNTHESIS

Cell-free protein synthesis (CFPS)

- Extracting and assembling the necessary molecular components of protein synthesis into a vessel can avoid confounding results associated with cell-based systems
- Executing DNA programs in a cell-free format can open new avenues for biomanufacturing and metabolic engineering



INTRODUCTION TO CELL-FREE PROTEIN SYNTHESIS

Applications of CFPS

- Monoclonal antibody production
- Vaccines
- Analyzing metabolic and genetic disorders
- Synthesis of non-canonical proteins
- Synthesis of niche drugs
- Membrane proteins
- Prototyping metabolic circuits
- Antimicrobial peptides

Limitations of CFPS

- Cost of synthesizing desired DNA template
- Resource exhaustion
- Inherent ribonuclease and protease activity
- Short active duration
- Small batch size

OBJECTIVES

General Objective

- To develop a minimalistic mathematical model that grasps the basic mechanics of protein synthesis in CFPS systems

Specific Objectives

- To understand the CFPS system towards DNA template loading capacity
- To understand the model behavior towards the consumption of biological nutrients
- To check the influence of inherent factors of the extract on active duration
- To provide better designs for CFPS Design-Build-Test-Learn (CFPS-DBTL) workflow



MODEL DEVELOPMENT

MODEL DEVELOPMENT

STEP 1

Literature survey on cell-free protein synthesis

SCIENTIFIC REPORTS

OPEN

High-yield production of “difficult-to-express” proteins in a continuous exchange cell-free system based on CHO cell lysates

Lena Thoring^{1,2}, Srujan K. Dondapati¹, Marlitt Stech¹, Doreen A. Wüstenhagen¹ & Stefan Kubick¹


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SCIENTIFIC
REPORTS
nature research

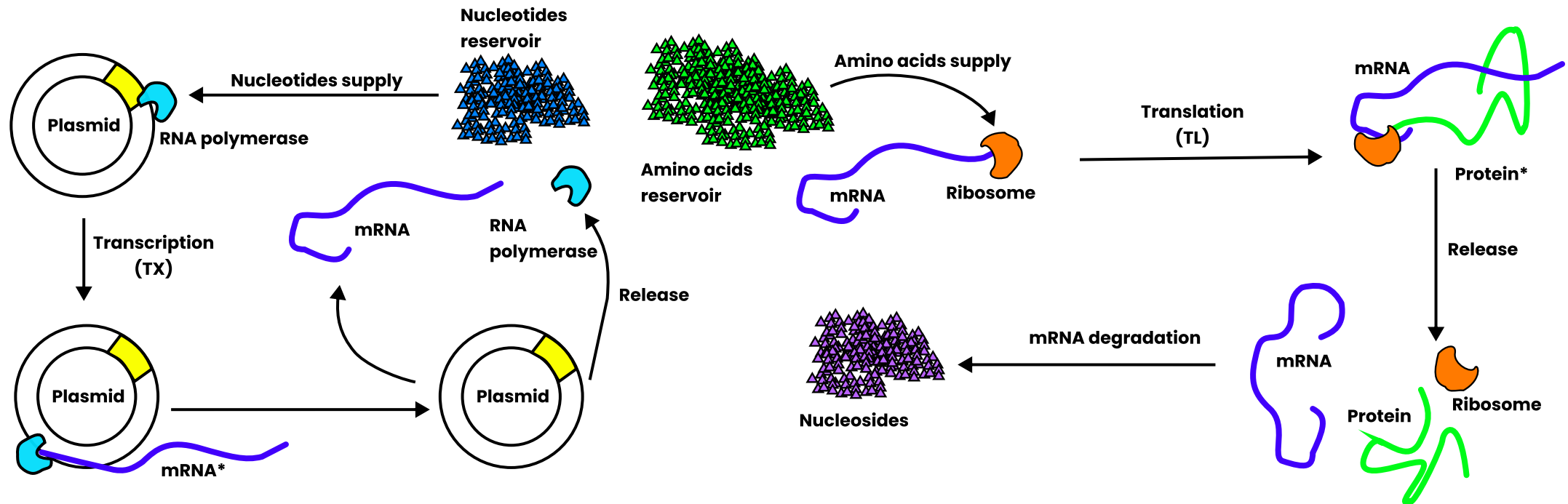
Quantitative modeling of transcription and translation of an all-*E. coli* cell-free system

Ryan Marshall & Vincent Noireaux 

MODEL DEVELOPMENT

STEP 2

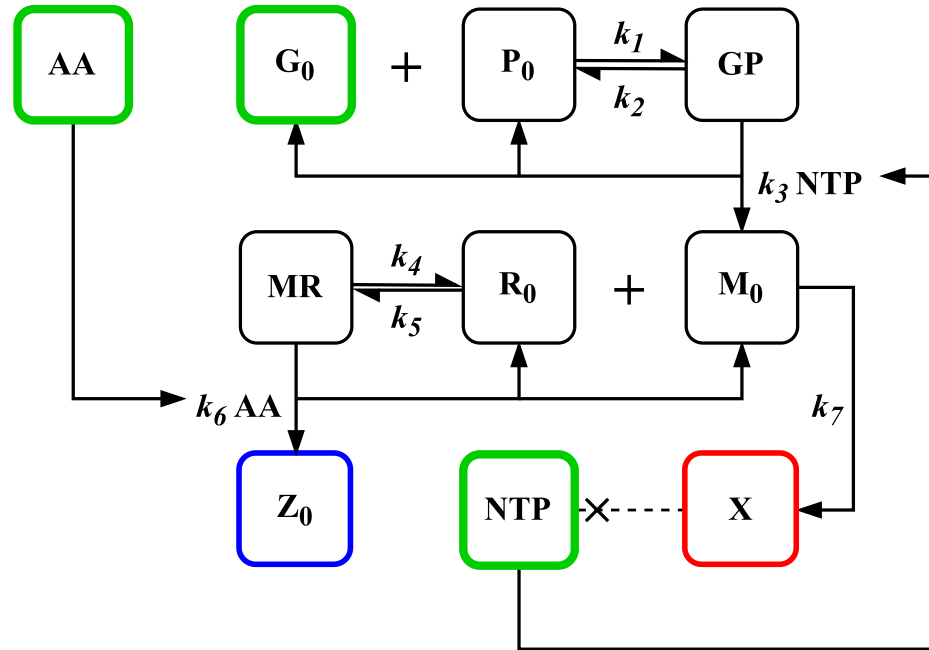
Identify the minimal molecular components required for protein synthesis



MODEL DEVELOPMENT

STEP 3

Construct the chemical reaction network based on literature findings



G₀ – plasmid

P₀ – RNA polymerase (RNAP)

GP – RNAP-plasmid complex

M₀ – mRNA

R₀ – ribosome

MR – mRNA-ribosome complex

NTP – nucleotide reservoir

AA – amino acids reservoir

Z₀ – reporter protein

k₁ – RNAP-promoter association

k₂ – RNAP-promoter dissociation

k₃ – mRNA production

k₄ – mRNA-ribosome association

k₅ – mRNA-ribosome dissociation

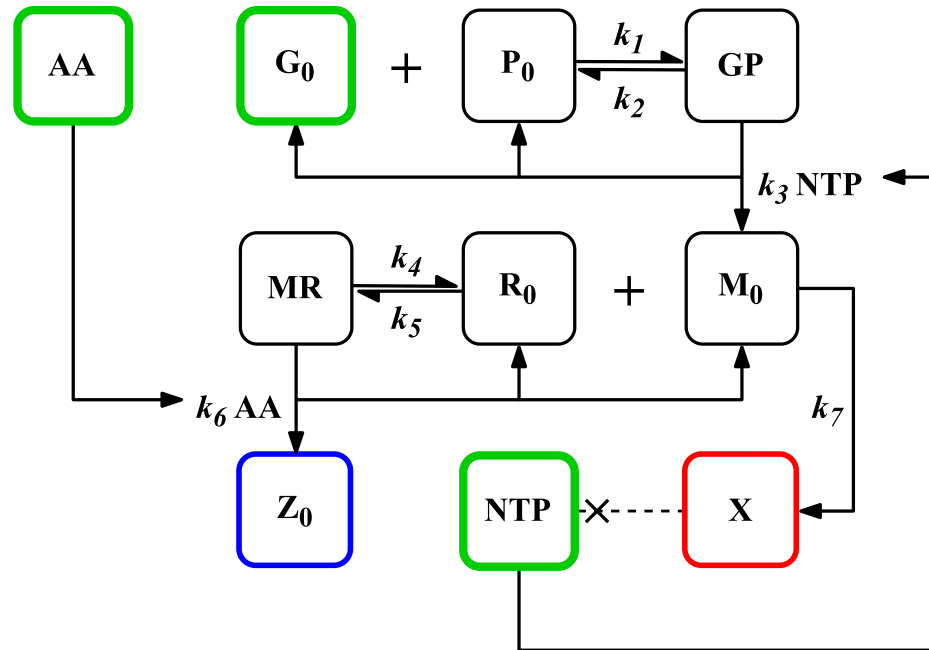
k₆ – protein production

k₇ – mRNA degradation

MODEL DEVELOPMENT

STEP 4

Develop mass action-based equations for each molecular component



Differential Equations

$$[\dot{G}_0] = -k_1[G_0][P_0] + k_2[GP] + k_3[NTP][GP]$$

$$[\dot{P}_0] = -k_1[G_0][P_0] + k_2[GP] + k_3[NTP][GP]$$

$$[\dot{GP}] = k_1[G_0][P_0] - k_2[GP] - k_3[NTP][GP]$$

$$[\dot{M}_0] = k_3[NTP][GP] - k_m[M_0] - k_4[M_0][R_0] + k_5[MR] + k_6[AA][MR]$$

$$[\dot{R}_0] = -k_4[M_0][R_0] + k_5[MR] + k_6[AA][MR]$$

$$[\dot{MR}] = k_4[M_0][R_0] - k_5[MR] - k_6[AA][MR]$$

$$[\dot{NTP}] = -k_3[NTP][GP]$$

$$[\dot{AA}] = -k_6[AA][MR]$$

$$[\dot{Z}_0] = k_6[AA][MR]$$

MODEL DEVELOPMENT

STEP 5

Carry out simulation for a collection of time points using a computational software (*R* and the package *deSolve*)

Initial Concentrations		Rate constants		Other parameters
$G_0 - 1 \text{ nmol l}^{-1}$	$P_0 - 1 \text{ nmol l}^{-1}$	$k_1 - 6 \times 10^9 \text{ mol}^{-1} \text{ l min}^{-1}$	$k_2 - 600 \text{ min}^{-1}$	Simulation time – 30 min
$R_0 - 1 \text{ nmol l}^{-1}$	$NTP - 1 \text{ nmol l}^{-1}$	$k_3 - 1 \times 10^9 \text{ mol}^{-1} \text{ l min}^{-1}$	$k_5 - 135 \text{ min}^{-1}$	Numerical integrator – BDF
$AA - 1 \text{ nmol l}^{-1}$	$GP - 0$ $M_0 - 0$	$k_4 - 6 \times 10^9 \text{ mol}^{-1} \text{ l min}^{-1}$	$k_7 - 18 \text{ min}^{-1}$	Time step – 0.001 min ⁻¹
$MR - 0$ $Z_0 - 0$		$k_6 - 1 \times 10^{10} \text{ mol}^{-1} \text{ l min}^{-1}$		Test gene – β galactosidase

Code Availability

<https://github.com/zachariah-ibrahim/cell-free-protein-expression>

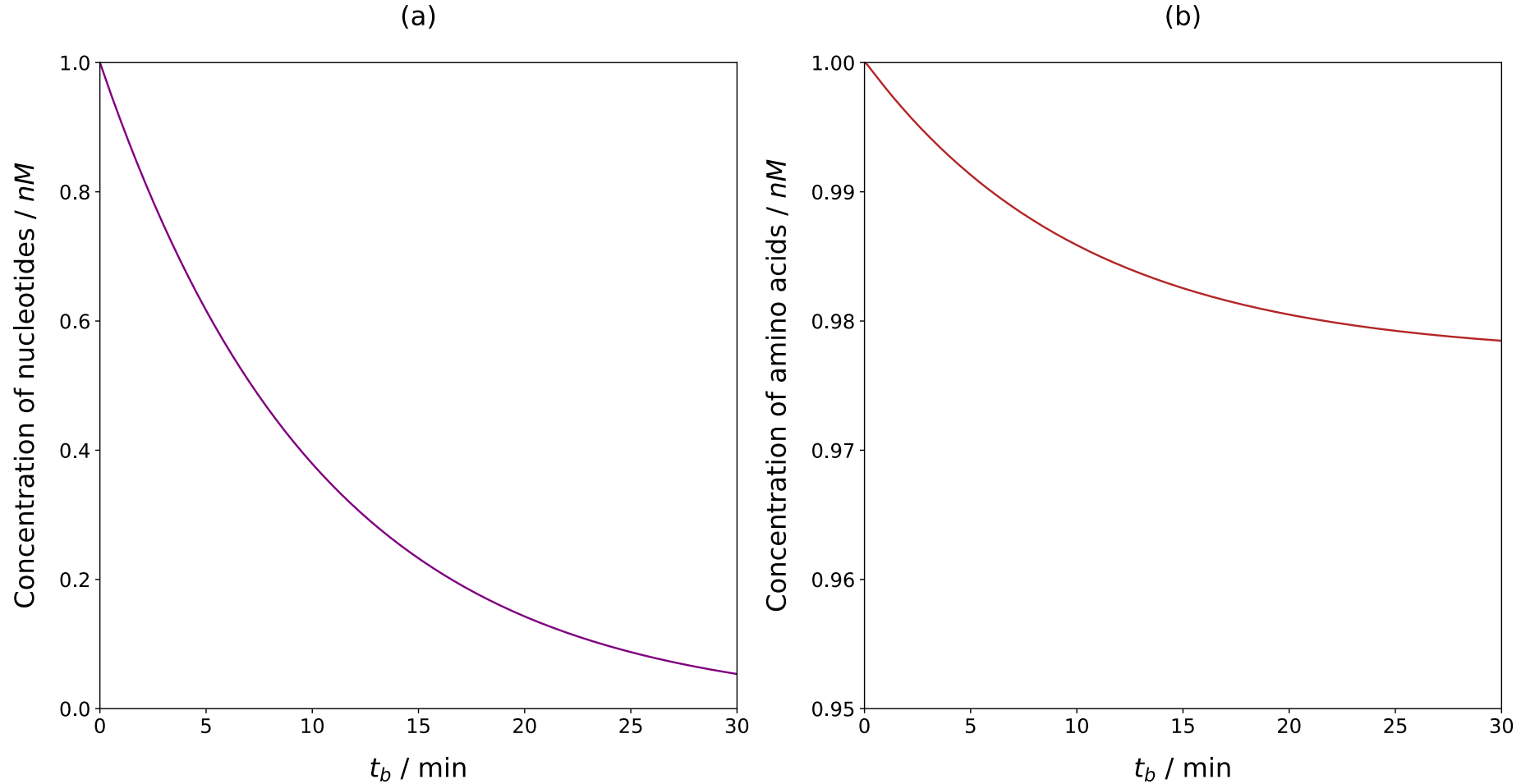
Parameter availability

Kierzek, A. M., Zaim, J., & Zielenkiewicz, P. (2001). The effect of transcription and translation initiation frequencies on the stochastic fluctuations in prokaryotic gene expression. The Journal of Biological Chemistry, 276(11), 8165–8172. doi:10.1074/jbc.M006264200



RESULTS & DISCUSSION

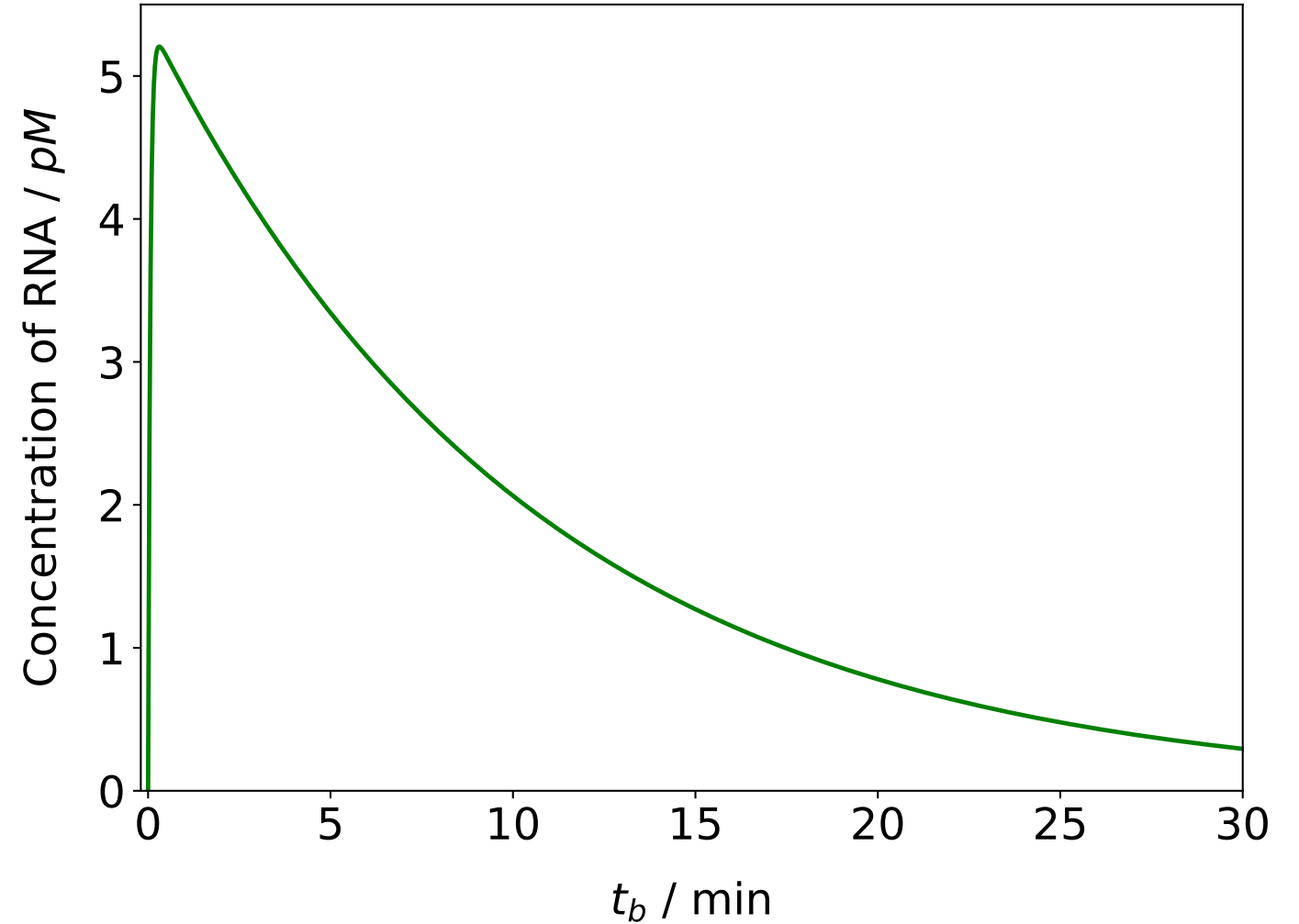
RESULTS & DISCUSSION



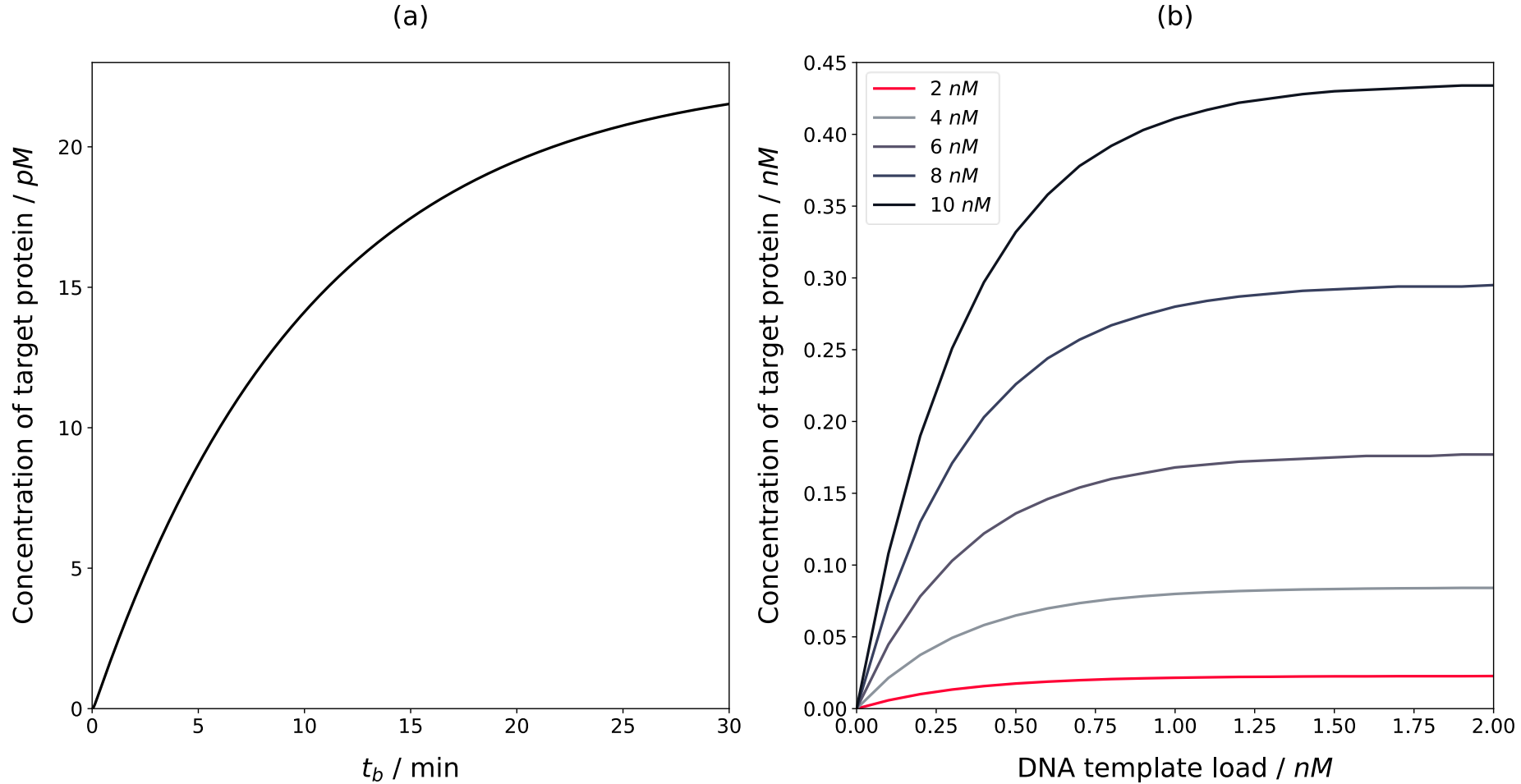
- a) The consumption of NTP is do not correlate with mRNA production**
- b) In contrast, the amino acids consumption correlate with protein production**

RESULTS & DISCUSSION

- The mRNA concentration goes through a maxima and decays exponentially

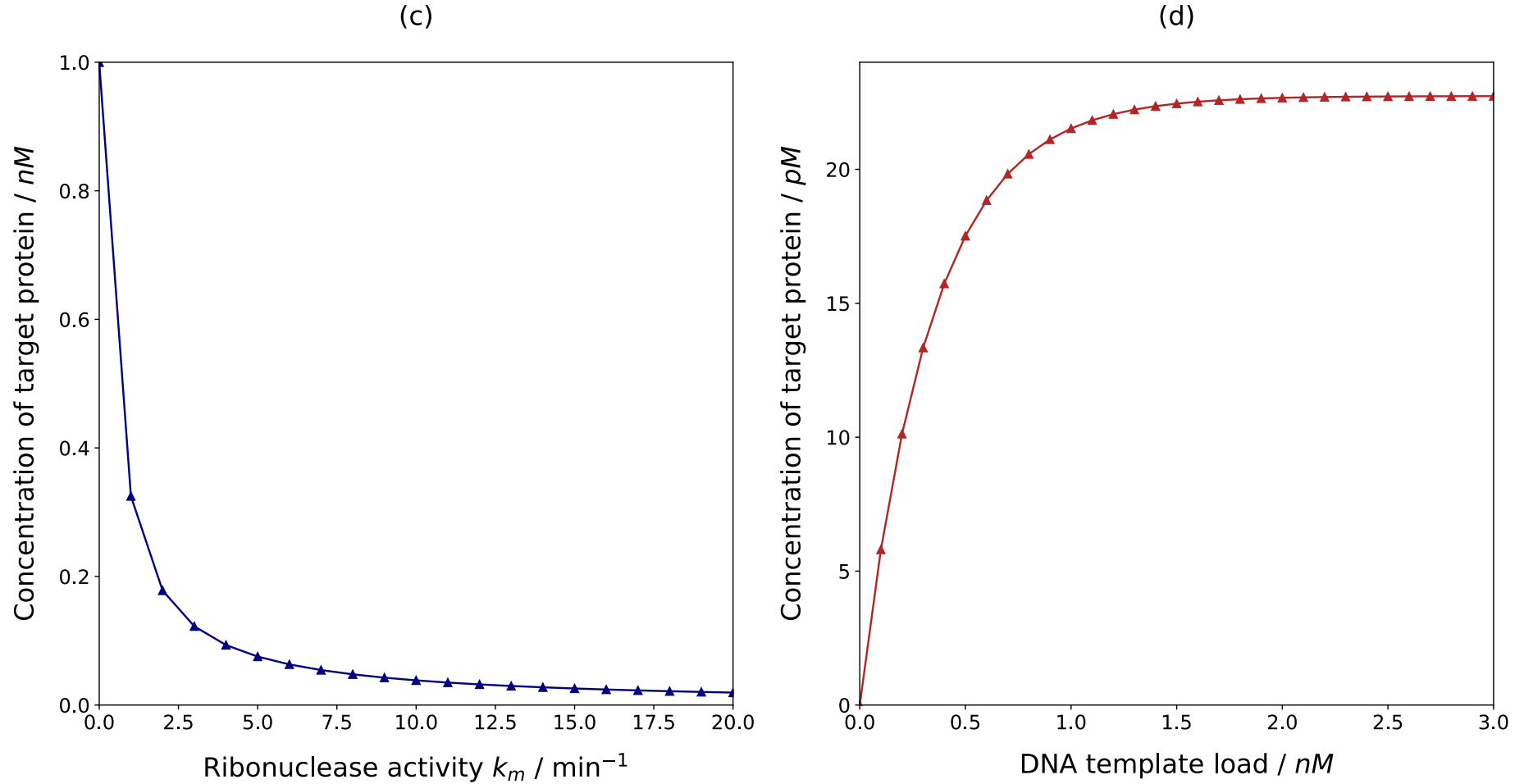


RESULTS & DISCUSSION



- a) For the reaction time of 30 min, the maximum concentration of reporter protein that can be obtained is 21 pM
- b) Increasing the biochemical resources available to CFPS system can increase the protein yield from 21 pM to 0.4 nM

RESULTS & DISCUSSION



- c) Suppressing the ribonuclease activity can improve the target protein yield significantly**
- d) The DNA loading indicates that the yield increases linearly and plateaus after a critical DNA concentration of 2.0 nM**

CONCLUSION

- **The CFPS system require constant supply of resources to perpetuate**
- **Inheriting detrimental components during extract preparation affects the performance of CFPS systems**
- **In the absence of detrimental activities, protein yield increases proportionally with the resources supplied**
- **The simulation studies will be useful for the communities that are involved in gene circuit engineering and biomanufacturing**

REFERENCES

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THANK YOU