

Def A function f has a <u>relative maximum</u> (or <u>local max</u>) at C if there is an interval I containing C such that $f(x) \leq f(c)$ for x in I.

Det for local minimum (or relative min) replace $f(x) \leq f(c)$ with $f(c) \leq f(x)$.

Theorem If f has a relative max/min at x=c, then either f'(c) = 0 or f'(c) is undefined.

NOTE: The reverse is not true

1 1 f(x)= x3

$$\int (x) = 3x^2$$

f'(0) = 0 / but f does not have a local max/min at 0.

Def If f'(c)=0 or undefined, we say c is a critical number of f. (Provided c is an the)

Exy Is
$$x = Tr$$
 a critical number of $f(x) = 8sin(x-\frac{\pi}{2})$
 $f'(x) = 8cos(x-\frac{\pi}{2}) = 8cos(\frac{\pi}{2}) = 0$

Ves

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 $f'(x) = 8c$

$$f'(x)$$
 undefined:

 $cos^2x = 0$
 $cosx = 0$

Un the interval $cosx = 0$
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$$\Rightarrow$$
 Ether 1+ x=0 OR ex=0
 $x=-1$ Never

$$Ex \frac{1}{f(x)} = (x^2 - 1)^3$$

 $f'(x) = 3(x^2 - 1)^2 (2x) \stackrel{\text{set}}{=} 0$

Euther,
$$6x=0$$
 OR $(x^2-1)^2=0$
 $x=0$ $x^2-1=0$ $x=-1$

$$Ex^{9}(f(x)) = 2x^{3} - 3x^{2} - 12x + 1$$

$$f'(x) = (6x^{2} - (6x - 12)) = 0$$

$$(6(x^{2} - x - 2)) = 0$$

$$(6(x - 2)(x + 1)) = 0$$

=) Either 600 OR
$$\chi$$
-2=0 OR χ +1=0 χ =-1

Quadratic Formula: $0 \times 2 + b \times + c = 0 \implies \chi = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$$E \times 10^{3} f(x) = \chi^{3} + 5\chi^{2} + 7\chi$$

$$f'(x) = 3\chi^{2} + 10\chi + 7$$

$$\chi = -10 \pm \sqrt{10^{2} - 4(3)(7)} = -10 \pm \sqrt{100 - 84} = -10 \pm \sqrt{10}$$

$$= -10 \pm 4 \implies \chi = -6, -14 \implies \chi = -1, -\frac{7}{3}$$