MY 1 Review · Tomorrow (tues. 9/23) · 8-9PM ·LILY 1105 · Lectures 2-10 Make Swe · Percils / Erasers oCal culater Section Number Tristructor's

Siva Somasundaram X1 X2 X3 X4 X5 X6 W8 W9 W10 W11 W12 W13 W1 W2 W3 W4 W5 W6 W7 X V7 V8 V9 V10 V11 V12 V13 X V1 V2 V3 V4 V5 V6 X U11 U12 U13 U14 U15 U16 U17 U18 U19 U20 U1 U2 U3 U4 U5 U6 U7 U8 U9 U10 T1 T2 T3 T4 T5 T6 T7 T8 T9 T10 T11 T12 T13 T14 T15 T16 T17 T18 T19 T20 R1 R2 R3 R4 R5 R6 R7 R8 R9 R10 R11 R12 R13 R14 R15 R16 R17 R18 R19 R20 P1 P2 P3 P4 P5 P6 P7 P8 P9 P10 P11 P12 P13 P14 P15 P16 P17 P18 P19 P20 O13 O14 O15 O16 N11 N12 N13 N14 N15 N16 N17 M12 M13 M14 M15 M16 M1 F15 F16 D1 D2 D3 D4 D5 D6 D7 D8 D9 D10 B15 B16 B1 B2 B3 B4 B5 B6 B7 B8 B9 B10 A7 A8 A9 A10 X A1 A2 A3 A4 A5 A6 **LILY 1105**

7:30 Section

(

8:30 Section

Pence

This is an optional assignment that will be worth 2 points of extra credit. You must show work to get credit.

NOTE: These are just review problems of Lectures 2-10; these are not necessarily representative of the problems of the exam. The exam can (and most likely will) have different problems.

Directions:

- 1. Complete each problem on the next page, make sure to show your work. Clearly mark the question number and final answer.
- 2. You have two options to turn in this assignment:
 - (a) **In-person:** You can slip it under my office door located in MATH 615. Make sure your name is on it and that it is stapled together (if there are multiple pages).
 - (b) Email: You may email your assignment to me at pencel1@purdue.edu
 - i. Scan your assignment so that it is one PDF (do not submit a bunch of images).
 - ii. In the subject line, write "EXTRA CREDIT 1 [your name]".
- 3. The answers will be given in the lecture after the due date (9/22). Therefore, **no late submissions** will be allowed.

Problem 1. Use the table below to compute numerically $\lim_{x\to 0} \frac{e^{\frac{3y}{x}}-1}{x}$

x	-0.1	-0.01	-0.001	0	0.001	0.01	0.1
f(x)	2.5918	2.9534	2.9955		3.0045	3.045	3.4986
[0.00] [0] [ENT] [DID [ENT] [0.001] [ENT]							
	olem 2. Evaluate:		5176	J	LNI CO.	EL FR	l
		e^	$\lim_{x \to 0} \frac{\sin(x) - x}{4x}$				

$$\lim_{x\to 0} \frac{\sin x - x}{4x} = \frac{1}{4} \lim_{x\to 0} \frac{\sin x - x}{x} = \frac{1}{4} \lim_{x\to 0} \left(\frac{\sin x}{x} - \frac{x}{x} \right)$$

$$= \frac{1}{4} \lim_{x\to 0} \left(\frac{\sin x}{x} - 1 \right) = \frac{1}{4} (1-1) = \boxed{0}$$

Problem 3. Let f(x) be the function below:

$$f(x) = \begin{cases} -x + 2 & x < -1\\ mx + b & -1 \le x \le 0\\ 1 - \sqrt{x} & x > 0 \end{cases}$$

What values do m and b need to be to make f continuous for every value of x?

Only places it could be continuous is - $\lim_{x\to 1} - f(x) = \lim_{x\to 1} (-x+2) = 3 = \lim_{x\to 1} f(-1) = \lim_{x\to 1} f(x)$ Dur line needs to contain (-1,3)

 $\chi=0$ lim $f(\chi) = \lim_{\chi \to 0^+} (1-\sqrt{\chi}) = |\frac{\psi + v + f(\chi)}{\chi}$ Our line needs to contain (COII)

$$M = \frac{3-1}{1-0} = \frac{2}{1} = -2$$

(2)
$$P(x)$$
 (ontinues when $Q(x) \neq 0$

Problem 4. Use the definition of the derivative to compute f'(x) if $f(x) = x^2 - 1$

Problem 5. Find the equation of the line tangent to $f(x) = \sqrt{x}$ at x = 4

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$[x^2 - 1]' = \lim_{h \to 0} \frac{(x+h)^2 - 1 - [x^2 - 1]}{h}$$

$$= \lim_{h \to 0} \frac{x^2 + 2xh + h^2 + x^2 + 1}{h} = \lim_{h \to 0} \frac{2xh + h^2}{h}$$

$$= \lim_{h \to 0} (2x + h) = 2x$$

Slope: f'(4) $f'(x) = [\sqrt{x}]' = [\chi^{\frac{1}{2}}]' = \frac{1}{2}[\chi^{\frac{1}{2}}]' = \frac$ **Problem 6.** Differentiate the following functions:

(i)
$$f(x) = 3x^4 + 7x^2 - 5x + 9$$

Power Rule:
$$f_{\mathbf{x}}(\mathbf{x}^{\mathbf{p}}) = \mathbf{p} \mathbf{x}^{\mathbf{p}-1}$$

$$f'(x) = 3[x']' + 7[x^2]' - 5[x]' + [9]'$$

$$= 3(4x^3) + 7(2x) - 5(1)$$

$$= 12 x^3 + 14x - 5$$

(ii)
$$g(x) = e^{x}(x^{3} + 1)$$
 Product Rule & $(fg)^{y} = f'g + fg'$

$$g' = [e^{x}(x^{3}H)]' = [e^{x}]'(x^{3}H) + [e^{x}](x^{3}H)$$

= $e^{x}(x^{3}H) + e^{x}(3x^{2})$

$$f(x) = \ln x = e^{x} \left(x^{3} + 3x^{2} + 1 \right)$$

$$(iii) h(x) = \frac{\ln(x)}{\sin(x)} g(x) = \sin x$$

(iii)
$$h(x) = \frac{\ln(x)}{\sin(x)}$$
 g(x)= $\sin x$

Quotient Rule:
$$(\frac{4}{9})' = \frac{f'g - fg'}{g^2}$$

$$W = \left(\frac{\ln x}{\sin x}\right)' = \frac{\left[\ln x\right]'\sin x - \left[\ln x\right]\left[\sin x\right]'}{\left[\sin x\right]^2} = \frac{\sin x - 1}{\sin x}$$

$$(iv) \ s(x) = \tan(x^2 + 3x)$$

Chan Rule:
$$\left[f(g(x))\right]' = f'(g(x)) \cdot g'(x)$$

$$S'(\chi) = \left[\tan\left(\chi^2 + 3\chi\right)\right] \cdot \left[\chi^2 + 3\chi\right] = \left[\sec^3\left(\chi^2 + 3\chi\right)\right]$$

$$w.r.t. \quad \chi^2 + 3\chi \quad w.r.t.\chi \quad \left[2\chi + 3\chi\right]$$

Problem 7. The position of a dampened pendulum is measured from the angle (in radians) from its resting point. Its position after t seconds is given by the equation:

$$s(t) = e^{-t} \cos\left(\frac{\pi}{2}t\right)$$

- (i) What is the velocity function v(t) (in radians per second)?
- (ii) What is the velocity after 1 second?

$$\frac{\partial}{\partial t} = \frac{\partial}{\partial t} = \frac{\partial}$$

Problem 8. Find $\frac{dy}{dx}$ if:

$$\ln(y) = \left[\frac{1}{x^{2} + 1} \right]^{x}$$

$$\ln(y) = \left[\frac{1}{x^{2} + 1} \right]^{x} + \frac{1}{x^{2} + 1} \right]$$

$$\lim_{y = (x^{2} + 1)^{x}} \left[\ln(x^{2} + 1) + \frac{2x^{2}}{x^{2} + 1} \right]$$