

Det A function of has a relative (or local) maximum if there is an interval I containing f(x) \left(c) for all x in I Det For relative minumums, replace $f(x) \leq f(c)$ with

Thm If f has a local max/min at X=C, then either f'(c) = 0 or f'(c) is undefined.

NOTE: The reverse is not true

NOTE: The reverse is not the
$$f'(0) = 0$$
 that 0 is not the location of a local max lmin

Def If f'(c) is O or undefined, we say C is critical number of f.

EXI Is
$$X=T$$
 a critical number of $f(x) = 8\sin(x-\frac{\pi}{2})$
 $f'(x) = 8\cos(x-\frac{\pi}{2})$
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No

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$$\frac{\cos x}{\cos x} = 0$$
On the interval [-11], IT)
$$x = \frac{\pi}{2} \cdot \frac{\pi}{2}$$

Ex5/Find all critical numbers of
$$f(x) = \frac{\ln(x)}{X}$$

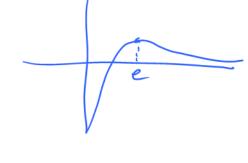
$$f'(x) = \frac{(\frac{1}{x}) \cdot x - \ln(x) \cdot (1)}{X^2} = \frac{1 - \ln(x)}{X^2}$$

$$f'(x)$$
 is undefined:
 $\chi^2 = 0 \implies [x = 0]$

$$|-|n(x) = 0$$

$$|n(x) = |$$

$$\boxed{\chi = e}$$



f has critical numbers at X = 0, C

Exle/Find the critical numbers for
$$f(x) = xe^{x}$$

 $f'(x) = [x]'e^{x} + x[e^{x}]' = e^{x} + xe^{x} = (1+x)e^{x}$

f(x) undefined: Never

$$f'(x) = 0: \qquad (1+x) e^{x} \text{ set } 0$$

$$Either: \qquad 1+x=0 \qquad OR \qquad x=0$$

$$X=-1 \qquad Never$$

$$Ex9 f(x) = 2x^{3}-3x^{2}-12x+1$$

$$f'(x) = 6x^{2}-6x-12 \qquad set \qquad 0$$

$$(6(x^{2}-x-2) = 0)$$

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$$(6(x-2)(x+1) = 0$$

$$X=-1$$

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$$Auadratic \qquad Formula: \qquad 0x^{2}+bx+c=0 \Rightarrow x=-\frac{b^{2}\sqrt{b^{2}-4ac}}{2a}$$

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$$= -\frac{10 \pm 4}{6} \implies \chi = -\frac{14}{6}, -\frac{6}{6}$$

$$\Rightarrow \chi = -\frac{7}{3}, -1$$