

Final Exam Review

Problems for Day 1 (Lectures 1-15): Limits/Continuity, Derivatives up to Related Rates

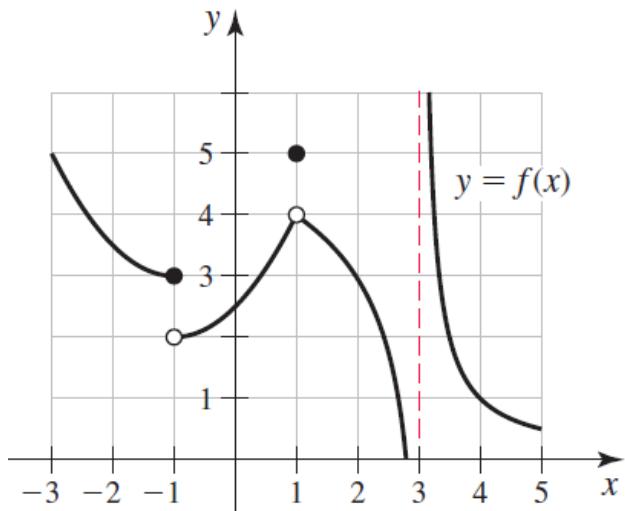
1. Compute the following limits:

$$(a) \lim_{x \rightarrow 1} \sqrt{5x + 6}$$

$$(b) \lim_{x \rightarrow 4} \frac{x^3 - 7x^2 + 12x}{4-x}$$

$$(c) \lim_{h \rightarrow 0} \frac{\sqrt{5(x+h)} - \sqrt{5x}}{h}, \quad x > 0$$

2. The graph of a function f is given below. Locate and classify all discontinuities of f .



3. Find y' if:

(a) $y = x^2 + 2x + 9$

(b) $y = 5t^2 \sin t$

(c) $y = \frac{e^x}{1+\cos x}$

(d) $y = (x + 1)^{\frac{1}{x}}$

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4. Given the algebraic curve $x^2y + y^3 = 5$, find the slope of the tangent line at $(2, 1)$.

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$$\frac{\ln t}{t^2}$$

5. The position (in meters) of a particle traveling in a straight line is given by $s(t) = \frac{\ln t}{t^2}$, where t is the time in seconds. Find the acceleration after 1 second.

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6. A spherical balloon is inflated at a rate of $10 \text{ cm}^3/\text{min}$. At what rate is the **diameter** of the balloon increasing when the balloon has a diameter of 5 cm?

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7. Two boats leave a dock at the same time. One boat travels north at 30 mph and the other travels east at 40 mph. After half an hour, how fast is the distance between the boats increasing?

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8. A plane is flying away from you at a speed of 270 mph at a constant altitude of 2 miles. Find the rate at which the angle of elevation is decreasing when the angle is $\pi/6$.