

**iSpy: Detection of Signals in Noise**  
**(EECE4688)**  
**Spring 2019**

**Homework 2**  
**(Assigned Jan. 24, 2019; due Jan. 30, 2019 in class.)**

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**Objective:** The objective of this exercise is to study the Neuman-Pearson detection principle.

**Task:**

- Consider the following detection problem: The observation  $y$  of a random variable  $Y$  is known to contain a signal in noise. The signal either equals  $A_0$ , or it equals  $A_1 > A_0$ . The noise is zero-mean Gaussian of known variance  $\sigma_Z^2$ .
  - (i) Develop the Neuman-Pearson detection rule.
  - (ii) Determine the probability of correct detection as a function of the probability of false alarm.
- Use Matlab to generate 10,000 detection trials, with  $A_0$  occurring with probability  $P_0 = 0.3$  (and  $A_1$  occurring with probability  $P_1 = 0.7$ ). Set the noise variance to  $\sigma_Z^2 = 1$ , and the signal values such that  $SNR_0 = \frac{A_0^2}{\sigma_Z^2}$  is 10 dB and  $SNR_1 = \frac{A_1^2}{\sigma_Z^2}$  is 15 dB.
  - (i) Set the desired probability of false alarm to  $P_{fa}^* = 10\%$ . Count the instances of correct detection and estimate the probability of correct detection.
  - (ii) Repeat for different values of  $P_{fa}^*$ , ranging from 0 to 100 % in steps of 10%. Plot the estimated probability of correct detection vs. the probability of false alarm. Plot the theoretical ROC on the same graph. Comment on the result.
  - (iii) Estimate the actual probability of false alarm, and plot it against the design value  $P_{fa}^*$ . Comment on the result.

**Reporting:** Your report should be typed, and not exceed two single-sided pages. It should be written in a professional manner. Figures and mathematical expressions should be used whenever meaningful. Figures should always have axes labeled in appropriate units (e.g. time [s], time [ms], frequency [Hz], frequency [kHz], SNR or SNR [dB], etc.). Include any Matlab code as an appendix. Please put your name on top of the report.