Stat 787 - Assignment 2

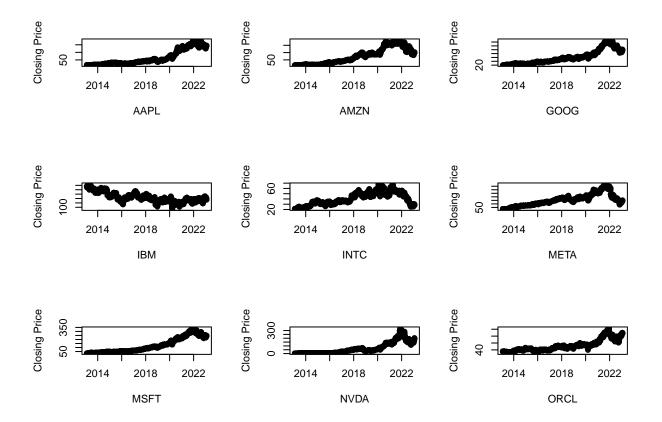
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Exercise 1

The following R chunk loads the data for the closing prices of nine major tech companies over the last ten years, and plots them as time series.

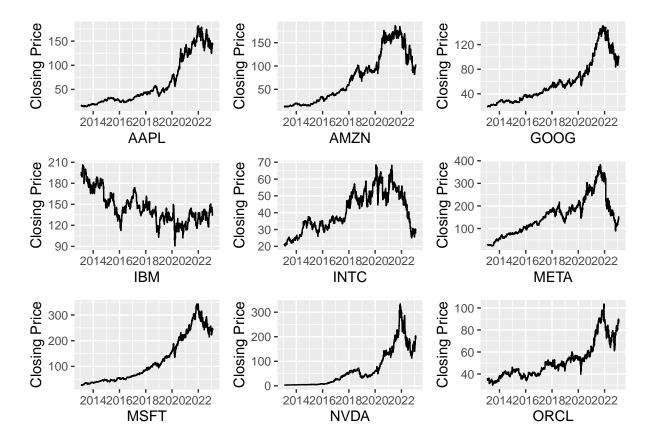
```
setwd("C:/Users/16317/Documents/Spring 2023/STAT 787/Assignment 2")
close <- read.csv("ClosingPrices.csv")</pre>
head(close)
##
         Date
                  AAPL
                          AMZN
                                   GOOG
                                              IBM INTC META MSFT
                                                                      NVDA
## 1 2/1/2013 16.20071 13.2500 19.31759 196.1568 21.36 29.73 27.93 3.0925 36.21
## 2 2/4/2013 15.79714 12.9990 18.90464 194.8279 21.16 28.11 27.44 3.0400 35.13
## 3 2/5/2013 16.35143 13.3445 19.07201 193.8719 21.18 28.64 27.50 3.1100 35.48
## 4 2/6/2013 16.33393 13.1110 19.18235 192.1797 20.99 29.05 27.34 3.0850 35.10
## 5 2/7/2013 16.72214 13.0115 19.27650 190.9560 20.81 28.65 27.28 3.0725 34.56
## 6 2/8/2013 16.96357 13.0975 19.56093 192.8107 21.00 28.55 27.55 3.0925 34.90
close$Date <- as.Date(close$Date, "%m/%d/%Y")</pre>
par(mfrow=c(3,3))
plot(close$AAPL ~ close$Date, xlab="AAPL", ylab="Closing Price")
plot(close$AMZN ~ close$Date, xlab="AMZN", ylab="Closing Price")
plot(close$GOOG ~ close$Date, xlab="GOOG", ylab="Closing Price")
plot(close$IBM ~ close$Date, xlab="IBM", ylab="Closing Price")
plot(close$INTC ~ close$Date, xlab="INTC", ylab="Closing Price")
plot(close$META ~ close$Date, xlab="META", ylab="Closing Price")
plot(close$MSFT ~ close$Date, xlab="MSFT", ylab="Closing Price")
plot(close$NVDA ~ close$Date, xlab="NVDA", ylab="Closing Price")
plot(close$ORCL ~ close$Date, xlab="ORCL", ylab="Closing Price")
```



The same plotting will be done again, but using ggplot.

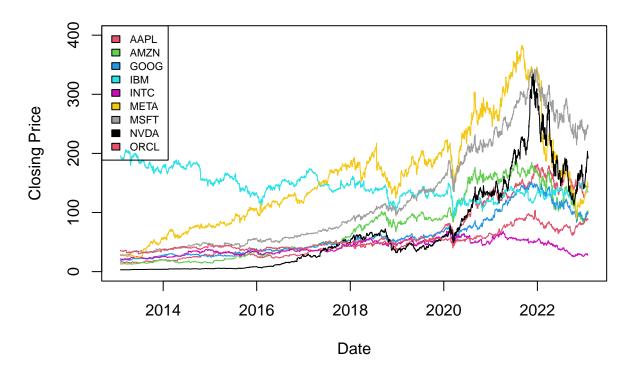
```
library(ggplot2)
library(dplyr)
```

```
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
##
p1 <- ggplot(close, aes(x=Date, y=AAPL)) + geom_line() + xlab("AAPL") + ylab("Closing Price")
p2 <- ggplot(close, aes(x=Date, y=AMZN)) + geom_line() + xlab("AMZN") + ylab("Closing Price")
p3 <- ggplot(close, aes(x=Date, y=GOOG)) + geom_line() + xlab("GOOG") + ylab("Closing Price")
p4 <- ggplot(close, aes(x=Date, y=IBM)) + geom_line() + xlab("IBM") + ylab("Closing Price")
p5 <- ggplot(close, aes(x=Date, y=INTC)) + geom_line() + xlab("INTC") + ylab("Closing Price")
p6 <- ggplot(close, aes(x=Date, y=META)) + geom_line() + xlab("META") + ylab("Closing Price")
p7 <- ggplot(close, aes(x=Date, y=MSFT)) + geom_line() + xlab("MSFT") + ylab("Closing Price")
p8 <- ggplot(close, aes(x=Date, y=NVDA)) + geom_line() + xlab("NVDA") + ylab("Closing Price")
p9 <- ggplot(close, aes(x=Date, y=ORCL)) + geom_line() + xlab("ORCL") + ylab("Closing Price")
library(patchwork)
p1 + p2 + p3 + p4 + p5 + p6 + p7 + p8 + p9
```



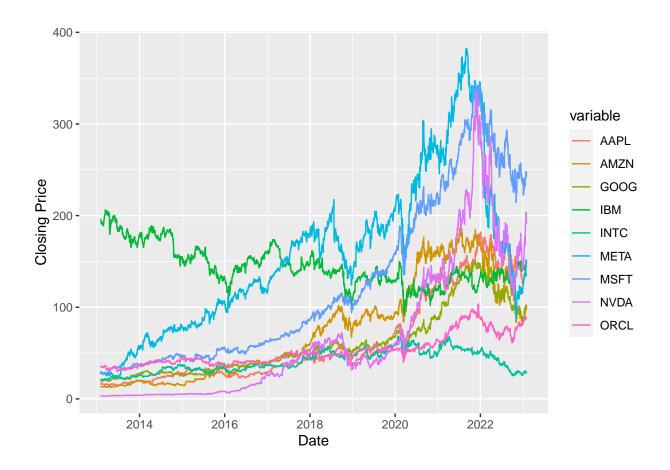
We can see from both plots above that Apple, Amazon, Google, Meta, Microsoft, Nividia, and Oracle all have similar trends. From 2013 until 2022 we see an exponential increase in closing price, but then a decrease in 2023. Note that we see a big jump after 2020 with this companies, probably due to the Covid-19 pandemic. As for IBM, it appears their stock has decreased somewhat steadily over the last decade. Intel's stock increases in what appears to be a linear trend over from 2013 to 2021, and then took a major dip over the last two years.

The following R chunks plot the time series seen above on one plot. The first chunk does so with traditional plotting and the second with ggplot.



```
library(reshape2)
meltdf <- melt(close, id="Date")

ggplot(meltdf, aes(x=Date, y=value, colour=variable, group=variable)) +
  geom_line() + ylab("Closing Price")</pre>
```



Exercise 2

Using the R data set mtcars, ten linear learners were built using bootstrap samples of the data.

data(mtcars)
mtcars

##	mpg	cyl	disp	hp	drat	wt	qsec	vs	am	gear	carb
## Mazda RX4	21.0	6	160.0	110	3.90	2.620	16.46	0	1	4	4
## Mazda RX4 Wag	21.0	6	160.0	110	3.90	2.875	17.02	0	1	4	4
## Datsun 710	22.8	4	108.0	93	3.85	2.320	18.61	1	1	4	1
## Hornet 4 Drive	21.4	6	258.0	110	3.08	3.215	19.44	1	0	3	1
## Hornet Sportabout	18.7	8	360.0	175	3.15	3.440	17.02	0	0	3	2
## Valiant	18.1	6	225.0	105	2.76	3.460	20.22	1	0	3	1
## Duster 360	14.3	8	360.0	245	3.21	3.570	15.84	0	0	3	4
## Merc 240D	24.4	4	146.7	62	3.69	3.190	20.00	1	0	4	2
## Merc 230	22.8	4	140.8	95	3.92	3.150	22.90	1	0	4	2
## Merc 280	19.2	6	167.6	123	3.92	3.440	18.30	1	0	4	4
## Merc 280C	17.8	6	167.6	123	3.92	3.440	18.90	1	0	4	4
## Merc 450SE	16.4	8	275.8	180	3.07	4.070	17.40	0	0	3	3
## Merc 450SL	17.3	8	275.8	180	3.07	3.730	17.60	0	0	3	3
## Merc 450SLC	15.2	8	275.8	180	3.07	3.780	18.00	0	0	3	3
## Cadillac Fleetwood	10.4	8	472.0	205	2.93	5.250	17.98	0	0	3	4
## Lincoln Continental	10.4	8	460.0	215	3.00	5.424	17.82	0	0	3	4
## Chrysler Imperial	14.7	8	440.0	230	3.23	5.345	17.42	0	0	3	4
## Fiat 128	32.4	4	78.7	66	4.08	2.200	19.47	1	1	4	1
## Honda Civic	30.4	4	75.7	52	4.93	1.615	18.52	1	1	4	2

```
4 71.1 65 4.22 1.835 19.90
## Toyota Corolla
                        33.9
## Toyota Corona
                        21.5
                               4 120.1 97 3.70 2.465 20.01
                                                                       3
                                                                             1
                               8 318.0 150 2.76 3.520 16.87
                                                                             2
## Dodge Challenger
                        15.5
## AMC Javelin
                               8 304.0 150 3.15 3.435 17.30
                                                                             2
                        15.2
                                                                       3
## Camaro Z28
                        13.3
                               8 350.0 245 3.73 3.840 15.41
                                                                             4
## Pontiac Firebird
                        19.2
                               8 400.0 175 3.08 3.845 17.05
                                                                  0
                                                                       3
                                                                             2
## Fiat X1-9
                        27.3
                               4 79.0 66 4.08 1.935 18.90
                                                                             1
                               4 120.3 91 4.43 2.140 16.70
## Porsche 914-2
                        26.0
                                                                       5
                                                                             2
## Lotus Europa
                        30.4
                               4 95.1 113 3.77 1.513 16.90
                                                                       5
                                                                             2
## Ford Pantera L
                               8 351.0 264 4.22 3.170 14.50
                                                                       5
                                                                             4
                        15.8
                                                                 1
## Ferrari Dino
                        19.7
                               6 145.0 175 3.62 2.770 15.50
                                                                       5
## Maserati Bora
                               8 301.0 335 3.54 3.570 14.60 0 1
                                                                       5
                        15.0
                                                                            8
## Volvo 142E
                               4 121.0 109 4.11 2.780 18.60 1
                                                                             2
                        21.4
L <- 10
n <- nrow(mtcars)</pre>
models <- list()
for(i in 1:L)
  boot <- mtcars[sample(n, replace=T),]</pre>
  learner <- lm(mpg ~ ., data=boot)</pre>
  models[[i]] <- learner</pre>
}
models
## [[1]]
##
## Call:
## lm(formula = mpg ~ ., data = boot)
##
## Coefficients:
   (Intercept)
                                      disp
                                                                 drat
                                                                                 wt
                         cyl
                                                     hp
##
      28.36778
                    -0.11827
                                   0.02308
                                               -0.09836
                                                             -0.11799
                                                                          -5.45729
##
          qsec
                                                   gear
                                                                 carb
                          VS
                                        am
##
                                  5.39885
       1.01524
                    -5.74371
                                               -0.50020
                                                              1.94158
##
##
## [[2]]
##
## Call:
## lm(formula = mpg ~ ., data = boot)
##
## Coefficients:
##
   (Intercept)
                                                                 drat
                         cyl
                                      disp
                                                     hp
                                                                                 wt
      -5.48398
                                   0.02146
                                               -0.01882
                                                              0.25119
                                                                           -5.80589
##
                     0.02467
##
          qsec
                          ٧s
                                                   gear
                                                                 carb
                    -1.25406
       1.98149
                                  1.43569
                                                1.44264
##
                                                              0.29871
##
##
## [[3]]
##
## Call:
## lm(formula = mpg ~ ., data = boot)
##
```

```
## Coefficients:
                                     disp
## (Intercept)
                                                                drat
                     cyl
                                                    hp
                                                                                wt
      0.699918
                   0.373926
                                -0.018502
                                                            3.488044
##
                                             -0.009424
                                                                         1.371262
##
                                                                carb
          qsec
                         VS
                                       am
                                                  gear
##
     -0.057662
                  -2.593914
                                 2.517439
                                              4.410051
                                                           -3.043890
##
##
## [[4]]
##
## Call:
## lm(formula = mpg ~ ., data = boot)
## Coefficients:
## (Intercept)
                        cyl
                                     disp
                                                   hp
                                                                drat
                                                                                wt
     -12.98905
##
                    1.02307
                                 -0.02097
                                               0.06594
                                                             2.77867
                                                                         -0.12766
##
          qsec
                         vs
                                                   gear
                                                                carb
                                       am
##
       0.64367
                    4.25841
                                  8.32932
                                               1.08308
                                                            -2.59642
##
##
## [[5]]
##
## Call:
## lm(formula = mpg ~ ., data = boot)
## Coefficients:
## (Intercept)
                        cyl
                                     disp
                                                    hp
                                                                drat
                                                                                wt
##
  -24.236069
                  -1.102674
                                 0.024870
                                              0.007605
                                                            2.159339
                                                                        -6.337379
          qsec
                         ٧s
                                       am
                                                   gear
                                                                carb
##
      3.018243
                  -4.338715
                                -0.039774
                                              1.128686
                                                            0.352654
##
##
## [[6]]
##
## Call:
## lm(formula = mpg ~ ., data = boot)
## Coefficients:
## (Intercept)
                                                                drat
                        cyl
                                     disp
                                                    hp
                                                                               wt.
##
     -71.57629
                   -7.17685
                                  0.03272
                                               0.07591
                                                             6.39133
                                                                         -7.90751
##
                                                   gear
          qsec
                         ٧s
                                                                carb
                                       am
##
       6.13040
                  -22.80519
                               -18.97073
                                               9.16280
                                                            -1.09351
##
##
## [[7]]
## Call:
## lm(formula = mpg ~ ., data = boot)
##
## Coefficients:
## (Intercept)
                        cyl
                                     disp
                                                    hp
                                                                drat
##
     -39.19941
                    0.11564
                                  0.05322
                                              -0.02111
                                                             0.60596
                                                                         -8.94001
##
          qsec
                         ٧s
                                       am
                                                  gear
                                                                carb
##
       3.66038
                   -2.77458
                                  3.25002
                                               2.10027
                                                             0.89610
##
```

```
##
## [[8]]
##
## Call:
## lm(formula = mpg ~ ., data = boot)
##
## Coefficients:
   (Intercept)
                                                                   drat
##
                          cyl
                                       disp
                                                       hp
                                                                                    wt
##
       2.28531
                    -0.38112
                                    0.06792
                                                 -0.05329
                                                               -0.42498
                                                                             -9.16091
##
          qsec
                           ٧s
                                                     gear
                                                                   carb
##
       1.46698
                     0.89313
                                    1.11110
                                                  3.58466
                                                                0.85864
##
##
## [[9]]
##
## Call:
## lm(formula = mpg ~ ., data = boot)
## Coefficients:
##
   (Intercept)
                          cyl
                                       disp
                                                       hp
                                                                   drat
##
       3.69196
                    -0.19277
                                    0.01695
                                                 -0.01848
                                                               -1.34984
                                                                             -4.98286
##
          qsec
                           vs
                                         am
                                                                   carb
                                                     gear
                                                               -0.24973
##
       1.58979
                    -2.09404
                                    0.56309
                                                  2.74323
##
##
## [[10]]
##
## Call:
## lm(formula = mpg ~ ., data = boot)
##
## Coefficients:
## (Intercept)
                                       disp
                                                                   drat
                                                                                    wt
                          cyl
                                                       hp
                  -0.7080426
                                               -0.0435802
                                                             -0.9002313
                                                                           -5.6076349
##
    10.3733487
                                 0.0290937
##
          qsec
                           VS
                                                     gear
                                                                   carb
                                         am
##
     1.7485188
                  -2.9302333
                                 4.2258274
                                                0.0004737
                                                              1.2306109
```

Then, a matrix is created to store the coefficients and MSE of each model. From this matrix, the "average" model is calculated along with its MSE.

```
models.mat <- matrix(NA, nrow=L, ncol=12)
for(i in 1:L)
{
    models.mat[i,] <- c(models[[i]]$coefficients, mean((models[[i]]$residuals)^2))
}

fhat.avg <- c()
for(i in 1:12)
{
    avg <- mean(models.mat[,i])
    fhat.avg <- c(fhat.avg, avg)
}

singular <- lm(mpg ~ ., data=mtcars)
compare <- matrix(NA, nrow=2, ncol=12)
compare[1,] <- fhat.avg</pre>
```

```
compare[2,] <- c(singular$coefficients, mean((singular$residuals)^2))
compare</pre>
```

```
[,1]
                                                 [,4]
##
                         [,2]
                                     [,3]
                                                           [,5]
                                                                     [,6]
                                                                                [,7]
## [1,] -10.80665 -0.8142412 0.02298455 -0.01136004 1.288149 -5.295588 2.1197059
        12.30337 -0.1114405 0.01333524 -0.02148212 0.787111 -3.715304 0.8210407
##
               [,8]
                         [,9]
                                  [,10]
                                             [,11]
                                                      [,12]
## [1,] -3.9382897 0.7820825 2.515569 -0.1405254 3.098620
         0.3177628 2.5202269 0.655413 -0.1994193 4.609201
```

The first row of the matrix compare seen above contains the coefficients and MSE of the average model, while the second row contains that of the singular linear model. Comparing the two, we can see that most of the coefficient are quite similar, but the MSE of the average model shows that it performs better than the singular model.

Exercise 3

The following data set contains the coordinates of the countries of Europe. From this data, dendrograms are plotted of four different hierarchical clustering of the manhattan distances between countries. Single, double, average, and Ward D2 clustering were used.

```
europe <- read.csv("europe.csv")
head(europe)</pre>
```

```
name abbreviation ISO.alpha.2 ISO.alpha.3 ISO.numeric land.area.km
##
     zoom
## 1
                            Ukr.
                                                        UKR
                                                                     804
        3 Ukraine
                                            UA
                                                                                603700
                                            FR
                                                                     250
## 2
        3
            France
                             Fr.
                                                        FRA
                                                                                547030
                                                        ESP
                                                                     724
## 3
        3
             Spain
                           Spain
                                            ES
                                                                                504782
## 4
        3
            Sweden
                            Swe.
                                            SE
                                                        SWE
                                                                     752
                                                                                449964
## 5
        3 Germany
                            Ger.
                                            DE
                                                        DEU
                                                                     276
                                                                                357021
## 6
        3 Finland
                            Fin.
                                            FΙ
                                                        FIN
                                                                     246
                                                                                337030
     population latitude longitude continent
##
## 1
       45415596
                      49.0
                                 32.0
                                              en
## 2
       64768389
                      46.0
                                  2.0
                                              eu
## 3
       46505963
                      40.0
                                 -4.0
                                              eu
## 4
                      62.0
        9045000
                                 15.0
                                              eu
## 5
       82369000
                      51.5
                                 10.5
                                              eu
## 6
        5244000
                      64.0
                                 26.0
                                              eu
coords <- cbind(europe$latitude, europe$longitude)</pre>
```

```
coords <- cbind(europe$latitude, europe$longitude)
countries <- europe$name
hc.single <- hclust(dist(coords, method="manhattan"), method="single")
hc.double <- hclust(dist(coords, method="manhattan"), method="complete")
hc.avg <- hclust(dist(coords, method="manhattan"), method="average")
hc.WD2 <- hclust(dist(coords, method="manhattan"), method="ward.D2")

par(mfrow=c(2,2))
plot(hc.single)
plot(hc.double)
plot(hc.avg)
plot(hc.WD2)</pre>
```

Cluster Dendrogram

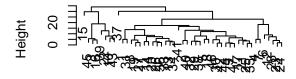
Cluster Dendrogram





Cluster Dendrogram

Cluster Dendrogram





dist(coords, method = "manhattan")
 hclust (*, "average")

dist(coords, method = "manhattan")
 hclust (*, "ward.D2")

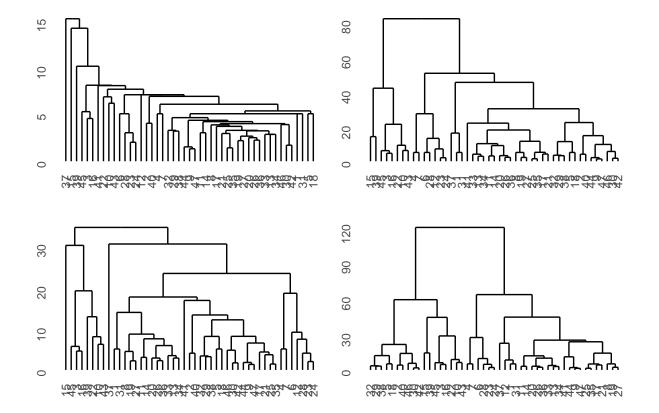
The dendrograms were recreated using ggplot.

library(dendextend)

```
##
## Welcome to dendextend version 1.16.0
## Type citation('dendextend') for how to cite the package.
##
## Type browseVignettes(package = 'dendextend') for the package vignette.
  The github page is: https://github.com/talgalili/dendextend/
##
## Suggestions and bug-reports can be submitted at: https://github.com/talgalili/dendextend/issues
## You may ask questions at stackoverflow, use the r and dendextend tags:
    https://stackoverflow.com/questions/tagged/dendextend
##
##
   To suppress this message use: suppressPackageStartupMessages(library(dendextend))
##
##
## Attaching package: 'dendextend'
## The following object is masked from 'package:stats':
##
##
       cutree
#install.packages("ggdendro")
library(ggdendro)
```

```
##
## Attaching package: 'ggdendro'
## The following object is masked from 'package:dendextend':
##
## theme_dendro

dend.single <- as.dendrogram(hc.single)
d1 <- ggdendrogram(dend.single)
dend.double <- as.dendrogram(hc.double)
d2 <- ggdendrogram(dend.double)
dend.avg <- as.dendrogram(hc.avg)
d3 <- ggdendrogram(dend.avg)
dend.WD2 <- as.dendrogram(hc.WD2)
d4 <- ggdendrogram(dend.WD2)
d1 + d2 + d3 + d4</pre>
```



I was able to find the packages igraph and graph, but I was not able to figure out how to create a "graphplot" with clustering of group size 3. I did a lot of searching and used chat gpt, but unfortunately everything I tried and chat gpt coded returned an error. The libraries are commented in the R chunk below.

```
#install.packages("igraph")
#library(igraph)
#if (!require("BiocManager", quietly = TRUE))
# install.packages("BiocManager")
#BiocManager::install("graph")
#library(graph)
```