

H 2 ZPH PG 5

b. Find the reciprocal of 111 in \mathbb{Z}_{200}

$$111^{-1}$$

$$(111 \times k) \bmod 200 = 1$$

$$1 = 5 \cdot 200 + -9 \cdot 111$$

$$b = -9 \bmod 200 = 191$$

$$111 \otimes 191 = (111 \cdot 191) \bmod 200 = 21201 \bmod 200 = 1$$

$$\text{Therefore, } 111^{-1} = 191$$

6. Find all integers x which leave a remainder 4 when divided by 5 and a remainder 7 when divided by 11. That is, solve the following equations simultaneously

$$x \bmod 5 = 4 \quad \text{and} \quad x \bmod 11 = 7$$