

## H 2 ZPA pg 4

4. List all elements of  $\mathbb{Z}_{21}$  that have a reciprocal

$\gcd(21, k)$  when  $k = (1, 2, 4, 5, 8, 10, 11, 13, 16, 17, 19, 20)$

This list covers all elements of  $\mathbb{Z}_{21}$  that have a reciprocal

5. a.) Find 2 integers such that  $111x + 200y = 1$

$$200 = 1 \cdot 111 + 89$$

$$111 = 1 \cdot 89 + 22$$

$$89 = 4 \cdot 22 + 1$$

$$22 = 22 \cdot 1 + 0$$

$$1 = 89 - 4 \cdot 22$$

$$1 = 89 - 4 \cdot (111 - 1 \cdot 89)$$

$$1 = -4 \cdot 111 + 5 \cdot 89$$

$$1 = -4 \cdot 111 + 5 \cdot (200 - 1 \cdot 111)$$

$$1 = 5 \cdot 200 + [-4 + (5 \cdot -1)] 111$$

$$1 = 5 \cdot 200 + -9(111)$$

$$\text{So } x = 5$$

$$y = -9$$