

Final Project: Knapsack Algorithms - 20 points

Important: This assignment is longer than the others so it is a good idea to get an early start. Late assignments or assignments not meeting the specifications of the assignment WILL NOT BE ACCEPTED.

You have just started work at the **Fly-By-Night Consulting Company** and they have been approached by a secretive potential client. Your boss recognizes the client's problem as the classic 0-1 knapsack problem. This may be a great opportunity for your company if you can find the right implementation to solve the client's problem. However, as usual, **there are issues**:

- Your company has no experience with Knapsack Algorithms and you are the only one with any time to quickly come up to speed.
- The client refuses to give you many details about the characteristics of the problem, they are worried about losing an advantage they feel they have in their market. Your task is to help your company be able to recommend the right approach at the same meeting your company will sign a non-disclosure agreement. To get ready, your boss has asked you to explore different algorithmic approaches and make sure you know their strengths and weaknesses.

You are to explore four approaches to solving the 0-1 Knapsack Problem **using Java** (full enumeration/brute force, greedy, dynamic programming, and branch-and bound). To make sure you understand the tradeoffs between the different algorithms you must implement the algorithms and run them on some test data to compare their running time and solution accuracy. (You may look at other code, **but you must document its source.**) Each of the following components of the assignment should be done in a **separate method or class** that is easy to read and understand. **Generally** methods should be less than a page long. White space should be used sparingly to make it easy to read!

Ensure you can read in the problem correctly

A knapsack problem instance will be in a text file written in the form. C is the capacity and is an integer. N is the number of items, each item is preceded by its index that will serve as a unique identifier.

```
N
1  v1  w1
2  v2  w2
.  .    .
.  .    .
N  vN  wN
C
```

Full Enumeration

The 0-1 problem can be solved by a full enumeration of the search space. Every binary string of length N represents a subset and thus valid candidate solution. A method should loop through every possible binary string of length N and evaluates the value and weight of each of these solutions.

Output Upon termination, the program must output the solution the following format:

```
Using Brute force the best feasible solution found:  <value> <weight>
<item> <item> <item> ...
```

where the items are the indexes of the items to be placed in the knapsack, **items listed in ascending index order of the indices for the items specified in the file beginning with index 1.**

E.g.

```
Using Brute force the best feasible solution found:  234 17
1 3 7 12...
```

Greedy Search

Greedy search can be applied to the 0/1 Knapsack problem, but it is not guaranteed to give an optimal solution. Remember that a greedy search has the form:

```
While solution not constructed
  Select best remaining element and try adding it in
```

What is the sense of "best" here? What is the criterion by which the items should be ordered? In your implementation, first sort the items by **your criterion** so that you don't have to search through all of them each step. **Make sure your comments indicate your criterion and why it is a reasonable one to have chosen.**

Output Upon termination, the program should output the following:

```
Greedy solution (not necessarily optimal):  <value> <weight>
<item> <item> <item> ...
```

items listed in ascending index order as above.

Dynamic Programming

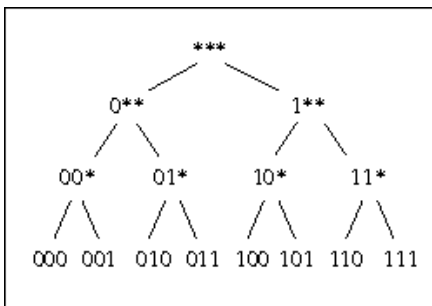
Output Upon termination, the program should output the following:

```
Dynamic Programming solution:  <value> <weight>
<item> <item> <item> ...
```

items listed in ascending index order as above.

Branch-and-Bound

You will recall that a branch-and-bound approach is based on a tree search. At each node of the tree is a **partial solution**, with some solution components (items) determined, and some not. At the leaves of the tree are complete solutions. A partial solution can be represented as a string such as **011011*******, where the *s represent the parts of the solution that are not specified. (There is always a block of 0s and 1s followed by a block of *s). All possible ways of filling in the remaining bits of the solution will be below this node in the tree. Here is a search tree for a problem with three items:



The Branch-and-Bound approach is to visit some of the internal nodes, but to prune off the subtrees of nodes where an optimal solution *cannot be*, thus reducing the number of nodes to be visited. To dismiss a node without expanding it, we use a bound function. **One option is the *fractional knapsack upper bound* discussed in the text on pages 436-438.** Your program must clearly document the fragment of code that gives the computation that you use for upper bound of a candidate solution.

Your branch-and-bound algorithm may use a **best-first search strategy** based on these bound values. If you choose to do this, then every time you program generates a partial solution that is feasible, it will calculate its bound value and then place the item in a **priority queue**. The item at the head of the queue (the one that will be served next) will be the partial solution with the best bound seen so far. **Other options are possible.** You should understand the pros and cons of whatever approach you use on computation time and space.

Output Upon termination, the program should output the following:

```
Using Branch and Bound the best feasible solution found:  <value> <weight>
<item> <item> <item> as specified for the other approaches.
```

Final Report

Your write up should be less than three typewritten pages – I will not accept longer write-ups and it must be in at least 12 point readable font with reasonable spacing. **If is not easy to read it does not get read. However in the past students have been leaving out too much detail: just giving a table and some bullet points without any explanation. This is will not earn you anywhere near full credit.** The writeup is important it counts for up to 8 points of the 20! It should reflect what you have learned about the different approaches. Details are important. In the past students have lost significant points for incorrect conclusions or generalizations.

The report should document the pros and cons of each approach and if and when a particular algorithmic approach might be appropriate for the potential client. Things to consider are: problem size, frequency of having to generate solutions, type of data, time to find a solution, etc. **You should have a table that summarizes the results.** Finally there should be a summary of some potential ways to improve any of the specific algorithms you have implemented. E.g. different data structures, different orderings of the data etc. Your goal is to communicate your understanding of the tradeoffs between the different approaches. **There must be a well written narrative of the pros and cons of each approach and possible improvements.**

Run greedy, dynamic programming, and branch-and-bound on the datasets easy.20.txt, easy50.txt, hard50.txt, easy.200.txt, and hard.200.txt. **Run full enumeration on easy.20.txt only.** **Note: You may have to halt your branch-and-bound early and take the best solution value to that point. Thus you will need to put a timer in your program to complete after a certain number of minutes and then print the results of your best solution found up to that point along with the time it ran.** You branch and bound is not required to complete on hard200.txt. You may find it challenging to have it complete on easy200 and/or hard50.txt but the best implementations will be able to do this.

Record your results in a table like the one below recording the best value found and the total weight if your program completes or the value and weight when the program is terminated by you. In addition, you may want to make comments about the length of time the program ran etc. In notes following the table document what you observed and learned. **Do not fudge the information in the table!**

| | easy20 | easy50 | hard50 | easy200 | hard200 |
|----------|---------------|-------------------|-------------------|-------------------|-------------------|
| Enum | value(weight) | Do not run | Do not run | Do not run | Do not run |
| Greedy | value(weight) | value(weight) | value(weight) | value(weight) | value(weight) |
| Dyn Prog | value(weight) | value(weight) | value(weight) | value(weight) | value(weight) |
| B'n'B | value(weight) | value(weight) | value(weight) | value(weight) | value(weight) |

At your demo you will submit the writeup and programs specified.

Deliverables: These are all due when you make your final submission. You will get up to 5 additional points if you **successfully demo and make your final submission of all the deliverables on December 3 in lab.**

0. Demo in lab, showing outputs for all the different algorithms.
1. Your three page typed report
2. Hardcopy of your method(s) that generate the greedy candidate solution.
3. Hardcopy of your method(s) that generate the dynamic programming solution.
4. Hardcopy of your method(s) that generate the branch and bound solution – this may be up to two pages.

The total number of pages you should hand in is 6-7. No cover page is necessary. The pages must be stapled and in the order indicated above with your name and calpoly username on the report. You are responsible for meeting these specifications. Only submissions that meet these specifications will be graded.