Assignment 2

1.1 Show that $k \lg k = \Theta(n)$ implies $k = \Theta\left(\frac{n}{n \ln n}\right)$.

$$k \ln k = \Theta(n) \Longrightarrow \Theta(k \ln k) = n$$

$$\ln[n] = \Theta(\ln[k \ln k]) \qquad = \Theta(\ln k + \ln \ln k)$$

$$= \Theta(\ln k) n \qquad = \Theta(k \ln k)$$

$$\frac{n}{\ln n} = \frac{\Theta(k \ln k)}{\Theta(\ln k)} = \Theta\left(\frac{k \ln k}{\ln k}\right) = \Theta(k) \frac{n}{\ln n} \qquad = \Theta(k) \Longrightarrow$$