

# ECES 632 Homework 4

John MacLaren Walsh, Ph.D.

ECES 632, Winter Quarter, AY09-10

1. **Project Proposal** Write an abstract, complete with background references, on a statistical signal processing problem or problem area interesting to you and/or relevant to your job/research that you would like to investigate for your course project. The abstract is to ensure that your assignment matches your interests. Email me your abstract when it is ready. Over email, you and I will use the abstract to craft a specific mini-research problem of reasonable but limited scope.
2. Write a MATLAB program which calculates the order 20 forward linear prediction coefficients for a real valued wide sense stationary Gaussian process with mean zero and auto-correlation

$$R[k] := \begin{cases} .2 \exp(-.5|k|) + .6 \exp(-.25|k|) & |k| \leq 20 \\ 0 & \text{otherwise} \end{cases}$$

using the Levinson-Durbin algorithm. Also calculate the MSE of the order 20 linear predictor using the Levinson-Durbin algorithm, and compare it with an empirically observed MSE which you calculate by running the linear predictor on a length 10000 randomly generated sample from the given Gaussian random process and averaging the squared error.

3. Select an audio wav file of your choice that contains speech and load it into Matlab. Speech is a quasi-stationary signal: on short segments (e.g. 32 millisecond blocks) it appears stationary, but it is in its changing spectrum across different such blocks in which carries its information.
  - (a) Using a spectrogram, find a temporal region of the file over which the spectrum appears to be constant. Select the portion of the audio file associated with this temporal region and build an autocorrelation estimate for this region. Generate a linear predictor from this autocorrelation estimate using Levinson Durbin. Record the performance you achieve with this.
  - (b) Compare the empirical average squared prediction error over the block you used to calculate the auto-correlation estimate with the theoretical MSE given by Levinson Durbin. Make a plot of these two values as a function of the maximal auto-correlation lag estimated. Why are these two numbers different from one another?
  - (c) Repeat this experiment, but by measuring the average squared prediction error over a larger block than the one you used to calculate the auto-correlation estimate. Choose the size of this block to be one over which you can see that spectral properties of the data changing in the spectrogram. How do your estimated squared prediction errors compare now with the ones you obtained with the smaller (original) block? Why?
4. Write a MATLAB function which implements the root-MUSIC frequency estimation method. Test it out on a length 1000 signal containing a sinusoid with frequency  $\omega_1 = 3\pi/8$  and phase 0 with amplitude .6, and a sinusoid at frequency  $\omega_2 = \pi/17$  with phase  $\pi/16$  and amplitude .2 observed through complex Gaussian white noise with variance  $\sigma^2 = 1$  and mean 0. Try other lengths and observe how the performance of the estimate varies with different lengths and different Monte Carlo trials.