

# HW14

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```
climate = read.table("http://www.stat.duke.edu/courses/Fall10/sta290/datasets/climate.dat", header = TRUE)
climate$T.M = factor(climate$T.M, labels = c("T","M"))
titles = c("Mg/Ca", "Alkenone", "Faunal", "Sr/Ca", "Del180", "IceCore", "Pollen", "Noble Gas")
climate$proxy = factor(climate$proxy, labels = titles)

X = model.matrix(lm(deltaT~.,data = climate))

# I'm losing the Mg/Ca. Just do it manually
climate = read.table("http://www.stat.duke.edu/courses/Fall10/sta290/datasets/climate.dat", header = TRUE)
climate$T.M = droplevels(factor(climate$T.M, labels = c("T","M")))
climate$proxy = droplevels(factor(climate$proxy, labels = titles))

dummies.prox = NULL
for(i in 1:length(titles)){
  dummies.prox = cbind(dummies.prox, as.numeric(climate$proxy == titles[i]))
}

colnames(dummies.prox) = titles

interaction1 = dummies.prox * climate$latitude
interaction2 = dummies.prox * climate$lat^2

interact.labels = c("Mg/Ca:lat1", "Alkenoe:lat1", "Faunal:lat1", "Sr/Ca:lat1", "Del180:lat1", "IceCore:lat1")
interact2.labels = c("Mg/Ca:lat2", "Alkenoe:lat2", "Faunal:lat2", "Sr/Ca:lat2", "Del180:lat2", "IceCore:lat2")
colnames(interaction1) = interact.labels
colnames(interaction2) = interact2.labels

Y = climate$deltaT
## Lasso
# Interactions first
X.int.first = as.matrix(cbind(interaction1, interaction2, dummies.prox, poly(climate$latitude, 2)))
first.prelim = cv.glmnet(X.int.first, climate$deltaT, alpha = 1)
best.lam.first = first.prelim$lambda.min
interaction.first = glmnet(X.int.first, Y, alpha = 1, lambda = best.lam.first)
int.first = coef(interaction.first)

# Interactions flipped
X.int.flipped = as.matrix(cbind(interaction2, interaction1, dummies.prox, poly(climate$latitude, 2)))
flipped.prelim = cv.glmnet(X.int.flipped, Y, alpha = 1)
best.lam.flipped = flipped.prelim$lambda.min
interaction.flipped = glmnet(X.int.flipped, Y, alpha = 1, lambda = best.lam.flipped)
int.flipped = coef(interaction.flipped)

# Poly first
X.poly.first = as.matrix(cbind(poly(climate$latitude, 2), dummies.prox, interaction1, interaction2))
poly.prelim = cv.glmnet(X.poly.first, Y, alpha = 1)
best.lam.poly = poly.prelim$lambda.min
```

```
poly.first = glmnet(X.poly.first,Y,alpha = 1, lambda = best.lam.poly)
poly.flipped = coef(poly.first)
```

```
round(int.first,3)
```

```
## 27 x 1 sparse Matrix of class "dgCMatrix"
```

```
##              s0
## (Intercept)  -2.874
## Mg/Ca:lat1    .
## Alkenoe:lat1  .
## Faunal:lat1   0.006
## Sr/Ca:lat1    .
## Del180:lat1   0.011
## IceCore:lat1  0.141
## Pollen:lat1   .
## Noble Gas:lat1 .
## Mg/Ca:lat2    .
## Alkenoe:lat2  .
## Faunal:lat2   .
## Sr/Ca:lat2    .
## Del180:lat2   0.001
## IceCore:lat2  .
## Pollen:lat2   -0.002
## Noble Gas:lat2 .
## Mg/Ca         .
## Alkenone       0.072
## Faunal         0.574
## Sr/Ca          -1.666
## Del180         .
## IceCore        -0.120
## Pollen         -1.286
## Noble Gas      -1.977
## 1              .
## 2              -0.894
```

```
round(int.flipped,3)
```

```
## 27 x 1 sparse Matrix of class "dgCMatrix"
```

```
##              s0
## (Intercept)  -2.849
## Mg/Ca:lat2    .
## Alkenoe:lat2  .
## Faunal:lat2   .
## Sr/Ca:lat2    .
## Del180:lat2   0.001
## IceCore:lat2  -0.015
## Pollen:lat2   -0.002
## Noble Gas:lat2 .
## Mg/Ca:lat1    .
## Alkenoe:lat1  .
## Faunal:lat1   0.003
## Sr/Ca:lat1    .
## Del180:lat1   0.009
## IceCore:lat1  0.005
```

```
## Pollen:lat1      .
## Noble Gas:lat1   .
## Mg/Ca            .
## Alkenone         0.027
## Faunal           0.529
## Sr/Ca            -1.640
## Del180           .
## IceCore          .
## Pollen           -1.270
## Noble Gas        -1.962
## 1                .
## 2                -0.720
```

```
round(poly.flipped,3)
```

```
## 27 x 1 sparse Matrix of class "dgCMatrix"
##              s0
## (Intercept)  -2.684
## 1            .
## 2            -1.175
## Mg/Ca        .
## Alkenone     0.383
## Faunal       0.656
## Sr/Ca        -2.405
## Del180       -1.121
## IceCore      -2.294
## Pollen       -1.535
## Noble Gas    -2.699
## Mg/Ca:lat1   0.006
## Alkenoe:lat1 -0.004
## Faunal:lat1  0.038
## Sr/Ca:lat1   .
## Del180:lat1  0.013
## IceCore:lat1 0.031
## Pollen:lat1  -0.044
## Noble Gas:lat1 .
## Mg/Ca:lat2   .
## Alkenoe:lat2 -0.002
## Faunal:lat2  -0.001
## Sr/Ca:lat2   .
## Del180:lat2  0.004
## IceCore:lat2 0.000
## Pollen:lat2  -0.005
## Noble Gas:lat2 .
```

Discussion? Is this due to me just changing the  $\lambda$

```
# Bayesian Horseshoe
# Interactions first
X.int.first = as.matrix(cbind(interaction1,interaction2,dummies.prox,poly(climate$latitude,2)))
int.first.bhs = bhs(X.int.first,Y,T=10000)
int.first.bhs.coef = colMeans(int.first.bhs$beta)
names(int.first.bhs.coef) = c(interact.labels,interact2.labels,titles,"lat1","lat2")

# Interactions flipped
X.int.flipped = as.matrix(cbind(interaction2,interaction1,dummies.prox,poly(climate$latitude,2)))
```

```

int.flipped.bhs = bhs(X.int.flipped,Y,T=10000)
int.flipped.bhs.coef = colMeans(int.flipped.bhs$beta)
names(int.flipped.bhs.coef) = c(interact2.labels,interact.labels,titles,"lat1","lat2")

# Poly first
X.poly.first = as.matrix(cbind(poly(climate$latitude,2),dummies.prox,interaction1,interaction2))
poly.first.bhs = bhs(X.poly.first,Y,T=10000)
poly.first.bhs.coef = colMeans(poly.first.bhs$beta)
names(poly.first.bhs.coef) = c("lat1","lat2",titles,interact.labels,interact2.labels)

round(int.first.bhs.coef,3)

```

```

##      Mg/Ca:lat1  Alkenoe:lat1  Faunal:lat1  Sr/Ca:lat1  Del180:lat1
##      0.004      -0.002      0.010      0.002      0.010
##      IceCore:lat1  Pollen:lat1  Noble Gas:lat1  Mg/Ca:lat2  Alkenoe:lat2
##      0.062      -0.007      -0.005      0.000      -0.001
##      Faunal:lat2  Sr/Ca:lat2  Del180:lat2  IceCore:lat2  Pollen:lat2
##      0.000      -0.002      0.002      -0.006      -0.002
##      Noble Gas:lat2  Mg/Ca  Alkenone  Faunal  Sr/Ca
##      0.000      0.382      0.501      0.822      -1.188
##      Del180  IceCore  Pollen  Noble Gas  lat1
##      -0.132      -0.535      -1.262      -1.757      0.116
##      lat2
##      -0.822

```

```
round(int.flipped.bhs.coef,3)
```

```

##      Mg/Ca:lat2  Alkenoe:lat2  Faunal:lat2  Sr/Ca:lat2  Del180:lat2
##      0.000      -0.001      0.000      -0.002      0.002
##      IceCore:lat2  Pollen:lat2  Noble Gas:lat2  Mg/Ca:lat1  Alkenoe:lat1
##      -0.006      -0.002      0.000      0.004      -0.002
##      Faunal:lat1  Sr/Ca:lat1  Del180:lat1  IceCore:lat1  Pollen:lat1
##      0.010      0.002      0.010      0.060      -0.006
##      Noble Gas:lat1  Mg/Ca  Alkenone  Faunal  Sr/Ca
##      -0.004      0.418      0.546      0.872      -1.134
##      Del180  IceCore  Pollen  Noble Gas  lat1
##      -0.131      -0.542      -1.221      -1.721      0.099
##      lat2
##      -0.858

```

```
round(poly.first.bhs.coef,3)
```

```

##      lat1      lat2      Mg/Ca      Alkenone      Faunal
##      0.104      -0.812      0.374      0.493      0.805
##      Sr/Ca      Del180      IceCore      Pollen      Noble Gas
##      -1.157      -0.142      -0.535      -1.252      -1.781
##      Mg/Ca:lat1  Alkenoe:lat1  Faunal:lat1  Sr/Ca:lat1  Del180:lat1
##      0.004      -0.002      0.010      0.002      0.010
##      IceCore:lat1  Pollen:lat1  Noble Gas:lat1  Mg/Ca:lat2  Alkenoe:lat2
##      0.060      -0.007      -0.005      0.000      -0.001
##      Faunal:lat2  Sr/Ca:lat2  Del180:lat2  IceCore:lat2  Pollen:lat2
##      0.000      -0.002      0.002      -0.007      -0.002
##      Noble Gas:lat2
##      0.000

```

It is interesting to note that in our first two lasso models where the interactions come first but are flipped,

there isn't that much change. Many of the same variables that are shrunk to zero are still zero, and many of the coefficients are the same. However, when we put our poly term first, there are more terms included, which is suprising because in the lasso the order shouldn't matter.

Also, under our bayesian horseshoe models, it seems like there are consistently more coefficients not zero. As far as measures of uncertainty are concerned, it seems clear that lasso won't really have measures of uncertainty, but a clear benefit of doing the bayesian horseshoe are the measures of uncertainty where we could calculate credible intervals quite easily