

Assignment 2

1. A. Sample space =
 $s\{HHHH, THHH, HHHT, THHT, HHTH, THTH, HHTT, THTT, HTHH, TTHH, HTHT, TTHT, HTTH, TTTH, HTTT, TTTT\}$
 B. $\Pr(A) = 1/2$ (50%)
 C. $\Pr(B) = 6/16 = 3/8$ (37.5%)
 D. $\Pr(A \text{ and } B) = P(A)+P(B)-P(AB) = 1/2 + 3/8 - 3/16 = 11/16$ (68.75%)
 E. $E[X] = P(X=0) = 1/16, P(X=1) = 4/16, P(X=2) = 6/16, P(X=3) = 4/16, P(X=4) = 1/16$
 $0(1/16)+1(4/16)+2(6/16)+3(4/16)+4(1/16) = 2$
 We would expect 2 heads to appear in 4 fair coin flips.

2. A. $P = 1/4, 1/p = 1/(1/4) = 4$. 4 flips until heads appears.
 B. $P(H==T) = (n \text{ choose } n/2) (1/4)^n (3/4)^{n-n/2}$; n is the number of coin flips

3. Given that we will go through our array of unsorted a maximum of $n/2$ times before we get a good pivot and the run time for partitioning is $O(n)$. This gives us a runtime of $O(n^2)$ For the recursive part of the equation we will take $T(n/4)$ and $T(3n/4)$, this is assuming we pick the worst good pivot and have a split of the array between $1/4$ and $3/4$. This gives the following recurrence equation of:

$$T(n) = T(n/4) + T(3n/4) + O(n^2)$$

$$T(n) = 2T(3n/4) + O(n^2)$$

$$a=2, b=4/3, c=2$$

$$\log_{4/3} 2 > 2$$

Using the masters theorem this solves to $\Theta(n^{\log_{4/3} 2})$ which is the worst case time complexity for the given algorithm.

4.a

Key	Value
0	
1	20
2	16,5
3	44,88,11
4	94,39
5	12,23
6	

Key	Value
7	
8	
9	13
10	

b.

Key	Value
0	11
1	39
2	20
3	5
4	16
5	44
6	88
7	12
8	23
9	13
10	94

c.

Key	Value
0	16
1	11
2	88
3	20
4	23
5	44
6	94
7	12
8	39

Key	Value
9	13
10	5

d.

Key	Value
0	11
1	23
2	20
3	16
4	39
5	44
6	94
7	12
8	88
9	13
10	5

5. $a = n/m$ (n keys, m slots) =load factor

Successful Search: $\Theta(1 + a)$

-this is the same as an unsorted linked list

Unsuccessful search: $\Theta(1 + a)$

-this will be slightly faster with a sorted list, but still have to factor in the load factor

Insertion: $\Theta(1 + a)$

-same as a successful search

Deletion: $\Theta(1)$ (if doubly linked list) or $\Theta(1 + a)$ (if singly linked list)

Professor Marley's hypothesis is incorrect, there is no substantial performance gains.