

1. Calculate the third iterate of the logistic map with  $r = 2.5$  starting from  $x_0 = 0.5$ . Do this by hand. What is the third iterate you calculated? (choose the one that's closest; different computers and calculators do arithmetic slightly differently, so your answer may vary a bit).

$$x_3 = 0.586$$

$$x_3 = 0.606$$

$$x_3 = 0.625$$

2. Write a simple program that uses a loop to compute a specified number  $n$  of iterates of the logistic map, starting from a specified initial condition  $x_0$ , with a specified  $r$  parameter. Your program should take  $n$ ,  $x_0$ , and  $r$  as inputs or arguments. Check your program against the answer to the first problem above.

Using your program, compute the tenth iterate of the logistic map starting from  $x_0 = 0.2$ , with  $r = 2.6$ . What is the tenth iterate? Again, choose the value that's closest to what your program produced.

$$x_{10} = 0.6149$$

$$x_{10} = 0.5999$$

$$x_{10} = 0.6157$$

3. Point your browser to:

<http://tuvalu.santafe.edu/~jgarland/LogisticTools.html>

Use the application to compute and plot the first 50 iterates of the logistic map from  $x_0 = 0.2$  and  $r = 2$ . *Hint: you'll need to hit the "restart simulation" button after entering those values in the dialog boxes.* For now, ignore the plots on the left and the bottom of the window; we'll come back to those. Does the orbit (top right plot) reach a fixed point?

Yes

No

4. Using the same application, plot the first 50 iterates of the logistic map with  $r = 2.7$  starting from  $x_0 = 0.2$ . Does the orbit reach a fixed point?

Yes

No

5. If the orbits in questions 3 and 4 both reached a fixed point, is it at the same value of  $x$ , *i.e.*, is it the same fixed point?

Yes

No

One or both did not reach a fixed point.