Name: _	
Email address:	

CSE 373 Autumn 2010: Midterm #2 (closed book, closed notes, NO calculators allowed)

Instructions: Read the directions for each question carefully before answering. We may give partial credit based on the work you write down, so if time permits, show your work! Use only the data structures and algorithms we have discussed in class or that were mentioned in the book so far.

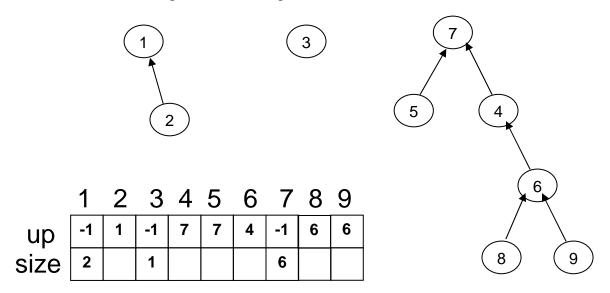
Note: For questions where you are drawing pictures, please circle your final answer for any credit.

Good Luck!

Total: 61 points. Time: 50 minutes.

Question	Max Points	Score		
1	11			
2	10			
3	10			
4	6			
5	8			
6	16			
Total	61			

1) [11 points total] Disjoint Sets: Given the array representation of up-trees discussed in class (where size[x] = total number of values in set x, and up[x] == -1 indicates that node x is a root node), for example (size is unspecified for non-root nodes):



a) [6 points] Fill in the code below for **Union by Size** (weighted Union) (does not have to be perfect Java code). (On a tie in size, the set referred to by the second parameter should be added to the set referred to by the first.)

```
int up[N];
int size[N];

void Union(int x, int y) {
     // Assuming x and y are roots of two different sets,
     // fill in code to implement union by size (weight)
     // Break ties in size by adding the set y
     // to the set x.
```

1) (cont) b) (1 pts) Now, draw the <u>set of uptrees</u> that results from executing a find(9) with path compression on the sets shown in on the previous page. You may update the set of uptrees on the previous page or redraw the sets here. If no changes occur, state that.						
c) (2 pts) Update the <u>array</u> to reflect the changes (if any) caused by that find operation. You may update the <u>array</u> on the previous page or redraw the array here. If no changes occur, state that.						
d) (2 pts) What is the worst case running time of a single find operation if union by size and path compression are used? $N = total \# of elements in all sets.$ (no explanation required)						

2) [10 points total] Hashing: Draw the contents of the two hash tables below. Show your work for partial credit. *If an insertion fails, please indicate which values fail and attempt to insert any remaining values*. The size of the hash table is 7. The hash function used is $H(k) = k \mod 7$

13, 17, 6, 24, 3

a) Separate chaining, where each bucket points to a sorted linked list.

0	
1	
2	
3	
4	
5	
6	

b) Double hashing, where $H2(k) = 7 - (k \mod 5)$

0	
1	
2	
3	
4	
5	
6	

- **2) (cont)**
- c) (1 pt) What is the **load factor** for the table a)?
- d) (1 pt) What is the **load factor** for the table b)?

3) [10 points total] Leftist Heaps:

a) [8 pts] Draw the *leftist* heap that results <u>from inserting</u>: 75, 28, 7, 61, 15, 55, 19, 4 in <u>that order</u> into an initially empty heap. You are only required to show the final heap, although if you draw intermediate heaps, <u>please circle your final result for ANY credit</u>.

- **3**) (cont)
- b) [2 pts] What is the null path length of the **root** in your final heap from part a)?

4) [6 points] Skew Heaps

Draw the skew heap that results from doing a **deletemin** on the skew heap shown below. You are only required to show the final tree, although if you draw intermediate trees, *please circle your final result for ANY credit*.

5) [8 points] Memory Hierarchy & Locality: Examine the code example below:

```
c[1] = 5;
z = 68;
j = 2;
while (j < 2000) {
    a[j] = a[j] + a[j-1];
    z = b[10] + z;
    System.out.println("d[j] = " + d[j]);
    j = j + 1;
}
f[25] = 60;
y = c[2000] + c[2001] + c[2002] + c[2003]</pre>
```

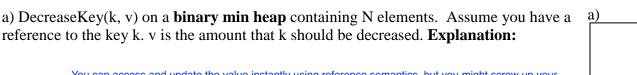
Considering only their use in the code segment above, for each of the following variables, indicate below what type of locality (if any) is demonstrated. Please circle *all that apply* (you may circle more than one item for each variable):

a	spatial	locality	temporal	locality	no	locality
b	spatial	locality	temporal	locality	no	locality
С	spatial	locality	temporal	locality	no	locality
d	spatial	locality	temporal	locality	no	locality
f	spatial	locality	temporal	locality	no	locality
j	spatial	locality	temporal	locality	no	locality
У	spatial	locality	temporal	locality	no	locality
Z	spatial	locality	temporal	locality	no	locality

6) [16 points total] Running Time Analysis:

- Describe the most time-efficient way to implement the operations listed below. Assume no duplicate values and that you can implement the operation as a member function of the class – with access to the underlying data structure.
- Then, give the tightest possible upper bound for the worst case running time for each operation in terms of N. **For any credit, you must explain why it gets this worst case running time. You must choose your answer from the following (not listed in any particular order), each of which could be re-used (could be the answer for more than one of a) -f)).

 $O(N^2)$, $O(N^{\frac{1}{2}})$, $O(N \log N)$, O(N), $O(N^2 \log N)$, $O(N^5)$, $O(2^N)$, $O(N^3)$, $O(\log N)$, O(1), $O(N^4)$, $O(N^N)$, $O(N^6)$, $O(N (\log N)^2)$, $O(N^2 (\log N)^2)$



You can access and update the value instantly using reference semantics, but you might screw up your binary min heap. In the worst case, this item has to percolate all the way up the heap, leading to an O(log N)

- b) Inserting an element in a **hash table** containing N elements where separate chaining is used and each bucket points to a sorted linked list. The table size = N. **Explanation**:
- c) Converting a **4-heap** (a d-heap where d=4) containing N elements into a **binary min** heap. Explanation:
- d) Rehashing values from a **hash table** containing 2N elements (where separate chaining is used and each bucket points to a sorted linked list). The original hash table size = N, the new hash table is size 2N. Explanation: