

ZAEEM YOUSAF (119-1196 3E2)

submitted to: Amina Khan (DS assignment 2)

Workout of Time Complexity

Contents

1 Q1/B Time complexity of iterative mirror	1
1.1 Detail	1
2 Q2/B Time complexity of spiral order traversal	1
2.1 Detail	2
3 Q4/B Time complexity of flattening a Binary Tree	2
3.1 Detail	2
4 Q5/B Time complexity of joining Two AVL Trees	2
4.1 Detail	2

1 Q1/B Time complexity of iterative mirror

ans: $O(n)$

1.1 Detail

all right nodes were pushed and popped $O(\log n)$ each time, a popped node's children were swapped and total time $O(n)$ max height of stack was the $n/2$. Tree was traversed from top to bottom while each time moving left and storing the right children to be treated afterward. *Total $O(\log_2 n) + O(n) = O(n) * p$

2 Q2/B Time complexity of spiral order traversal

ans: $O(n) + O(n) = O(n)$

2.1 Detail

Two Stacks were used. 'left_{toright}' and 'right_{toleft}' traversal was made level wise to push all elements from left to right and then right to left. $O(n)$ was for traversal as each node was visited and $O(n)$ was for pushing and then popping each element.

3 Q4/B Time complexity of flattening a Binary Tree

ans: $O(n)$

3.1 Detail

each node was visited recursively preorder and that node was inserted in **linkList** object. Note: Each node was inserted instead of data which was more difficult but it gives the real picture of how the tree was flattened. Therefore my flattened list looks like

4 Q5/B Time complexity of joining Two AVL Trees

ans: $O(h_1 + h_2)$ where h_1 is the height of T_1 and h_2 is the height of T_2 Note: T_2 is not merged node by node, Whole tree is attached at once almost

4.1 Detail

T_2 's smallest Element was broken and made root of new tree T_3 . Then T_1 was traversed right until height becomes $= h_2$ Then T_1 was broken in two parts at that that root and was connected to left of T_3 T_2 was attached on the right side of T_3 Then that T_3 was attached to parent of broken node in T_1 Node breaking is constant and this algorithm is very efficient for AVL trees with greater heights. $O(h_1 + h_2)$ is just due to traversal for the appropriate place where one T_2 could be attached.