

④ magnetic flux density (B):

The magnetic flux per unit area through a loop of small area is called the magnetic flux density, B , at the location of the loop.

It is a vector quantity. Its unit is tesla or weber/m².

The magnetic flux through any closed surface is the surface integral of the normal component of \vec{B} , that is

$$\phi = \int_S B_n da = \int_S \vec{B} \cdot d\vec{a}.$$

④ magnetic field strength H & magnetomotive force \mathcal{F} :

In a homogeneous medium, \vec{B} is related to the current \vec{I} through

$$\vec{B} \propto \frac{\mu \vec{I}}{r} \quad \text{①}$$

r = distance from the wire

μ = constant depends upon the medium.

μ is called the permeability and may be written as

$$\mu = \mu_v \mu_r$$

μ_v = absolute permeability

$$= 4\pi \times 10^{-7} \text{ H/m}$$

μ_r = relative permeability

$$= 1 \text{ (in vacuum)}$$

$$\approx 1 \text{ (in air)}$$

$$\therefore \mu = \mu_v$$

The proportionality factor is found to be $\frac{1}{2\pi}$, so the relation becomes

$$\vec{B} = \frac{\mu \vec{I}}{2\pi r} = \mu \vec{H}$$

where, $\vec{H} = \frac{\vec{I}}{2\pi r}$ A/m

The line integral is

$$\mathcal{F} = \int_a^b \vec{H} \cdot d\vec{s}$$

is defined as the magnetomotive force between the points a and b .

For the circular path,

$$\oint \vec{H} \cdot d\vec{s} = I$$

This equation known as Ampere's work law or Ampere's circuital law.

$$\oint \vec{H} \cdot d\vec{s} = nI$$

where n = number of turns.

$$\therefore H \approx \frac{I}{2\pi R} = \frac{\oint \vec{H} \cdot d\vec{s}}{2\pi R} = \frac{nI}{2\pi R} \quad \text{ampere-turns/m}$$

where $l = 2\pi R$ = length of the coil.

⊞ Ampere's work law in differential form:

$$\vec{\nabla} \times \vec{H} = \vec{J}$$

⊞ Maxwell's equations:

The electromagnetic equations are known as Maxwell's equations.

Differential form:

$$i) \vec{\nabla} \times \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$$

$$ii) \vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$iii) \vec{\nabla} \cdot \vec{D} = \rho$$

$$iv) \vec{\nabla} \cdot \vec{B} = 0$$

Integral form

$$i) \oint \vec{H} \cdot d\vec{s} = \int (\vec{J} + \frac{\partial \vec{D}}{\partial t}) \cdot d\vec{a}$$

$$ii) \oint \vec{E} \cdot d\vec{s} = -\int \frac{\partial \vec{B}}{\partial t} \cdot d\vec{a}$$

$$iii) \oint \vec{D} \cdot d\vec{a} = \int \rho dV$$

$$iv) \oint \vec{B} \cdot d\vec{a} = 0$$

Magnetic field:

The area around a magnet within which magnetic force is exerted, is called a magnetic field.

It is produced by moving electric charge.

Difference Electric & magnetic field:

Electric

i) created around electric charge.

ii) Its unit is N/m or V/m

iii) Its pole is monopole or dipole.

magnetic

i) created around moving electric charge & magnet

ii) Its unit is Gauss or Tesla.

iii) Its pole is dipole

Faraday's induction law: $\vec{E} = -\frac{d\vec{B}}{dt}$

Statement:

The induced electromotive force in any closed circuit is equal to the negative of the time rate of change of the magnetic flux enclosed by the circuit.

$$\therefore \text{EMF} = - \frac{d\phi}{dt}$$

$$\therefore V = - \frac{d\phi}{dt}$$

* magnetomotive force is called magnetic voltage.

The first two maxwell eqn. can be stated

i) the magnetic voltage around a closed path is equal to the electric current through the path.

$$\oint \vec{H} \cdot d\vec{l}$$

$$V = I$$

ii) the electric voltage through the path is equal to the magnetic current through the path.

$$I = \oint \vec{D} \cdot d\vec{A}$$

Stokes theorem:

$$\oint_C \vec{A} \cdot d\vec{s} = \int_S \vec{\nabla} \times \vec{A} \cdot d\vec{A}$$

$$d\vec{s} = \hat{r} ds \quad \text{and} \quad d\vec{A} = \hat{n} dA.$$

magnetic flux:

magnetic flux is a measurement of the total magnetic field which passes through a given area.

$$\phi = A \cdot B \cos \theta \quad \left| \begin{array}{l} A = \text{Area} \\ B = \text{magnetic flux density} \end{array} \right.$$

magnetic field strength (H):

It is a vector quantity, having the same direction as the magnetic flux density.

It is denoted by \vec{H} .

$$\vec{H} = \frac{\vec{B}}{\mu}$$