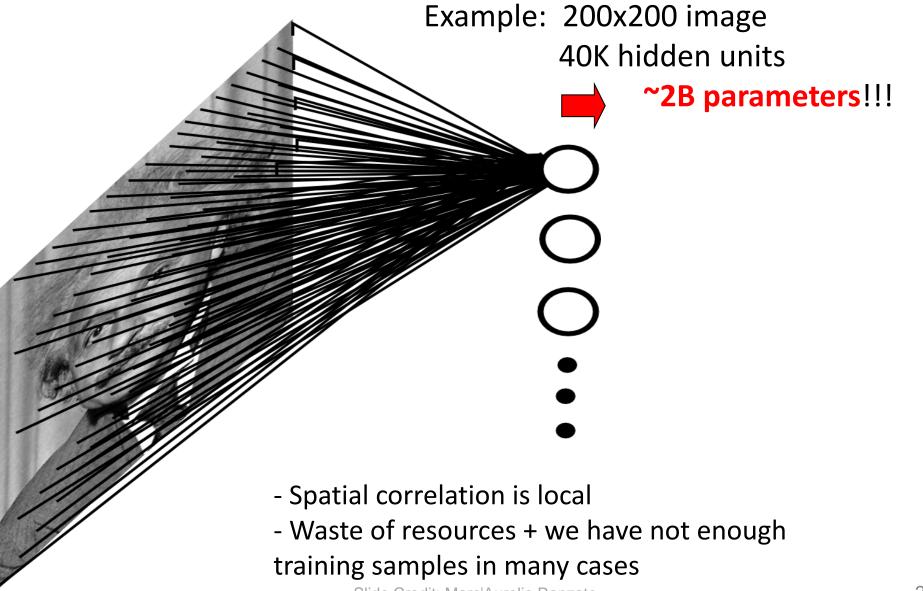
#### **COMP/EECE 7/8740 Neural Networks**

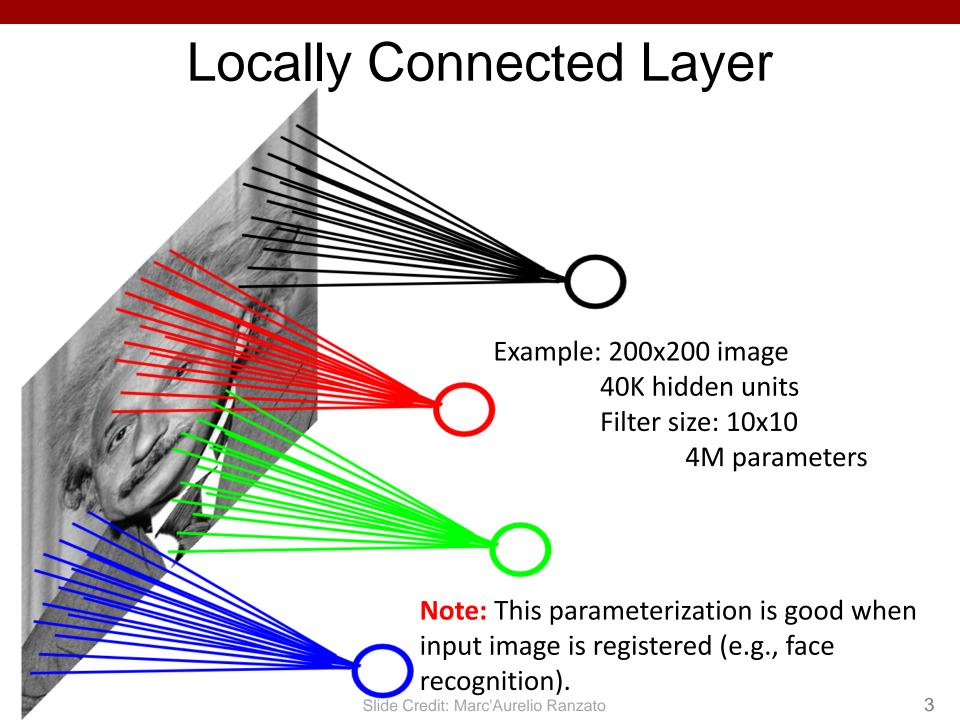
#### Topics:

- Fully connected to convolution layer
- Convolutional operations
  - Stride size and padding
- Convolutional Neural Networks
  - Convolution layers
  - Activation layers
  - Pooling layers

Md Zahangir Alom Department of Computer Science University of Memphis, TN

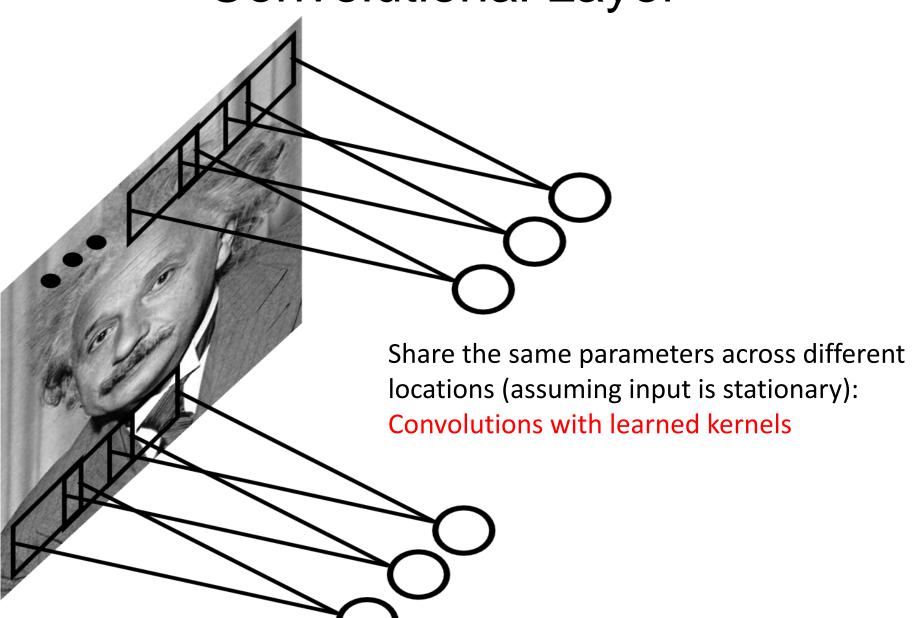
#### Fully Connected Layer





Locally Connected Layer **STATIONARITY?** Statistics is similar at different locations

Slide Credit: Marc'Aurelio Ranzato

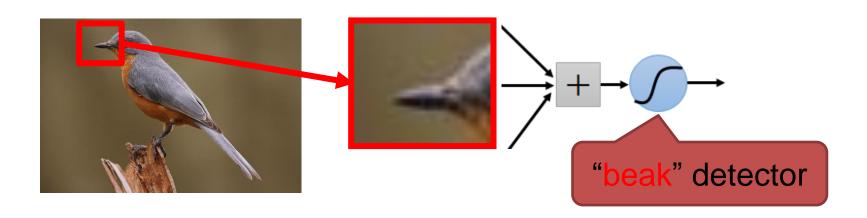


edit: Marc'Aurelio Ranzato

#### Consider learning an image:

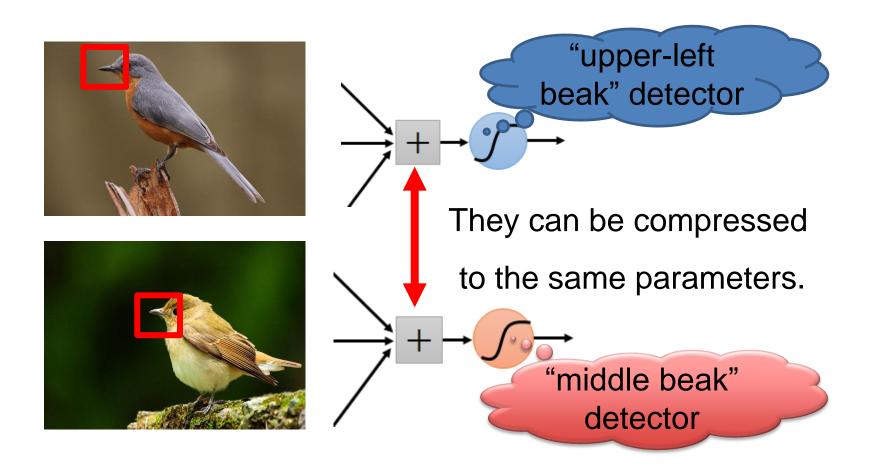
Some patterns are much smaller than the whole image

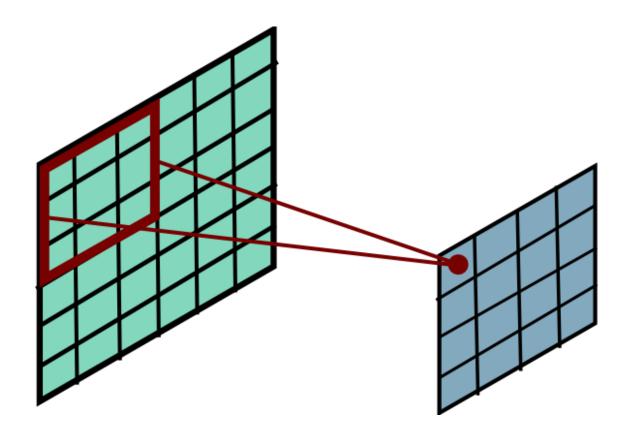
Can represent a small region with fewer parameters

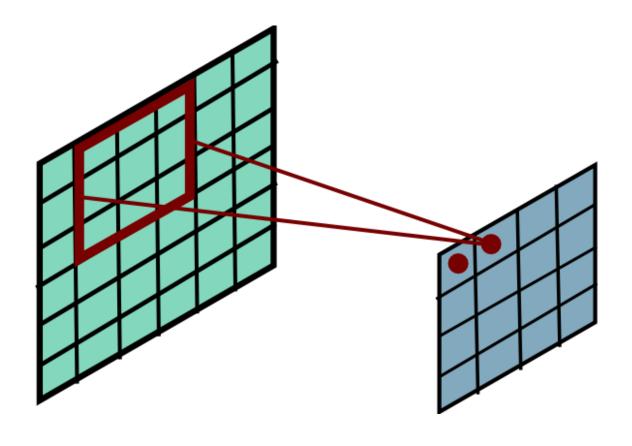


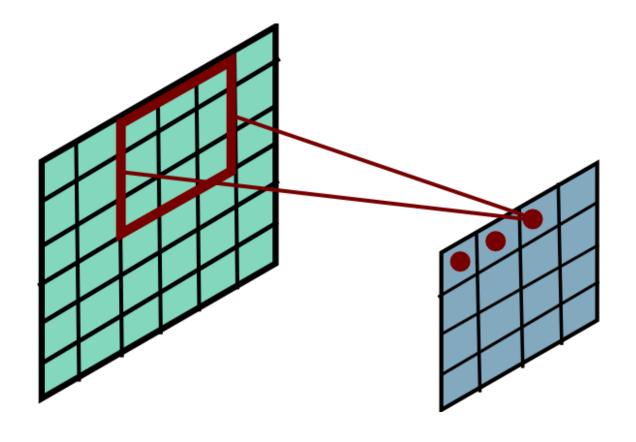
# Same pattern appears in different places: They can be compressed!

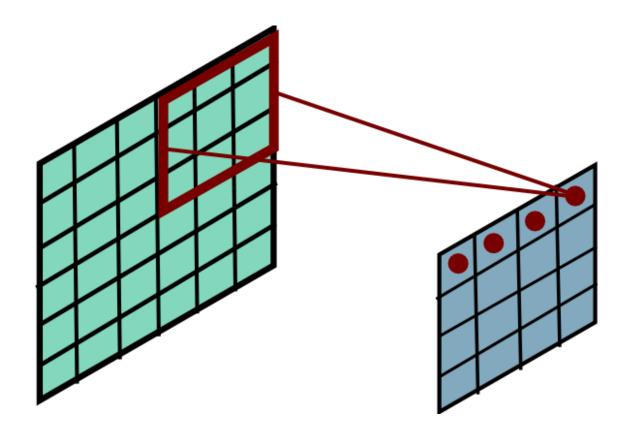
What about training a lot of such "small" detectors and each detector must "move around".

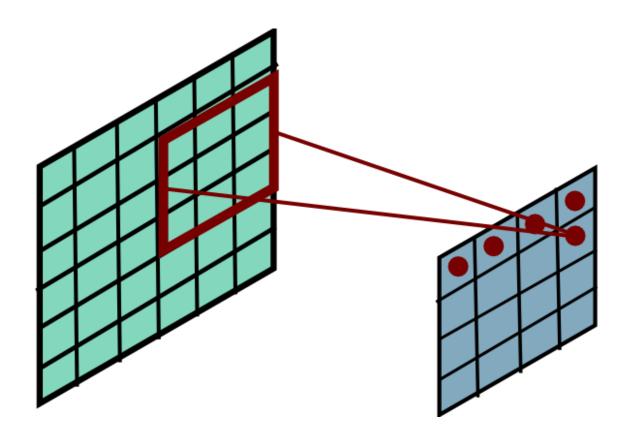


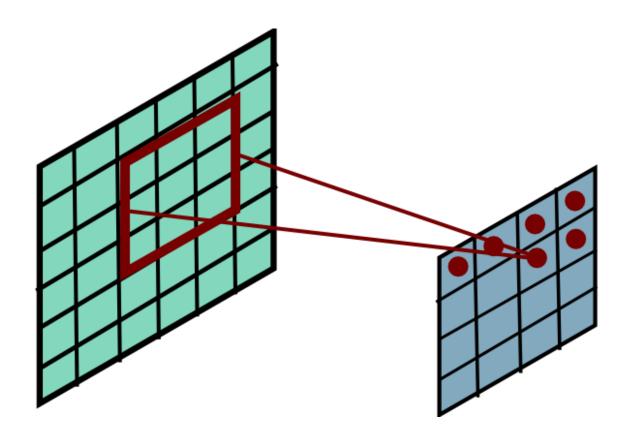


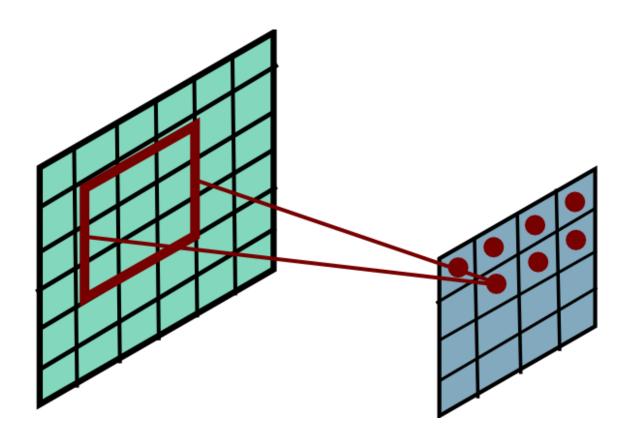


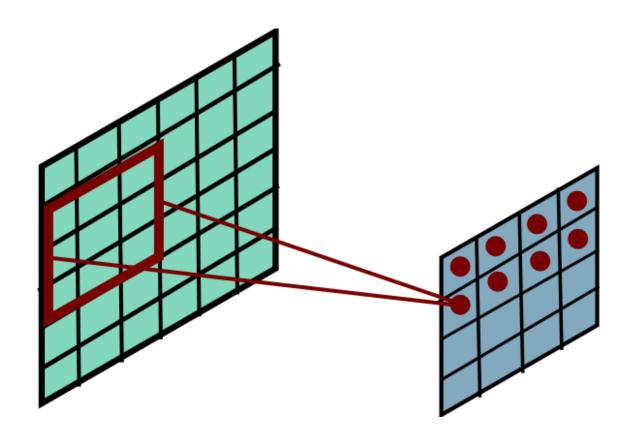


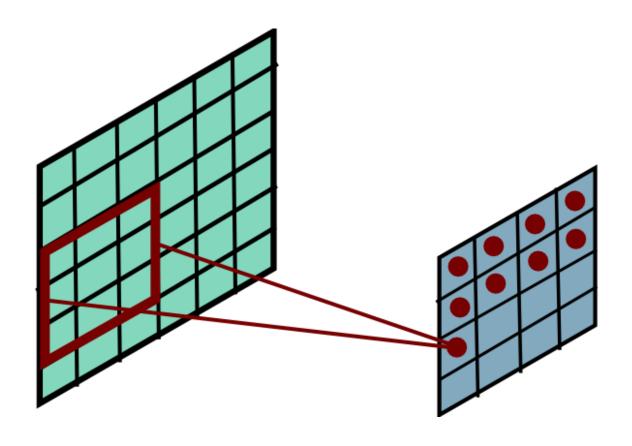




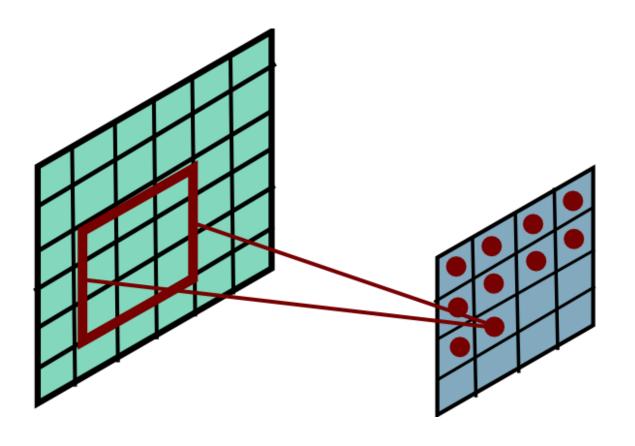


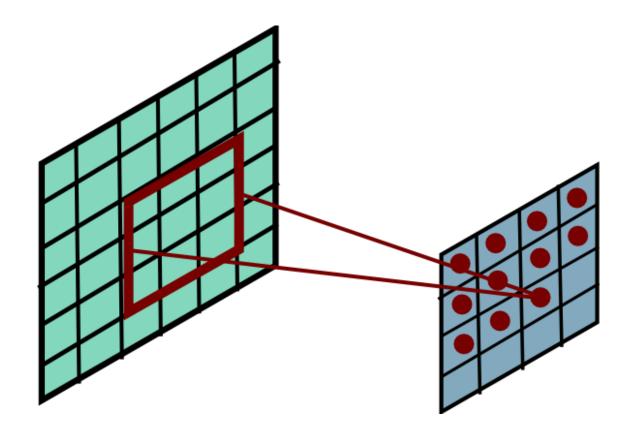


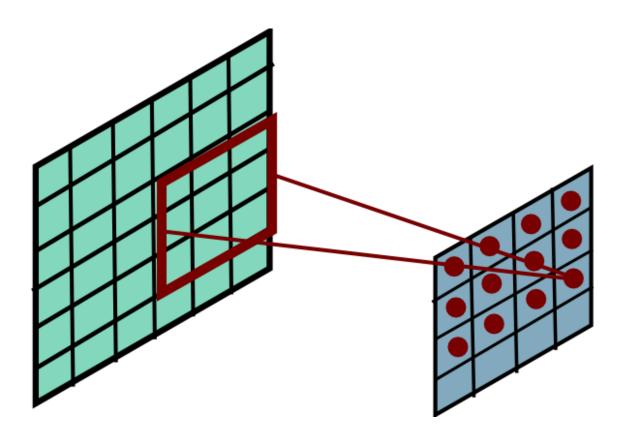


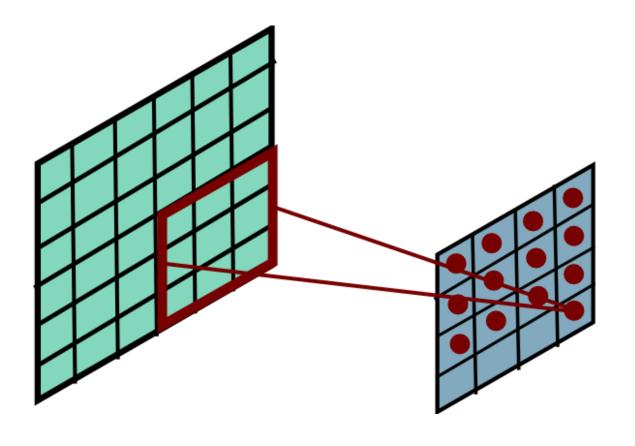


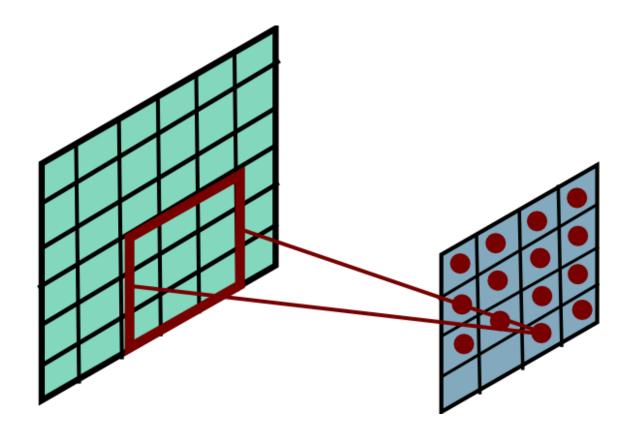
16

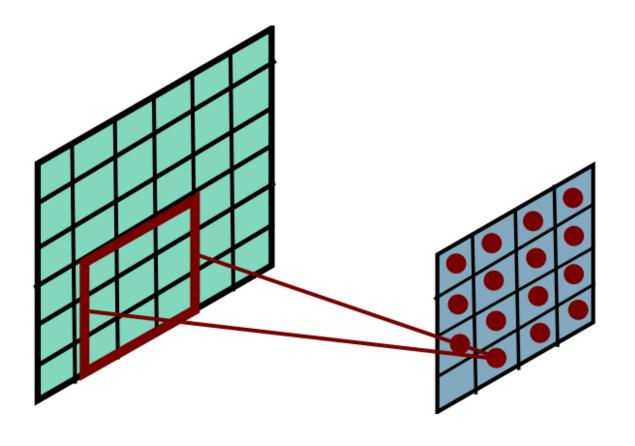


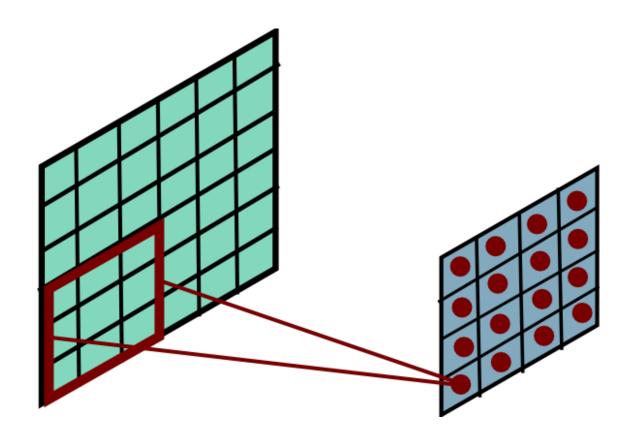












Mathieu et al. "Fast training of CNNs through FFTs" ICLR 2014

#### Convolution

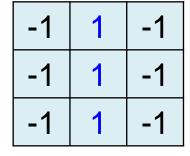
These are the network parameters to be learned.

1	0	0	0	0	1
0	~	0	0	~	0
0	0	1	1	0	0
1	0	0	0	1	0
0	1	0	0	1	0
0	0	1	0	1	0

6 x 6 image

1	-1	-1
-1	7	1
-1	-1	1

Filter 1



Filter 2

: :

Each filter detects a small pattern (3 x 3).

# 

Filter 1

stride=1

1	0	0	0	0	1
0	1	0	0	1	0
0	0	1	1	0	0
1	0	0	0	1	0
0	1	0	0	1	0

Dot

product

3

-1

6 x 6 image

# Convolutio 1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1

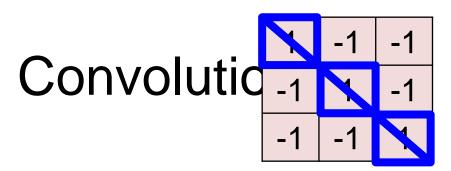
Filter 1

If stride=2

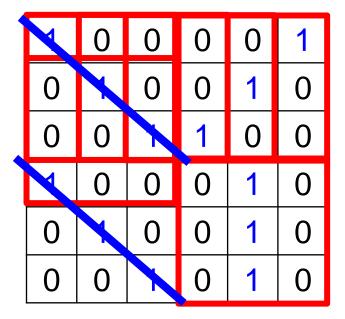
1	0	0	0	0	1
0	1	0	0	1	0
0	0	1	1	0	0
1	0	0	0	1	0
0	1	0	0	1	0
0	0	1	0	1	0

3 -3

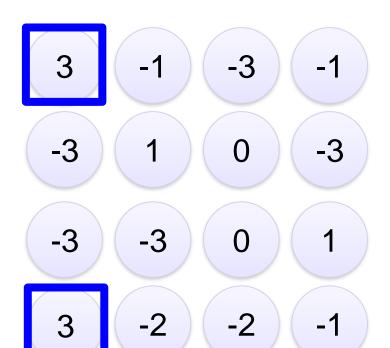
6 x 6 image



stride=1



6 x 6 image



Filter 1

# Convolutio

-1	1	-1
-1	1	-1
-1	1	-1

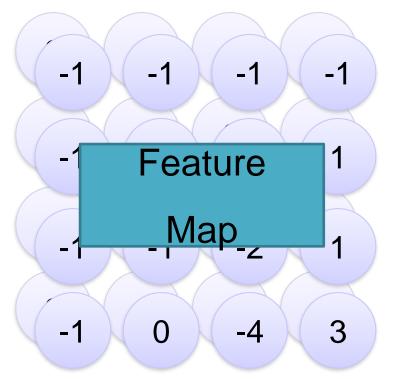
Filter 2

stride=1

1	0	0	0	0	1
0	1	0	0	1	0
0	0	1	1	0	0
1	0	0	0	1	0
0	1	0	0	1	0
0	0	1	0	1	0

6 x 6 image

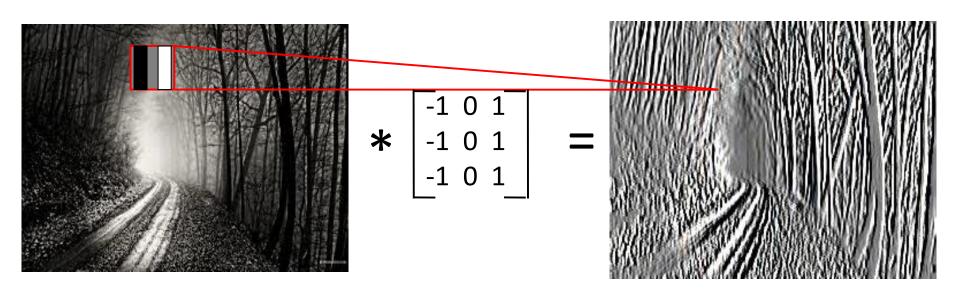
#### Repeat this for each filter



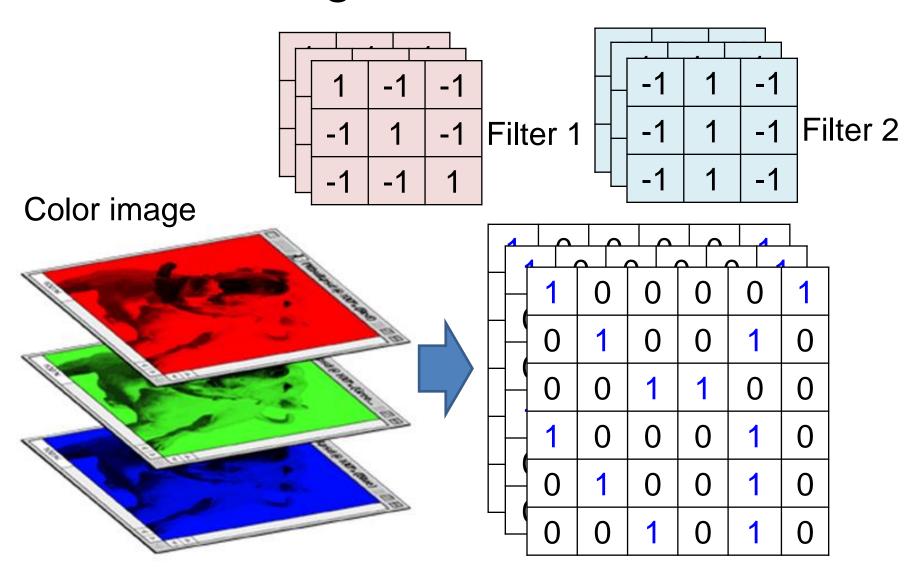
Two 4 x 4 images

Forming 2 v A v A matrix

#### Example: convolutional



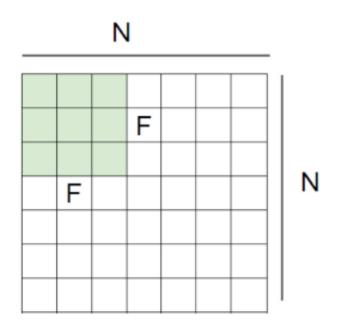
#### Color image: RGB 3 channels



#### Convolution: output dimension

- Stride controls how the filter convolves around the input volume.
- The amount by which the filter shifts is the stride.

Output size: (N - F) / stride + 1 e.g. N = 7, F = 3: stride 1 => (7 - 3)/1 + 1 = 5 stride 2 => (7 - 3)/2 + 1 = 3 stride 3 => (7 - 3)/3 + 1 = ...



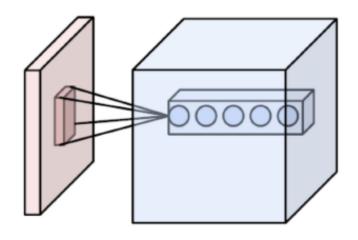
#### Examples time:

Input volume: 32x32x3

Receptive fields: 5x5, stride 1

Number of neurons: 5

Output volume: ?



Examples time:

Input volume: 32x32x3

Receptive fields: 5x5, stride 1

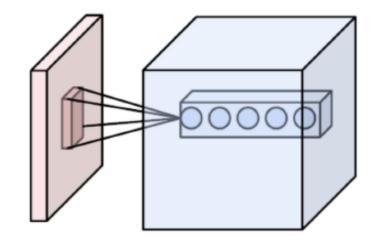
Number of neurons: 5

(N - F) / stride + 1

Output volume: (32 - 5) / 1 + 1 = 28, so: 28x28x5

How many weights for each of the 28x28x5

neurons?



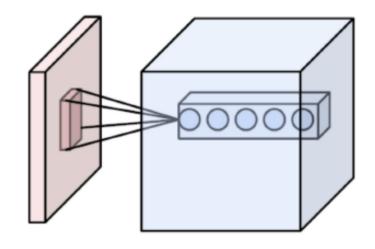
Examples time:

Input volume: 32x32x3

Receptive fields: 5x5, stride 2

Number of neurons: 5

Output volume: ?



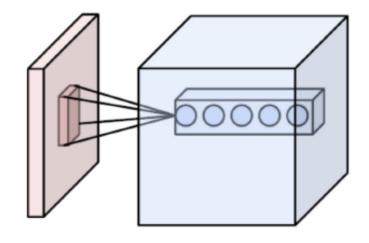
Examples time:

Input volume: 32x32x3

Receptive fields: 5x5, stride 2

Number of neurons: 5

Output volume: ?



Examples time:

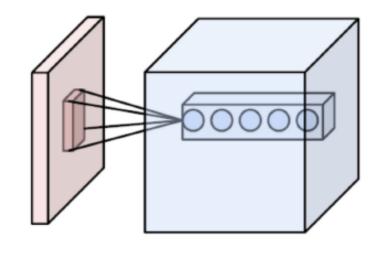
Input volume: 32x32x3

Receptive fields: 5x5, stride 2

Number of neurons: 5

(N - F) / stride + 1

Output volume: ? Cannot: (32-5)/2 + 1 = 14.5



# Example

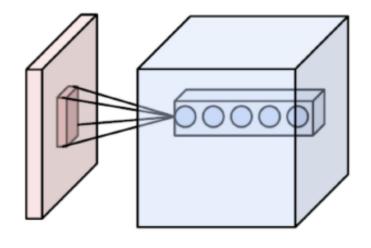
Examples time:

Input volume: 32x32x3

Receptive fields: 5x5, stride 3

Number of neurons: 5

Output volume: ?



Source: Jie Chen slides

# Example

Examples time:

Input volume: 32x32x3

Receptive fields: 5x5, stride 3

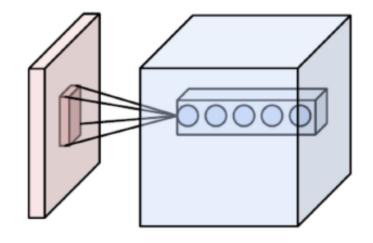
Number of neurons: 5

(N - F) / stride + 1

Output volume: (32 - 5) / 3 + 1 = 10, so: 10x10x5

How many weights for each of the 10x10x5

neurons?



Source: Jie Chen slides

# Example

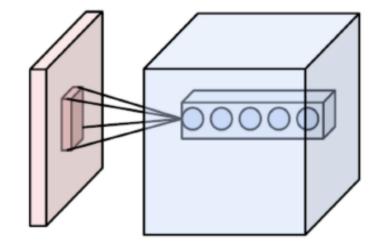
Examples time:

Input volume: 32x32x3

Receptive fields: 5x5, stride 3

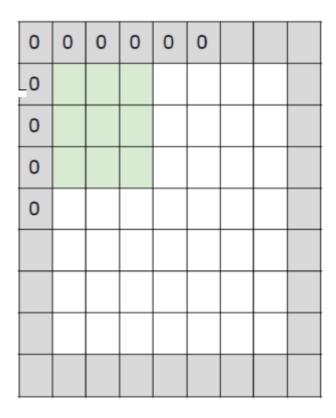
Number of neurons: 5

Output volume: (32 - 5) / 3 + 1 = 10, so: 10x10x5



# In practice: Common to apply zero padding

 Padding zero in the border of images (for each channels/ feature maps)



e.g. input 7x7
neuron with receptive field 3x3, stride 1
pad with 1 pixel border => what is the output?

# Output dimension with padding

The mathematical representation with padding p as follows:

$$n_{out} = \left[ \frac{n_{in} + 2p - k}{s} \right] + 1$$

 $n_{in}$ : number of input features

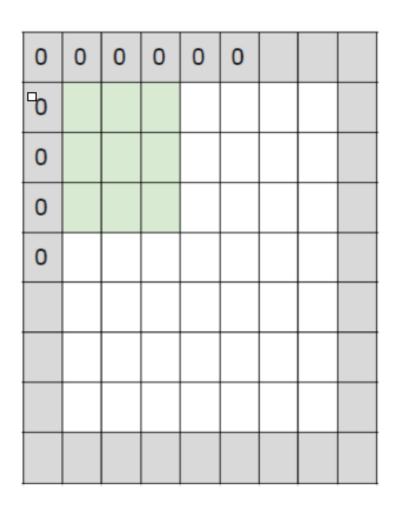
 $n_{out}$ : number of output features

k: convolution kernel size

p: convolution padding size

s: convolution stride size

# In practice: Common to zero padding



e.g. input 7x7
neuron with receptive field 3x3, stride 1
pad with 1 pixel border => what is the output?

(N - F) / stride + 1 = (9-3)/1 + 1 = 7

7x7 => preserved size!
in general, common to see stride 1, size F, and
zero-padding with (F-1)/2.
(Will preserve input size spatially)

# Types of Convolution

#### "Same convolution" (preserves size)

Input [9x9]

3x3 neurons, stride 1, pad **1** =>[9x9] 3x3 neurons, stride 1, pad **1** =>[9x9]

- No headaches when sizing architectures
- Works well

"Valid convolution" (shrinks size)

Input [9x9]

3x3 neurons, stride 1, pad **0** =>[7x7] 3x3 neurons, stride 1, pad **0** =>[5x5]

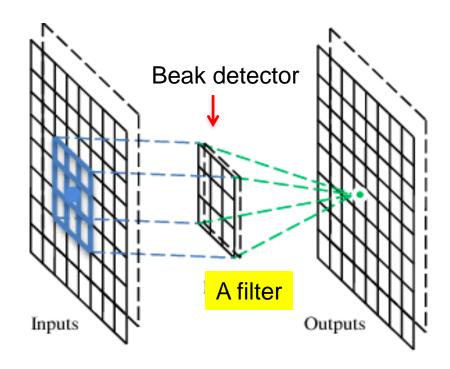


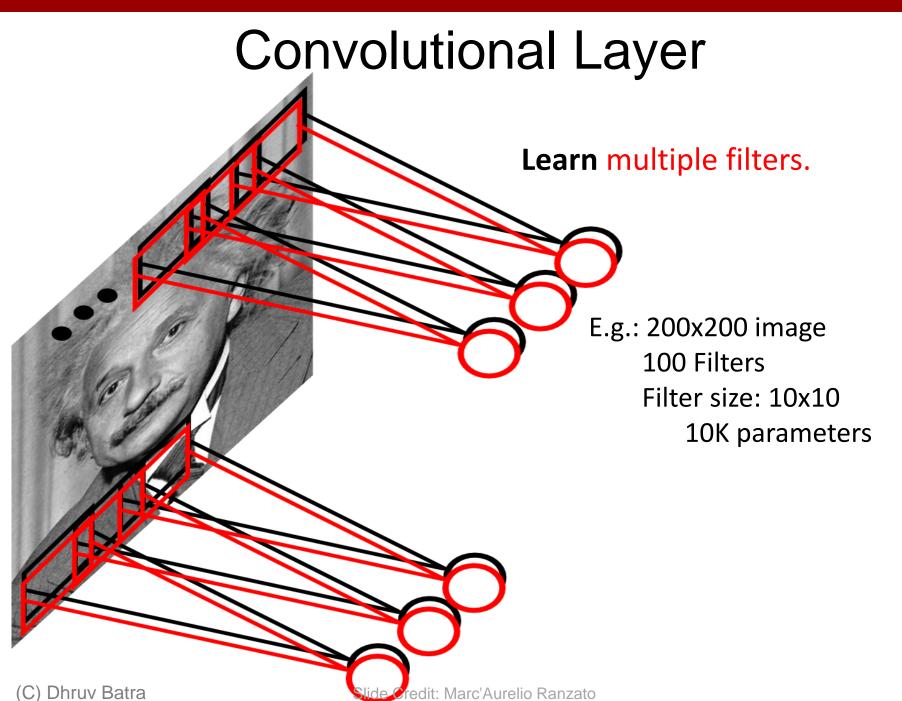
- Headaches with sizing the full architecture
- Works Worse! Border information will "wash away", since those values are only used once in the forward function

Source: Jie Chen slides

# A convolutional layer

A convolutional layer has a number of filters that does convolutional operation.





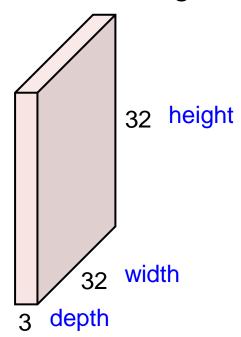
#### Convolution for feature extraction



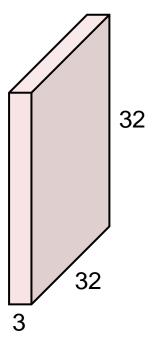


Input Feature Map

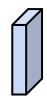
32x32x3 image -> preserve spatial structure



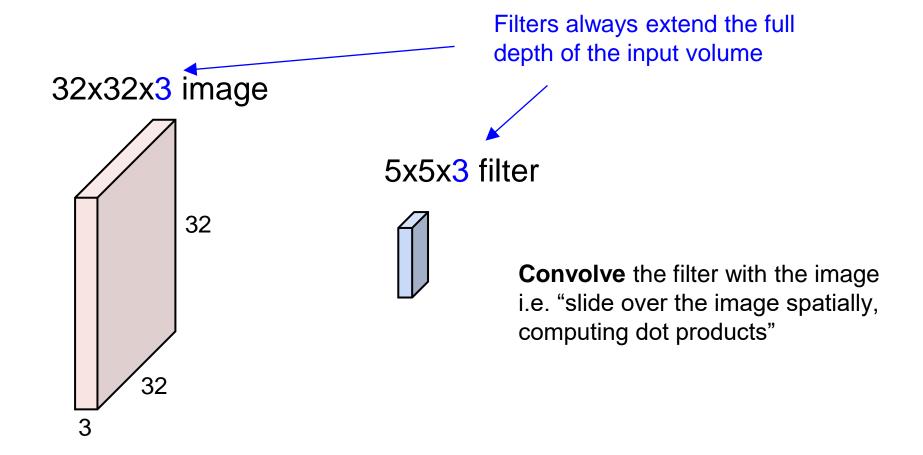
#### 32x32x3 image

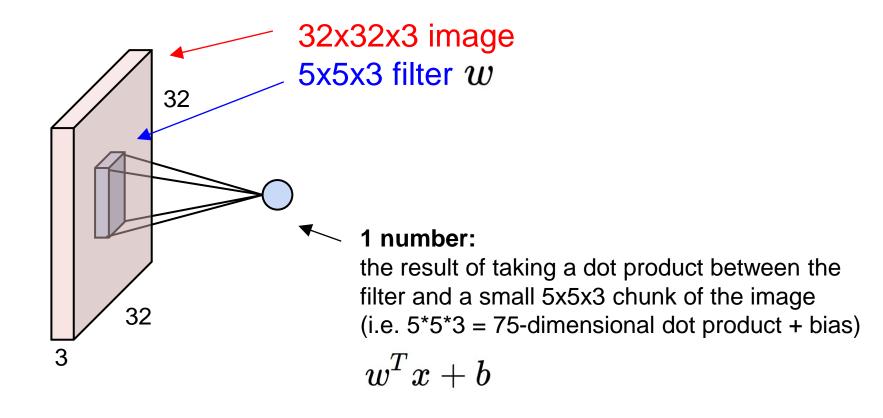


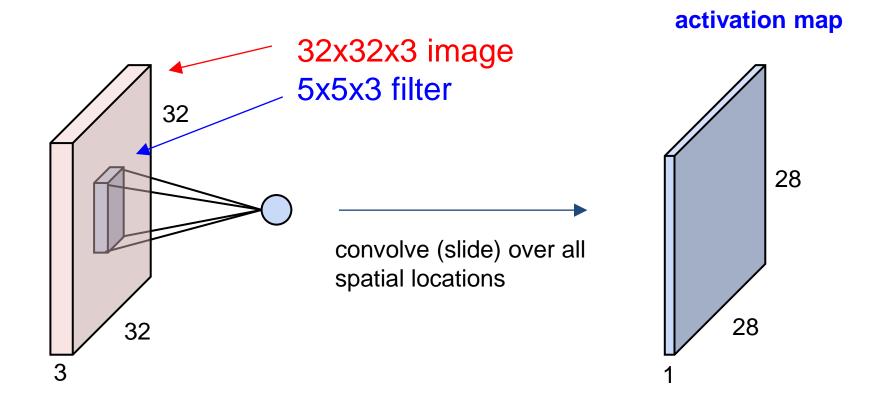
5x5x3 filter



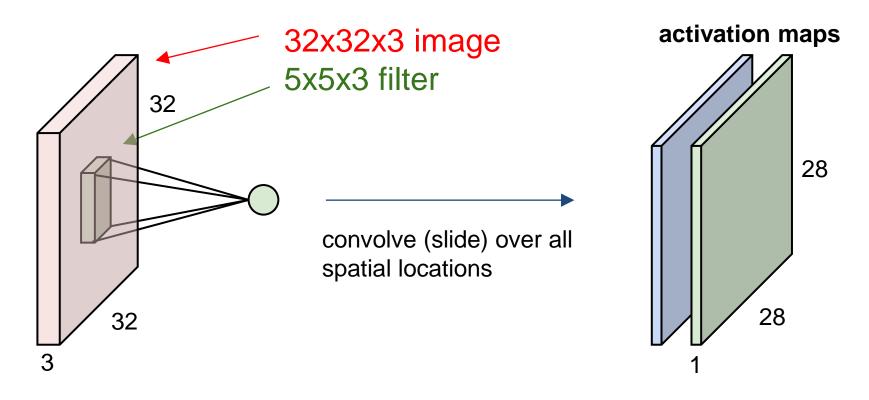
**Convolve** the filter with the image i.e. "slide over the image spatially, computing dot products"



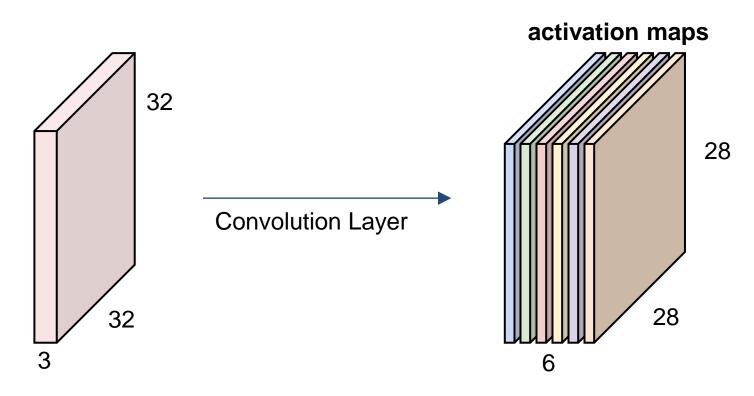




consider a second, green filter

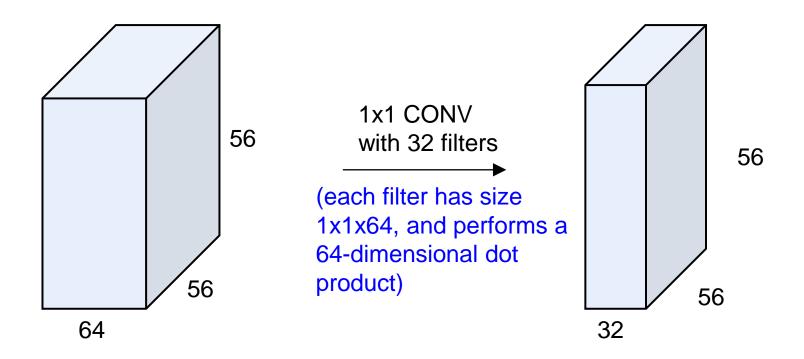


For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:



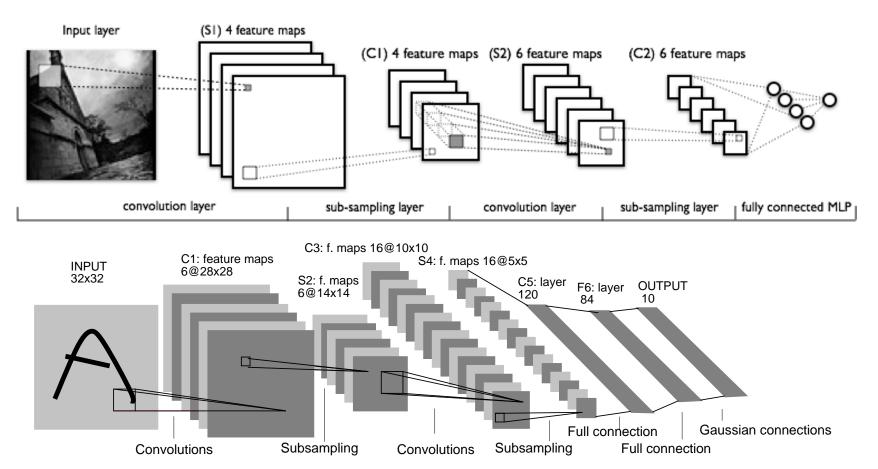
We stack these up to get a "new image" of size 28x28x6!

#### (Between, 1x1 convolution layers make perfect sense)

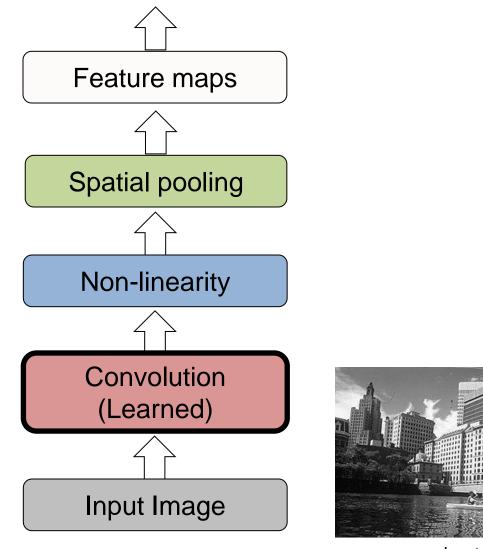


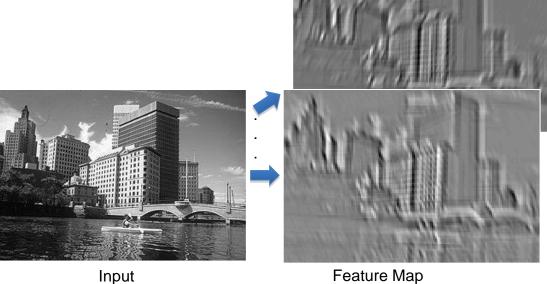
# Convolutional Neural Networks (CNN)

 A CNN is a neural network with some convolutional layers (and some other layers).



# Key operations in a CNN

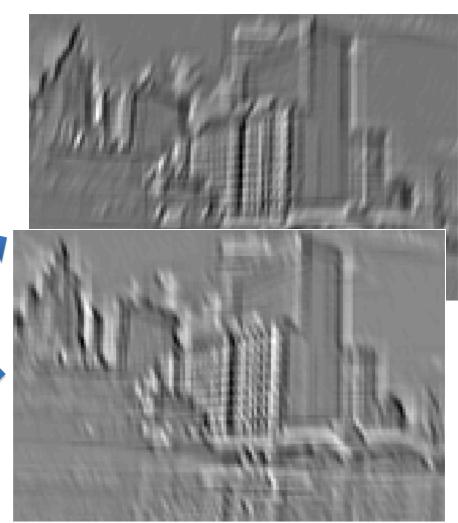




Source: R. Fergus, Y. LeCun

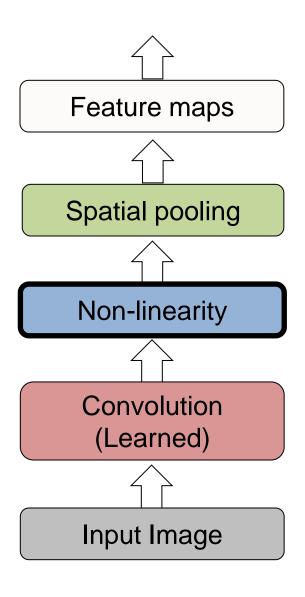
## Convolution as feature extraction



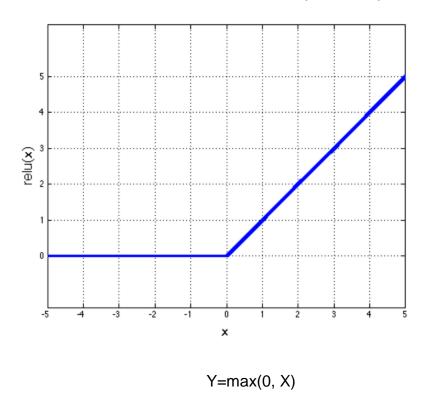


Input Feature Map

# Key operations: Activation function

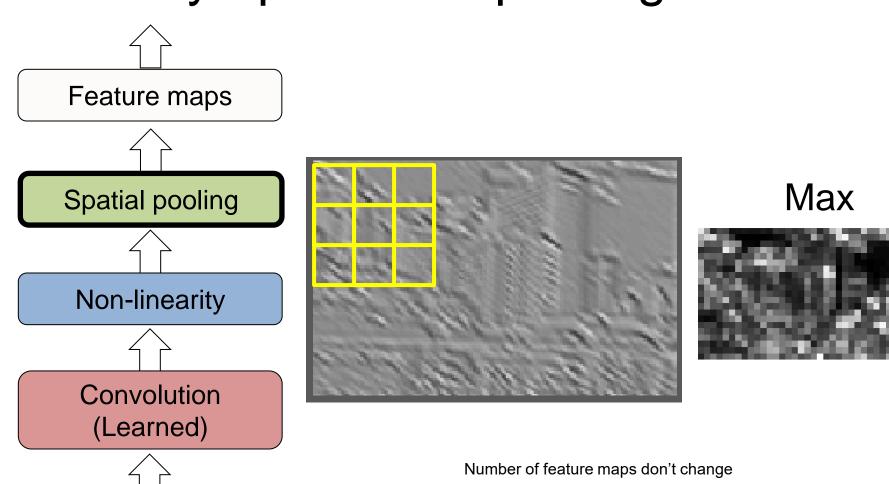


#### Rectified Linear Unit (ReLU)



Source: R. Fergus, Y. LeCun

# Key operation: pooling



Source: R. Fergus, Y. LeCun

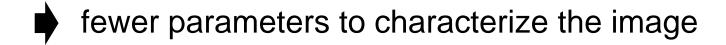
Input Image

## Why Pooling

Subsampling pixels will not change the object bird

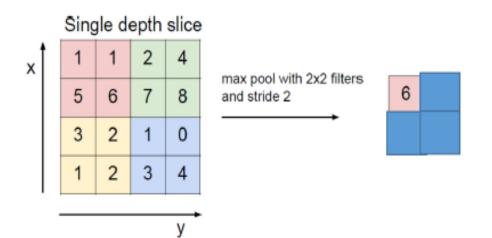


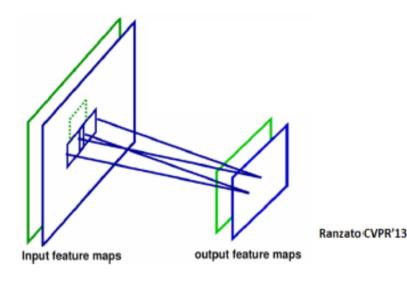
We can subsample the pixels to make image smaller



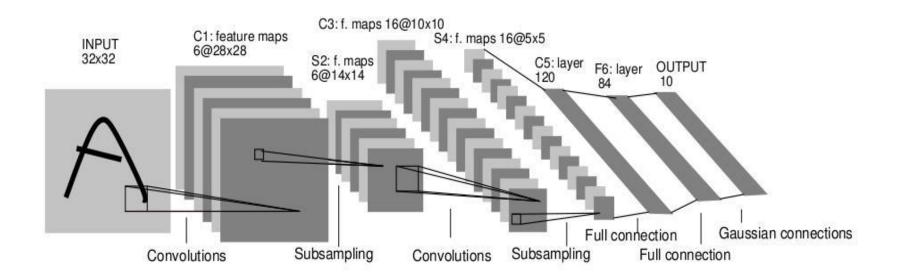
# Key operations: pooling

- Max-pooling
  - · partitions the input image into a set of rectangles, and for each sub-region, outputs the maximum value
  - Non-linear down-sampling
  - The number of output maps is the same as the number of input maps, but the resolution is reduced
  - Reduce the computational complexity for upper layers and provide a form of translation invariance
- Average pooling can also be used
- for pool layers, use pool size 2x2 (more = worse)





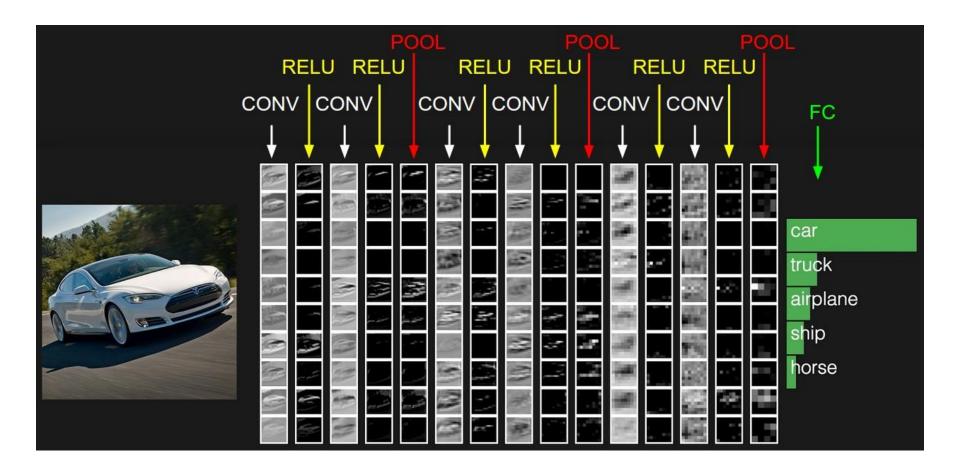
#### LeNet-5



- Average pooling
- Sigmoid or tanh nonlinearity
- Fully connected layers at the end
- Trained on MNIST digit dataset with 60K training examples

Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner, <u>Gradient-based learning applied to document recognition</u>, Proc. IEEE 86(11): 2278–2324, 1998.

#### AlexNet model: feature visualization

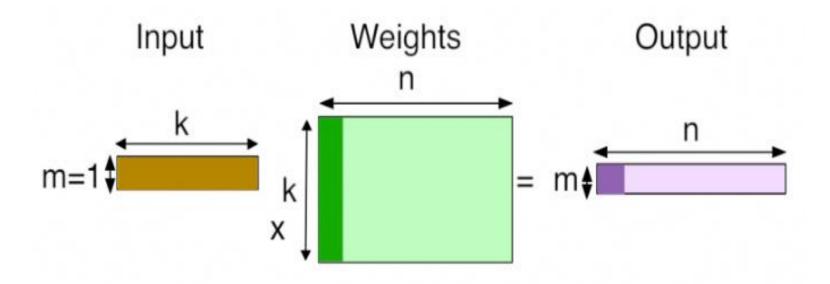


# Back-prop in Convolutional Network

#### Notes

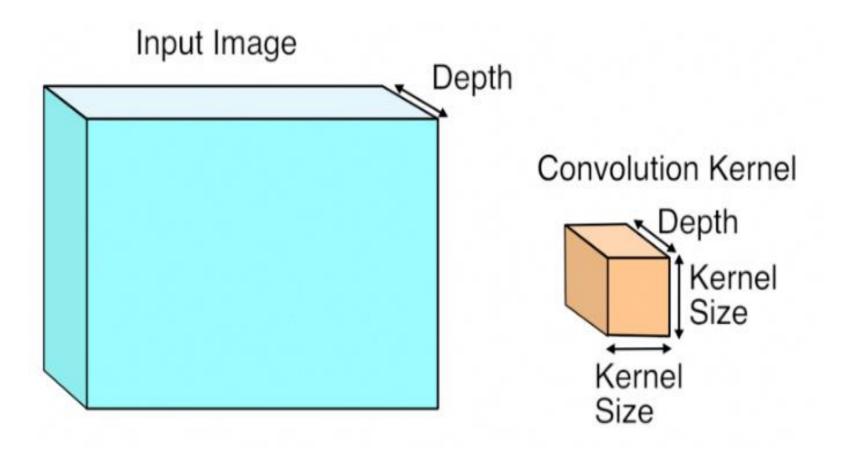
https://www.cc.gatech.edu/classes/AY2018/cs7643\_fall/slide
 s/L6\_cnns\_backprop\_notes.pdf

# FC Layer Implementation

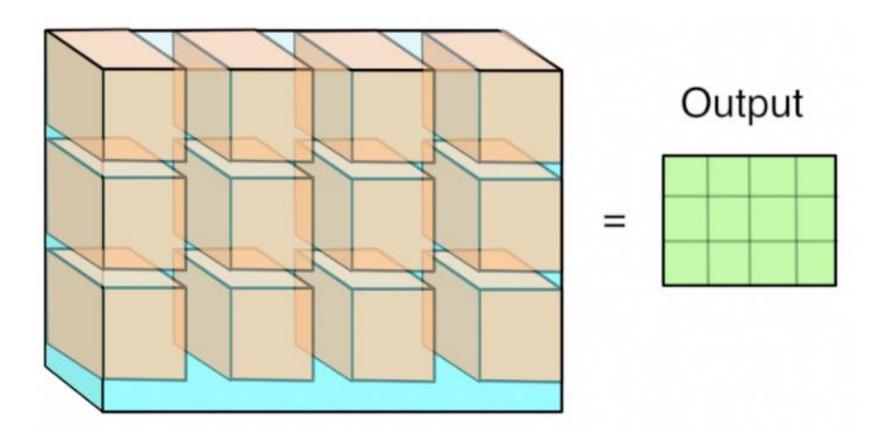


Operations in fully connected layer

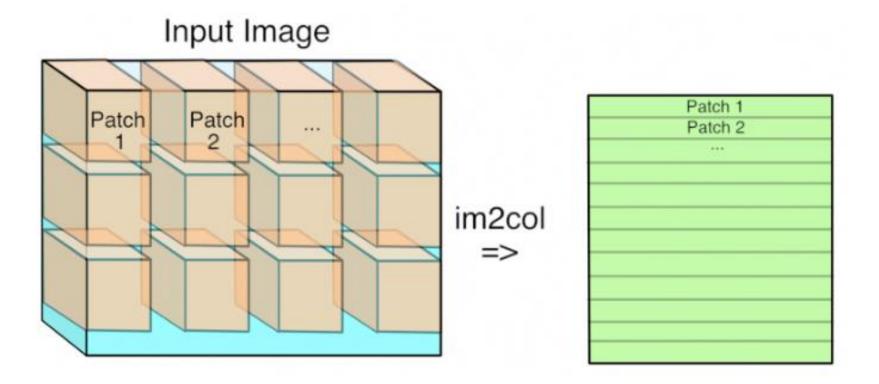
# **CNN** layer Implementation



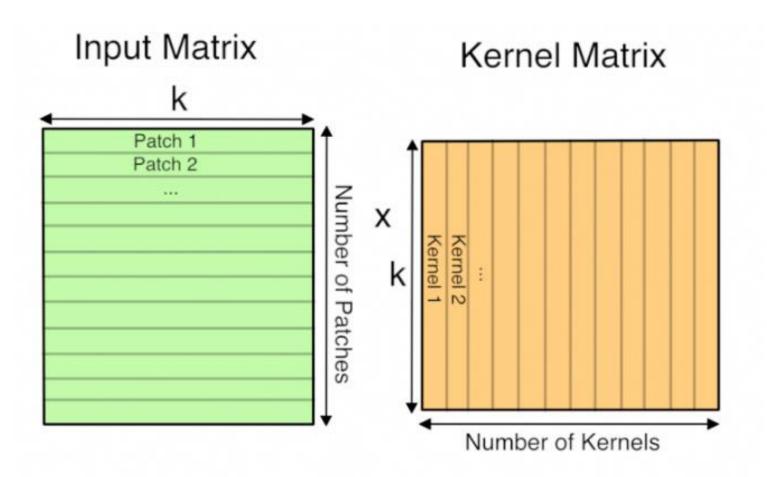
## Im2col



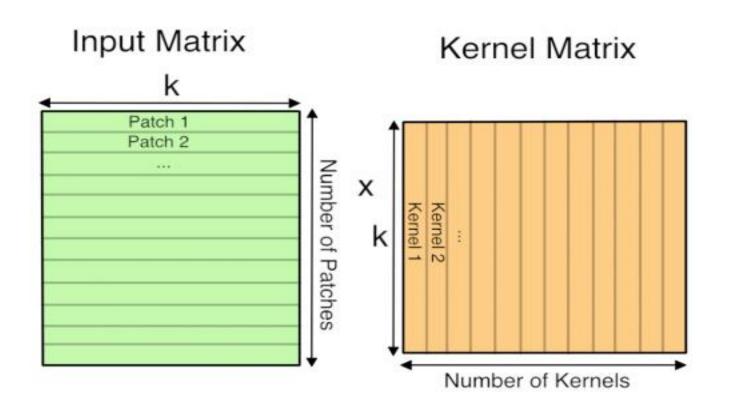
## Im2col



# **CNN** layer Implementation



#### **GEMM-framework**



# Computation parameters

Number of parameters in a CONV layer without bias:

$$(m * n)*k)$$

Number of parameters in a CONV layer with bias:

$$((m * n)+1)*k)$$

added 1 because of the bias term for each filter.

Here:

m: shape of width of the filter

n: shape of height of the filter

k: number of filters

## Summary

- Convolution operations
- Stride size and padding
- Convolutional Neural Networks
- LeNet architecture and time distribution of AlexNet layers
- What's next?
  - Receptive field for convolution
  - CNN Architectures
    - Classification
    - Segmentation and
    - Detection