

Assignment A1

(#02)

Date 18/4/2025

Q2)

Step 1: Population Initialization

$$C_1 = [1, 3, 1, 2, 3, 2, 1]$$

$$C_2 = [3, 2, 2, 1, 1, 3, 2]$$

$$C_3 = [3, 3, 2, 2, 1, 1, 3]$$

$$C_4 = [1, 1, 2, 3, 1, 2, 2]$$

$$C_5 = [1, 3, 3, 1, 1, 1, 2]$$

$$C_6 = [2, 2, 3, 2, 1, 1, 3]$$

Step 2: Evaluate fitness

| Chromosome | Task1 | Task2 | Task3 | Task4 | Task5 | Task6 | Task7 | F ₁ | F ₂ | F ₃ |
|----------------|-------|-------|-------|-------|-------|-------|-------|----------------|----------------|----------------|
| C ₁ | 50 | 128 | 32 | 70 | 72 | 24 | 99 | 5+8+16=18 | 4+3=7 | 8+6=14 |
| C ₂ | 45 | 112 | 36 | 84 | 84 | 30 | 108 | 7+6+3=16 | 8+4=12 | 5+3=8 |
| C ₃ | 45 | 128 | 36 | 70 | 84 | 27 | 117 | 6+3+9=18 | 4+7=11 | 5+8+9=22 |
| C ₄ | 50 | 120 | 36 | 91 | 84 | 24 | 108 | 5+8+16=19 | 4+3=7 | 7 |
| C ₅ | 50 | 128 | 28 | 84 | 84 | 27 | 108 | 5+7+8=20 | 9 | 8+4=12 |
| C ₆ | 60 | 112 | 28 | 70 | 84 | 27 | 117 | 6+3+9=18 | 5+7=12 | 4+9=13 |

Fitness:

$$C_1 = 50 + 128 + 32 + 70 + 72 + 24 + 99 \Rightarrow 475$$

$$C_2 = 45 + 112 + 36 + 84 + 84 + 30 + 108 \Rightarrow 499$$

$$C_3 = 45 + 128 + 36 + 70 + 84 + 27 + 117 \Rightarrow 507$$

$$C_4 = 50 + 120 + 36 + 91 + 84 + 24 + 108 \Rightarrow 513$$

$$C_5 = 50 + 128 + 28 + 84 + 84 + 27 + 108 \Rightarrow 509$$

$$C_6 = 60 + 112 + 28 + 70 + 84 + 27 + 117 \Rightarrow 498$$

Step 3: Roulette wheel selection:

| | Inverse | Probability |
|----------------|----------------------------|---|
| C ₁ | $\frac{1}{475} = 0.002105$ | $P(C_1) = \frac{0.002105}{0.012003} = 0.1753$ |
| C ₂ | $\frac{1}{499} = 0.002004$ | $P(C_2) = \frac{0.002004}{0.012003} = 0.1669$ |
| C ₃ | $\frac{1}{507} = 0.001972$ | $P(C_3) = \frac{0.001972}{0.012003} = 0.1643$ |
| C ₄ | $\frac{1}{513} = 0.001949$ | $P(C_4) = \frac{0.001949}{0.012003} = 0.1624$ |
| C ₅ | $\frac{1}{509} = 0.001965$ | $P(C_5) = \frac{0.001965}{0.012003} = 0.1637$ |
| C ₆ | $\frac{1}{498} = 0.002008$ | $P(C_6) = \frac{0.002008}{0.012003} = 0.1673$ |

C₁ & C₆ favoured because of lower costs



Step 4: Crossover (Single Point) $C_6 = [2, 2, 3, 2, 1, 1, 3]$

Pair 1: $C_1 = [1, 3, 1, 2, 3, 2, 1]$, Pair 2: $C_1 = [1, 3, 1, 2, 3, 2, 1]$, $C_2 = [3, 2, 2, 1, 1, 3, 2]$

Pair 3: $C_3 = [3, 2, 2, 1, 1, 3, 2]$, $C_6 = [2, 2, 3, 2, 1, 1, 3]$

Crossover at '3':

Crossover at '2':

Crossover at '4':

$O_1 = [1, 3, 1, 2, 1, 1, 3]$

$O_2 = [1, 3, 2, 1, 1, 3, 2]$

$O_3 = [3, 2, 2, 1, 1, 1, 3]$

$O_4 = [2, 2, 3, 2, 3, 2, 1]$

$O_5 = [3, 2, 1, 2, 3, 2, 1]$

$O_6 = [2, 2, 3, 2, 1, 3, 2]$

Step 5: Mutation (20% chance)

$O_1 = [1, 3, 1, 2, 1, 1, 3] \rightarrow$ swapping position 1 & 5 $\Rightarrow [1, 1, 1, 2, 1, 3, 3]$

$O_2 = [2, 2, 3, 2, 3, 2, 1]$

$O_3 = [1, 3, 2, 1, 1, 3, 2]$

$O_4 = [3, 2, 1, 2, 3, 2, 1] \rightarrow$ swapping position 4 & 5 $\Rightarrow [3, 2, 1, 2, 2, 3, 1]$

$O_5 = [3, 2, 2, 1, 1, 1, 3]$

$O_6 = [2, 2, 3, 2, 1, 3, 2]$

Step 6: Fitness of new population.

| Offspring | Task 1 | Task 2 | Task 3 | Task 4 | Task 5 | Task 6 | Task 7 | F ₁ | F ₂ | F ₃ |
|-----------|--------|--------|--------|--------|--------|--------|--------|----------------|----------------|----------------|
| O_1 | 50 | 120 | 32 | 70 | 84 | 30 | 117 | 23 | 7 | 12 |
| O_2 | 60 | 112 | 28 | 70 | 72 | 24 | 99 | 9 | 23 | 10 |
| O_3 | 50 | 128 | 36 | 84 | 84 | 30 | 108 | 18 | 13 | 11 |
| O_4 | 45 | 112 | 32 | 70 | 78 | 30 | 99 | 13 | 21 | 8 |
| O_5 | 45 | 112 | 36 | 84 | 84 | 27 | 117 | 16 | 12 | 14 |
| O_6 | 60 | 112 | 28 | 70 | 84 | 30 | 108 | 6 | 29 | 7 |

Fitness:

$$O_1 = 50 + 120 + 32 + 70 + 84 + 30 + 117 = 503$$

$$O_2 = 60 + 112 + 28 + 70 + 72 + 24 + 99 = 465$$

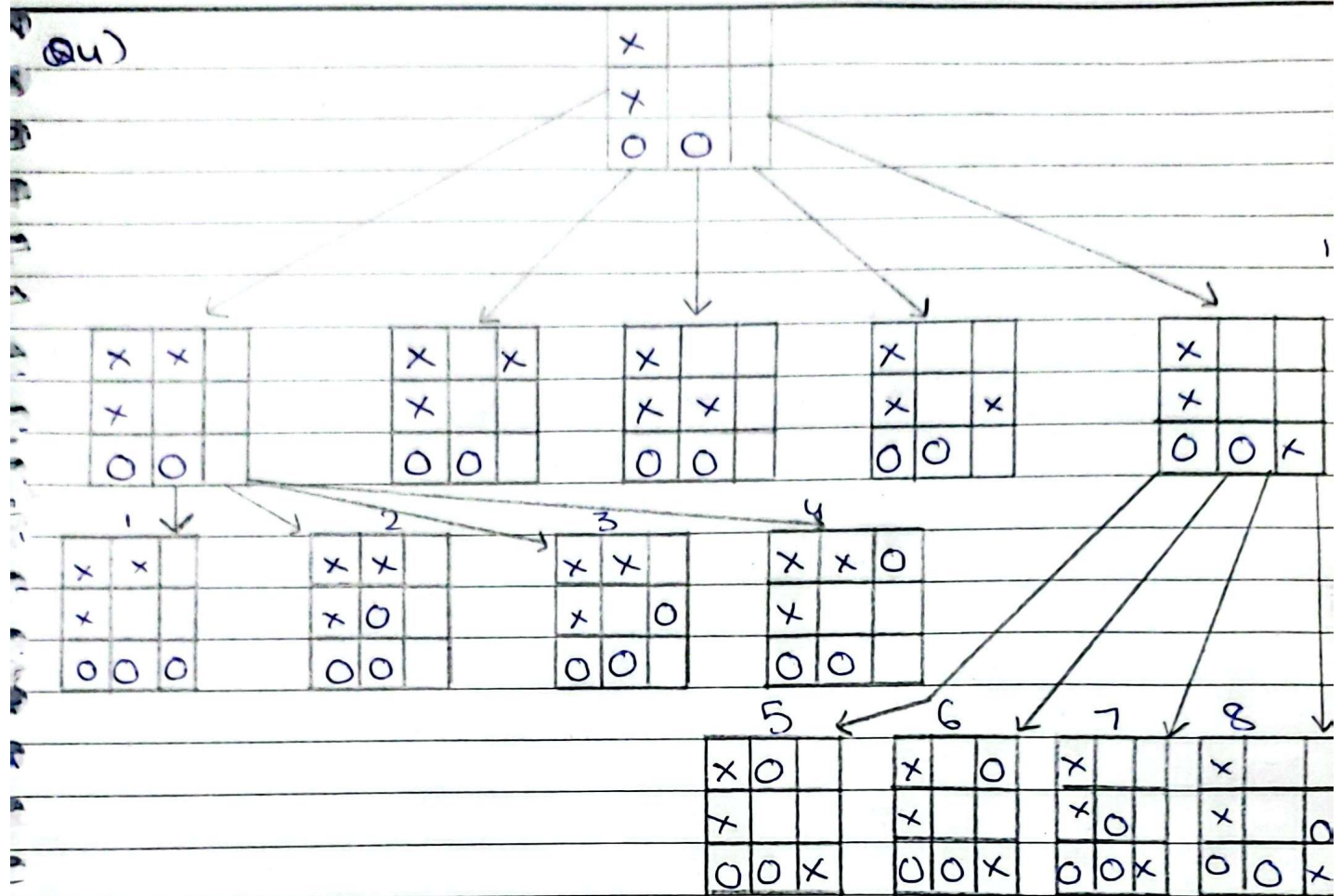
$$O_3 = 50 + 128 + 36 + 84 + 84 + 30 + 108 = 520$$

$$O_4 = 45 + 112 + 32 + 70 + 78 + 30 + 99 = 466$$

$$O_5 = 45 + 112 + 36 + 84 + 84 + 27 + 117 = 505$$

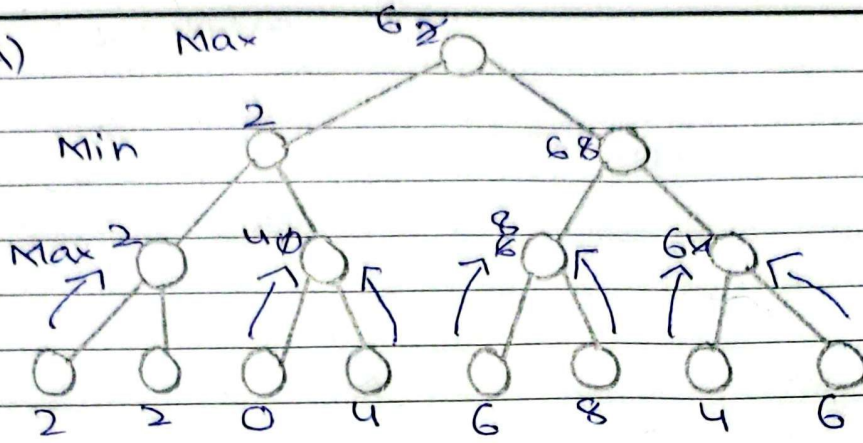
$$O_6 = 60 + 112 + 28 + 70 + 84 + 30 + 108 = 492$$

Q4)



| States | R_1 | R_2 | R_3 | C_1 | C_2 | C_3 | D_1 | D_2 | Sum R | Sum C | Sum D | V-Sum(R,C,D) |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------------|
| 1 | 100 | 10 | -100 | 0 | 0 | -10 | 0 | -10 | -90 | -10 | -10 | -910 |
| 2 | 100 | 0 | -100 | 0 | 0 | 0 | 0 | -100 | 0 | 0 | -100 | -100 |
| 3 | 100 | 0 | -100 | 0 | 0 | -10 | 10 | -10 | 0 | -10 | 0 | -10 |
| 4 | 0 | 10 | -100 | 0 | 0 | -10 | 10 | -100 | -90 | -10 | -90 | -190 |
| 5 | 0 | 10 | 0 | 0 | -100 | 10 | 100 | -10 | 10 | -90 | 90 | +10 |
| 6 | 0 | 10 | 0 | 0 | -10 | 0 | 100 | -100 | 10 | -10 | 0 | 0 |
| 7 | 10 | 0 | 0 | 0 | -100 | 10 | 0 | -100 | 100 | -90 | -100 | -180 |
| 8 | 10 | 0 | 0 | 0 | -10 | 0 | 100 | -10 | 10 | -10 | 90 | 90 |

Q5) A)



B) Max

