

HW 4

Exercise 1. Find the equation of the tangent plane and normal line to each of the following surfaces at the specific point.

- $xy + yz + zx - 1 = 0$ at $(1, 1, 0)$.
- $\sin(xy) + \sin(yz) + \sin(xz)$ at $(1, \pi/2, 0)$.
- $x = e^{2y-z}$ at $(1, 1, 2)$.

Exercise 2. (a) A differentiable curve $C(t)$ lies on the surface

$$x^2 + 4y^2 + 9z^2 = 14,$$

and is parametrized so that $C(0) = (1, 1, 1)$. Let

$$f(x, y, z) = x^2 + 4y^2 + 9z^2,$$

and let $h(t) = f(C(t))$. Find $h'(0)$.

(b) Let $g(x, y, z) = x^2 + y^2 + z^2$ and let $k(t) = g(C(t))$. Suppose also that $C'(0) = (4, -1, 0)$. Find $k'(0)$.