

Lab Report

Removing ϵ -Transitions from a Non-Deterministic Finite Automaton

Course: Compiler Design

Programming Language: C

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1. Introduction

This lab aims to implement a C program that removes epsilon (ϵ) transitions from a Non-Deterministic Finite Automaton (NFA). ϵ -transitions allow state changes without consuming input symbols and are commonly produced when building automata from regular expressions. Eliminating ϵ -transitions simplifies the automaton and is a necessary step before determinization.

2. Theoretical Background

An ϵ -NFA is an NFA that allows transitions labeled with ϵ . The ϵ -closure of a state q is defined as the set of all states reachable from q using only ϵ -transitions, including q itself. Computing ϵ -closures is the foundation of removing ϵ -transitions while preserving the language recognized by the automaton.

3. Algorithm Description

The elimination of ϵ -transitions is performed using a structured algorithm divided into five tasks.

Task 1: Reading the NFA

The automaton is read from user input, including the set of states, input symbols, symbol transitions, ϵ -transitions, the start state, and the set of final states.

Task 2: Computing ϵ -closures

For each state, the ϵ -closure is computed iteratively by exploring ϵ -transitions until no new reachable states are found.

Task 3: Computing New Transitions

For each state q and input symbol a , the new transition $\delta'(q, a)$ is computed as: $\delta'(q, a) = \epsilon\text{-closure}(\delta(\epsilon\text{-closure}(q), a))$. This ensures that ϵ -transitions are completely removed while preserving behavior.

Task 4: Computing New Final States

A state is considered final in the new automaton if its ϵ -closure contains at least one original final state.

Task 5: Displaying the Resulting NFA

The resulting ϵ -free NFA is displayed by listing the states, start state, final states, and all symbol-based transitions.

4. Implementation Details

The program is implemented in C using static arrays for simplicity and clarity. The design follows a modular approach with one function per task. Dynamic memory allocation is avoided to reduce complexity and improve reliability.

5. Illustrative Example

Consider an ϵ -NFA with states $\{0, 1\}$, alphabet $\{a, b\}$, start state 0, and final state $\{1\}$. State 0 has an ϵ -transition to state 1. The ϵ -closure of state 0 is $\{0, 1\}$, while the ϵ -closure of state 1 is $\{1\}$. After eliminating ϵ -transitions, both states become final states and the resulting automaton recognizes the same language.

6. Conclusion

In this lab, ϵ -transitions were successfully eliminated from a Non-Deterministic Finite Automaton. By computing ϵ -closures and reconstructing transitions, an equivalent ϵ -free NFA was obtained. This transformation preserves the recognized language and prepares the automaton for determinization into a DFA.

Appendix: Source Code

The complete C source code implementing the ϵ -transition elimination algorithm is provided separately in the appendix section as required.