#Step 1: Alice generates a symmetric key..... 1
#Step 2: Bob generates a public and private key using RSA.....2
#Step 3: Alice encrypts the symmetric key using Bob's public key.....3
#Step 4: Bob decrypts the symmetric key using his private key.....4
#Step 5: Bob encrypts a message using the symmetric key..... 5
#Step 6: Alice decrypts the message using the symmetric key..... 5

#Step 1: Alice generates a symmetric key

```
#Usage
alice = Alice()
bob = Bob()

#Step 1: Alice generates a symmetric key
alice.generate_symmetric_key()
print("Alice's symmetric key: ", alice.get_symmetric_key())
```

Alice generates a random symmetric key using urandom(16)

```
Alice's symmetric key:  b'=\x82\xb8\xff/\xae\xb1;@6+\x02V\xa6\x18\x03'
```

#Step 2: Bob generates a public and private key using RSA

```python
#Step 2: Bob generates a public and private key using RSA
prime_p = input("Enter the prime number p: ")

if prime_p.strip() == "":
    print("Reading prime number p from file", "\n")
    prime_p = read_prime_from_file("Assignment_1\q1\prime_p.txt")

prime_q = input("Enter the prime number q: ")

if prime_q.strip() == "":
    print("Reading prime number q from file", "\n")
    prime_q = read_prime_from_file("Assignment_1\q1\prime_q.txt")

bob.generate_key_using_rsa(prime_p, prime_q)
print("Bob's public key: (n , e)", bob.get_public_key(), "\n")
print("Bob's private key: (n , d)", bob.get_private_key(), "\n")
```

As the prime numbers are large, i read them from a file if no user input is given.

```python
def generate_key_using_rsa(self,prime_p: int , prime_q: int) -> None:
    n = prime_p * prime_q
    phi = (prime_p - 1) * (prime_q - 1)

    #Taking a prime number e such that 1 < e < phi and gcd(e, phi) = 1
    #Hardcoding to avoid iterating over all numbers between 1 and phi
    e = 65537

    # d is the modular multiplicative inverse of e (modulus phi)
    d = invert(e, phi)

    self.__public_key = (n, e)
    self.__private_key = (n, d)
```

RSA algorithm uses hard coded 'e' to save time.

```
Enter the prime number p:
Reading prime number p from file

Enter the prime number q:
Reading prime number q from file

Bob's public key: (n , e) (20574353463657743640068781547866766744044658403715995320902625671858951276443214567135386073925679567871737657797347913930990840791082006078665603817897171615833065761275593105910165978246552215614687328136765608135725505850823232895009604299343667138575865880858879046921367189097548224208970752295883393031123737001916432573253620485807165755387666066029766872772992604255585209558399515980413484441112632715198308939211851818162483009687925142436510448222322756853094786906138301364469178499086157307275066529589155463602088226626158628544389593116979857319221512933765927495918877468195982503773649562492696948394676882393128765742085975215323172083003984613032540633406615650141352364779853631128037927571819719085847578105536024680843238304679938925906439845195311159588051514170804098292071730238134691091187228809005373679991643696692658087655123251678270772130101192808847972324918019820991902271535466196544072485979340433008873290455835697769664998094970272982702688168180180561140792459572480199885242047628858373493993134209897208892978762536126619180509928639777695682133758564648445335446763681493471484608206060202249045338805950651181527396546843057014413491669703115581788014439644284082486596691100265793416089256292076909836830529806868316439704460756235545574799946159405447297696049180559542508711222025009152218060406513216877270242234588087532989788042962673905532614530516686001458376645251110900338862882617381506461002985349727493539799487017128688722139876676329747753676125693052709864486477022487073521914847790935233249489165577164167711413878733876644742490648523044091168555701670432032036199076517148549507879568974022351928470560843917481377909419931134518463758513631565815039643417349191631217498290592182484512757367608256450046878524041175340384861800570775536816109753615481695711045207280978141345920734622115521387710501545653124092599896810770330202408495173634085435808449059613833066728701556713113124803688885362126712112174302209832915434089223281437695170487515854000305210566838260056646948033047412, mpz(575003216565230682685353011017787966620263306715995804351209991006253797975699098237105347101671951668734832140952781469337974335000775170265406105754924081535008365478315704606330164727655904879989339002629047528287758617519383453171484676361106866823558536636636872753153360108572420056984779716786722007823947729785115299434086291908662954483355669189395321879880222355914144661767728848355848656194568243599975162526978718554426721375794498327797536130272061028343092972167978838332417069340891911068922974989022925937213079402412201842379753482441263107964445826374254019451630758441349890314691118246771466861935695716584391330810583405895973052199326031069735117588906229415823106046833556310340328581841408236381949775024947408037341464026201651184354235348672859483805293427156026040910872607998790759727510457125859045168794260638818182939409856230433506969093692795652622886465963426829558389925452185568306806312766222700139651171077538856446257999462098539681679717546406132654614576025038600090175158070052265663439701111684386029833323126165561404767205621339140596988071320562498193513793575860050383318867434578270974772515366467782748965545962715383351988414924161531134455318265441403509501031520838799437386375598287536580309805802504676985798018795817175199783225691982944128891685856343684201760829904844806737033717135431148528160793353243550227466087839623961397830102492112661397913893562596656117630283018439875406470274785645189606936406486321337337016679087133969365419236008568374560609262020573079881433123185171200466187948769610716321646281286058112247439593667116949676961359643472597890285365143900647126488938975532524807033671676794422696054106311686229778831154363942923530827564482980874497056936289990983925688085574193290617774501283411608358394491636589748443770170440488934264787187544917681358419457949713751024678068570213770775863715876169382402883230978600252742959108102672650578577512172345174361058096203216934449566392912665766056695469362962681400755939465551511872874901373417726604832651840785))
```

#Step 3: Alice encrypts the symmetric key using Bob's public key

```python
class Alice:
    def encrypt_message(self, message: bytes, bob_public_key: Tuple[int, int]) -> int:
        message_int = int.from_bytes(message, byteorder='big')
        n, e = bob_public_key

        #Encrypting the message using RSA
        cipher_text = powmod(message_int, e, n)
        return cipher_text
```

```
Alice's symmetric key:  b'=\x82\xb8\xff/\xae\xb1;@6+\x02V\xa6\x18\x03'

c: Cipher text from Alice (encrypted symmetric key)-:  10301554822930007488825509906089675532814582900806528702308323259504418575269843882192247041
43124515707425559346406533421854126287046649485598658672001764951384698472344979841496331525014143990668449111135763768399265125288941085427459447584691511035678849704766039035673367625606268400254007121758307050521056432544975303498304881108416577658187348947969655729542539353362565394176363298729500793782662023983209536883979291416786559252934448497404301667094902667464840409202133290246880947307524448351448904921986819571173241506084859395424556227171886593866204399249113041275819284302017171460719898586264902363441018123186024077159123422806975099156516652361090844823973846859707614887635874423174994170742708514141308343007785857830206599277042011027148816859906853778717465904070510663867326749371671091286812493158257284941916573272650007396242698292312735440070397307378149533124571932160331024942083436736254195174038123293768508548973656520332397207268588035861503642685275966899269308420864621648607254851955362598119454823883849144309087927242762290365431947569886114728853894063875712701768957984629535001749365630145007974334680720220423247426146978897109859704038028568408795108580594949546749424071323003963233699487263121589334619878486652097357674821315363855456110863474796690584636097045743839060707992630758511512781337556178756559241682833049206809888653681705085966680748058820958372003735598763893513196059051137879588246612970193685041514959004438430763835282216179247965687015160173896058702488891559678103598341688890888779998469361986881482927089606612572651692177717242620609679607332426149105654667384224121285987207436303618983525722878392964191219025270219314403343585796149122107741035294539066024091643643851307620550400256177965942767909206931385797298766961099515775635230404274752971335058170731839901402905578561087107516666018441035208608005442789015855962874813330928711919659280418103016878946628541033622967656679819014809505284054776889566444382569841304487435
```

#Step 4: Bob decrypts the symmetric key using his private key

```python
class Bob:
    def decrypt_alice_symmetric_key(self, cypher_text: int) -> bytes:

        #Decrypting the message using RSA
        message_int = powmod(cypher_text, d, n)

        #convert the integer to bytes as the original symmetric key was in bytes
        byte_length = (message_int.bit_length() + 7) // 8
        message = message_int.to_bytes(byte_length, byteorder='big')

        self.__alice_symmetric_key = message
        return self.__alice_symmetric_key
```

```
Symmetric key decrypted by Bob:  b'=\x82\xb8\xff/\xae\xb1;@6+\x02V\xa6\x18\x03'
```

#Step 5: Bob encrypts a message using the symmetric key

```python
class Bob:

    def encrypt_using_symmetric_key(self, message: Optional[bytes] = None) -> bytes:
        if message is None:
            print("Message is not provided so generating a random message")
            message = urandom(16)
            print("Generated message: ", message, "\n")

        cipher = Salsa20.new(key=self.__alice_symmetric_key)
        cipher_text = cipher.nonce + cipher.encrypt(message)

        return cipher_text
```

```
Enter the message to be encrypted:
Message is not provided so generating a random message
Generated message:  b'S\xf2d2\x93ZPNvdx\xb6\x8d\x89\x01\x88'

Cipher text from Bob (encrypted message):  b'B_\x9dK\xc5 \xd2\x9a\x0c~\xb2A\xed\xfa\xe2 \x95\x9e|$\xc1ge\xcd'
```

#Step 6: Alice decrypts the message using the symmetric key

```python
class Alice:
    def decrypt_salsa20_cipher(self, cipher_text: bytes) -> bytes:
        print("Received Cipher text: ", cipher_text)

        nonce = cipher_text[:8]
        cipher = Salsa20.new(key=self.__symmetric_key, nonce=nonce)
        message = cipher.decrypt(cipher_text[8:])
        return message
```

Decrypts using Salsa20

```
Received Cipher text:  b'B_\x9dK\xc5 \xd2\x9a\x0c~\xb2A\xed\xfa\xe2 \x95\x9e|$\xc1ge\xcd'
Decrypted message Alice:  b'S\xf2d2\x93ZPNvdx\xb6\x8d\x89\x01\x88'
```