

## 3.3.3

## Karnaugh Maps.

3 Inputs.

	AB			
	00	01	11	10
C 0		1		
C 1		1		

	AB			
	00	01	11	10
C 0				
C 1		1	1	

	AB			
	00	01	11	10
C 0				1
C 1	1			

	AB			
	00	01	11	10
C 0	1			1
C 1	1			1

	AB			
	00	01	11	10
C 0		1	1	
C 1		1	1	

	AB			
	00	01	11	10
C 0	1			
C 1				1

	AB			
	00	01	11	10
C 0			1	1
C 1			1	1

	AB			
	00	01	11	10
C 0	1			
C 1				1

	AB			
	00	01	11	10
C 0	1	1		
C 1	1	1		

	AB			
	00	01	11	10
C 0	1	1		1
C 1	1	1		1

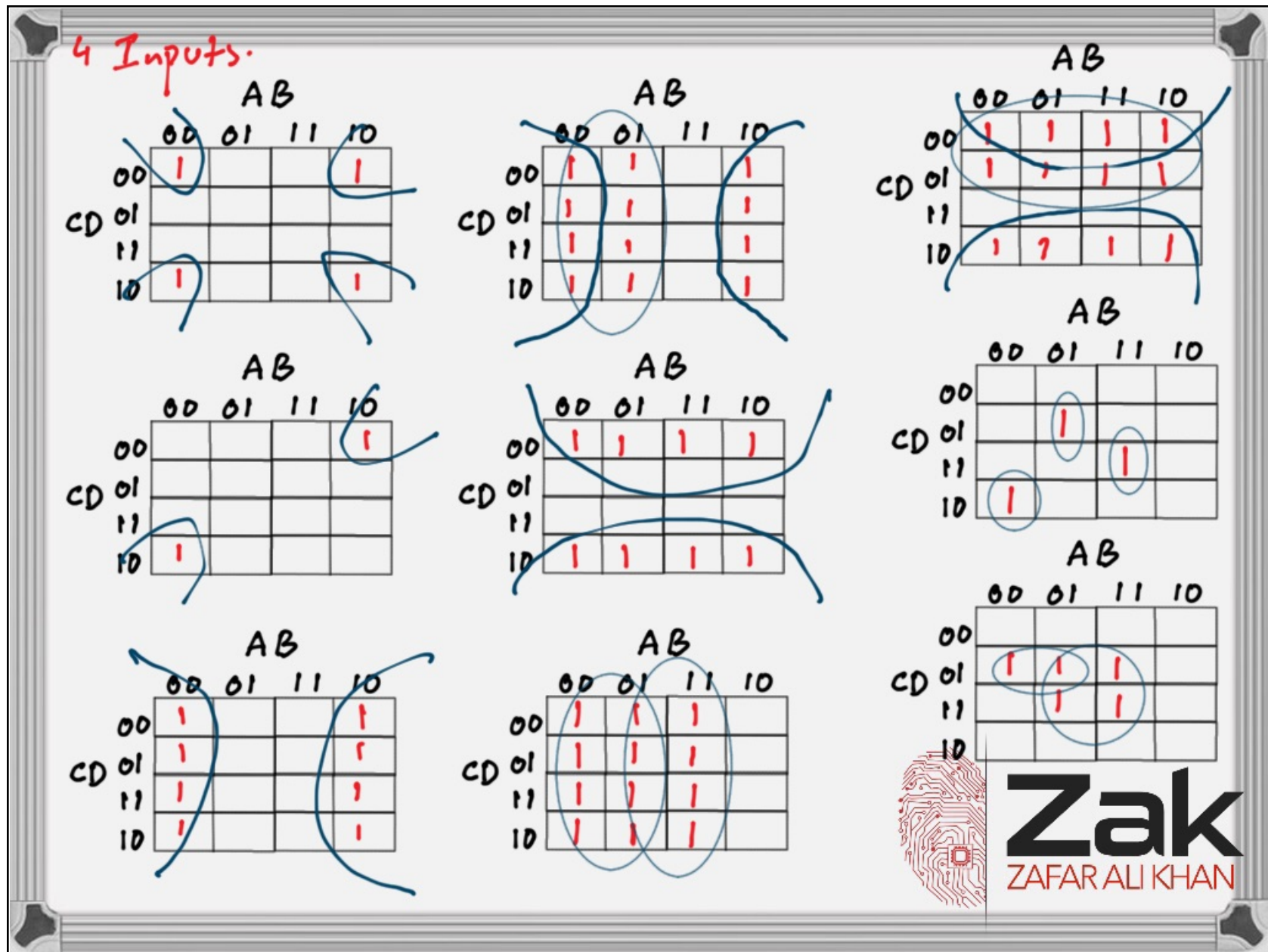
	AB			
	00	01	11	10
C 0	1	1	1	1
C 1				

	AB			
	00	01	11	10
C 0			1	1
C 1	1	1		

	AB			
	00	01	11	10
C 0	1	1	1	
C 1	1	1	1	



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INPUT				OUTPUT	
P	Q	$\bar{Q}$	R	$P\bar{Q}$	$PR$ Z
0	0	1	0	0	0
0	0	1	1	0	0
0	1	0	0	0	0
0	1	0	1	0	0
1	0	1	0	1	1
1	0	1	1	1	1
1	1	0	0	0	0
1	1	0	1	0	1

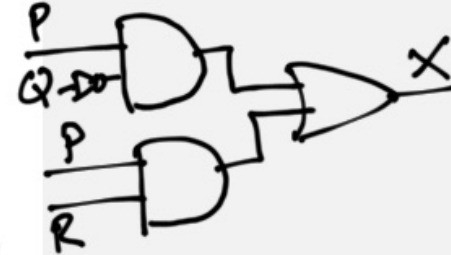
Sum of products

$$Z = P\bar{Q}\bar{R} + P\bar{Q}R + PQR$$

1 0 0    1 0 1    1 1 1

$$Z = P\bar{Q} + PR \quad \text{Ans.}$$

✓  $P\bar{Q}\bar{R}$   
✓  $P\bar{Q}R$   
✓  $PQR$



ii) For the truth table above complete the Karnaugh Map (K-map).

		PQ			
		00	01	11	10
R	0				1 ✓
	1			1 ✓	1 ✓

~~$P\bar{Q}\bar{R}$~~   
 ~~$P\bar{Q}R$~~   
 $P\bar{Q}$

~~$P\bar{Q}\bar{R}$~~   
 ~~$P\bar{Q}R$~~   
 $PR$

Loops

32 16 8 4 2 1



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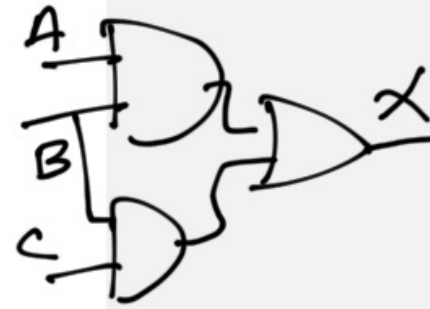
5 (a) (i)

INPUT				OUTPUT	
A	B	AB	C	BC	X
0	0	0	0	0	0 ✓
0	0	0	1	0	0 ✓
0	1	0	0	0	0 ✓
0	1	0	1	1	✓ 1 ✗
1	0	0	0	0	✓ 0
1	0	0	1	0	✓ 0
1	1	1	0	0	✓ 1 ✗
1	1	1	1	1	✓ 1 ✗

$$X = \bar{A}BC + AB\bar{C} + ABC$$

Sum of 7 products.

$$X = AB + BC$$



(ii) For the truth table above complete the Karnaugh Map (K-map).

		AB			
		00	01	11	10
C	0			1 ✓	
	1		1	1 ✓	

$$\frac{AB\bar{C} + ABC}{AB}$$

$$\frac{ABC + \bar{A}BC}{BC}$$



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(b) The truth table for a logic circuit with four inputs is given below:

INPUT				OUTPUT
P	Q	R	S	Z
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

$$X = QS + P'QR$$

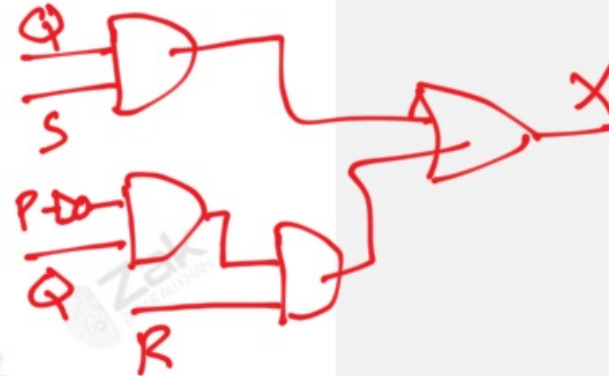
$$\bar{P}Q\bar{R}S \quad 0101 \checkmark$$

$$\bar{P}QRS \quad 0111 \checkmark$$

$$P\bar{Q}\bar{R}S \quad 0110 \checkmark$$

$$PQ\bar{R}S \quad 1101 \checkmark$$

$$PQRS \quad 1111$$



(i) Complete the K-map corresponding to the truth table above.

		PQ			
		00	01	11	10
RS	00				
	01		1	1	
	11		1	1	
	10		1		

$$\begin{array}{l} \bar{P}Q\bar{R}S \\ \bar{P}QRS \\ P\bar{Q}\bar{R}S \\ PQ\bar{R}S \\ \hline QS \end{array}$$

$$\begin{array}{l} \bar{P}QR\bar{S} \\ \bar{P}QRS \\ \hline \bar{P}QR \end{array}$$

(ii) Draw loop(s) around appropriate groups of 1's to produce an optimal sum-of-products. [2]

(iii) Using your answer to part (b)(ii), write the simplified sum-of-products Boolean function. [2]



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