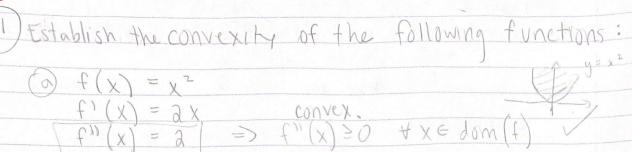
ANLY580 - Assignment 1

Excellent!

as intr

10/10



(b)
$$f(x) = \ln(x)$$

 $f'(x) = \frac{1}{x}$
 $f''(x) = -\frac{1}{x^2} = f''(x) < 0$... Neither
convex or concave but over a

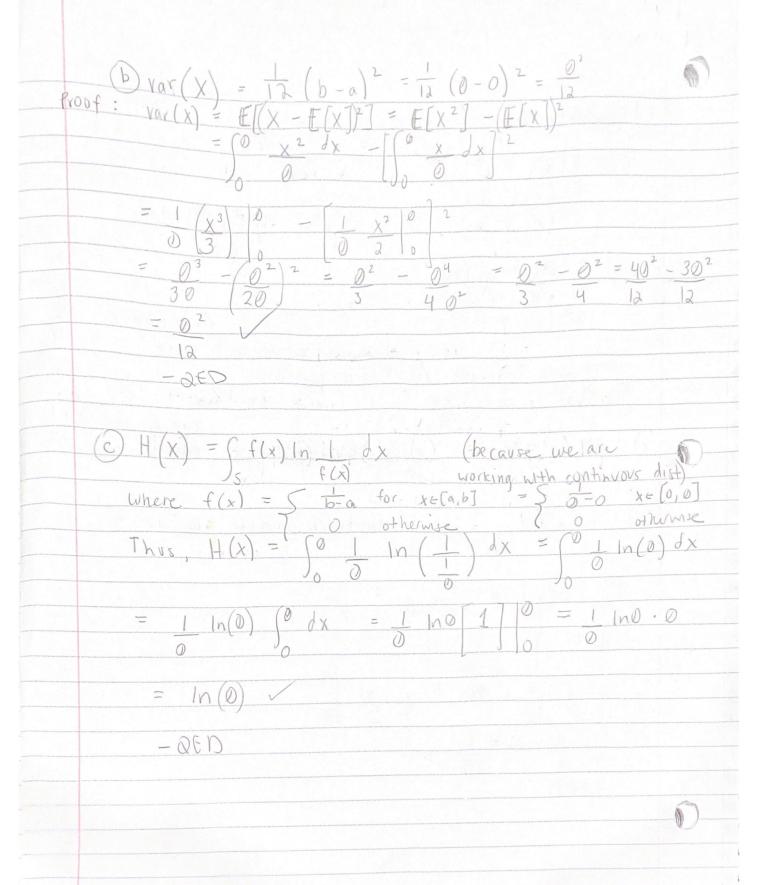
"finte interval
$$(0, \alpha)$$
 is concave.
C) $f(x) = 1/(1+e^{-x})$ $y = 1$

10/10

a)
$$E_{\chi}[\chi] = \frac{1}{2(a+b)} = \frac{1}{20}$$

$$=\frac{10^{2}-0}{2}$$

you meant theta/2 surely!



40/40 | X ~ Uni(0,0) We know f(x|0) = 1 for x = (0,0] Let's first look at the likelihood function, ((0), We have M independent samples, 50 $\mathcal{L}(0) = \frac{M}{\prod_{i=1}^{m}} f(X_i, 0) = \frac{1}{DM} \text{ for } X_1, \dots, X_M \in [0, 0]$ We can then say from the above statement that: ((0) = 0 if 0 < max (X1, ..., XM) $\mathcal{L}(0) = 1$ if $0 = \max(X_1, \dots, X_H)$ Since the likelihood function is decreasing, we see that $\hat{O} = \max(X_1, ..., X_M)$. H) Monty Hall Problem:

[Bayes' Theorem] . P(H) = probability your choice is \$1 MIL

. P(B) = prob has crickets behind it

P(A|B) = P(B|A) P(A) = P(crickets | million) P(million)

. P(B|A) P(A) = P(crickets | million) P(million) 20/20 p (B) P(crickets million) P(million) +P(crickets | ~ million) · P(MILLION) P(crickets | MILLION) = 1 P (MILLION) = 1/3 P(crickets ~ MILLION) = 1 P(2MILLION) = 1-P(MILLION) = 2/3 Probability your first choice is \$1 MILLION GIVEN the door shown has chickents behind is 1/3. Thus you should switch because that probability is 1-12(AIB) = 2/3. There is a 2/3 chance the switched door has \$1 MIL given crickets shown.

XERN 20/20 $= E_{X} \left[\left(X - E_{X} \left[X \right] \right) \left(X - E_{X} \left[X \right] \right) \right]$ M positive semi-definite iff XTMX = 0 + X EIR" For any random vector we can write $x = x \cdot E_x [(x - E_x [x])(x - E_x [x])^T] \cdot x$ $= \mathbb{E}_{x} \left[\left(x^{\top} \cdot \left[x - \mathbb{E}_{x} \left[x \right] \right] \left[x - \mathbb{E}_{x} \left[x \right] \right]^{\top} x \right]$ $= \mathbb{E}_{x} \left[\left(x - \mathbb{E}_{x} \left[x \right] \right) \left(\left[x - \mathbb{E}_{x} \left[x \right] \right] x \right) \right]$ $= \mathbb{E}_{x} \left[\left(x - \mathbb{E}_{x} \left[x \right] \right) \mathbb{E}_{x} \left[x \right] \right]^{2}$ Thus the square of any real numbers in X of size TEX = 252 = 0 ... & is positive semi-definite by proving the given above statement - QED