



**SV: What if  $X$  is not separable w.r.t.  $y$ ? What about noise?**



We can introduce slack variables,  $\xi_i$  :

$$\min_{\mathbf{w}, b} \|\mathbf{w}\|_2^2 + c \sum_{i=1}^M \xi_i$$

$$\text{s.t.} \quad \forall i \quad y_i(\mathbf{w}^T \mathbf{x}_i + b) \geq 1 - \xi_i$$

$$\text{where} \quad \xi_i = \begin{cases} 1 - y_i(\mathbf{w}^T \mathbf{x}_i + b) & \text{if } y_i(\mathbf{w}^T \mathbf{x}_i + b) < 1 \\ 0 & \text{if } y_i(\mathbf{w}^T \mathbf{x}_i + b) \geq 1 \end{cases}$$

which can be reduced to:

$$\begin{aligned} \min_{\mathbf{w}, b} \quad & \|\mathbf{w}\|_2^2 + c \sum_{i=1}^M \max \left( 1 - y_i(\mathbf{w}^T \mathbf{x}_i + b), 0 \right) \\ \text{s.t.} \quad & y_i(\mathbf{w}^T \mathbf{x}_i + b) \geq 1 - \max \left( 1 - y_i(\mathbf{w}^T \mathbf{x}_i + b), 0 \right) \end{aligned}$$

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# Lab: Text Normalization