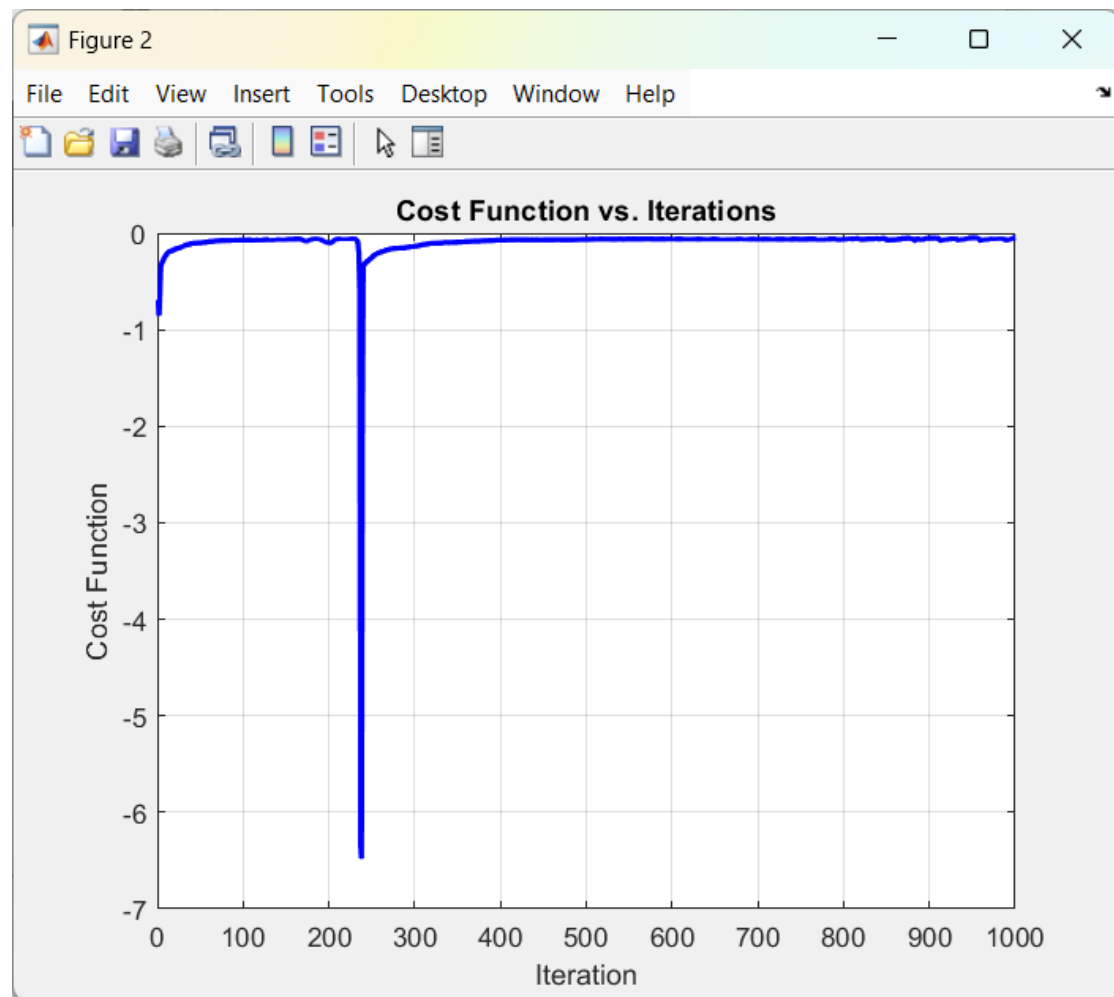
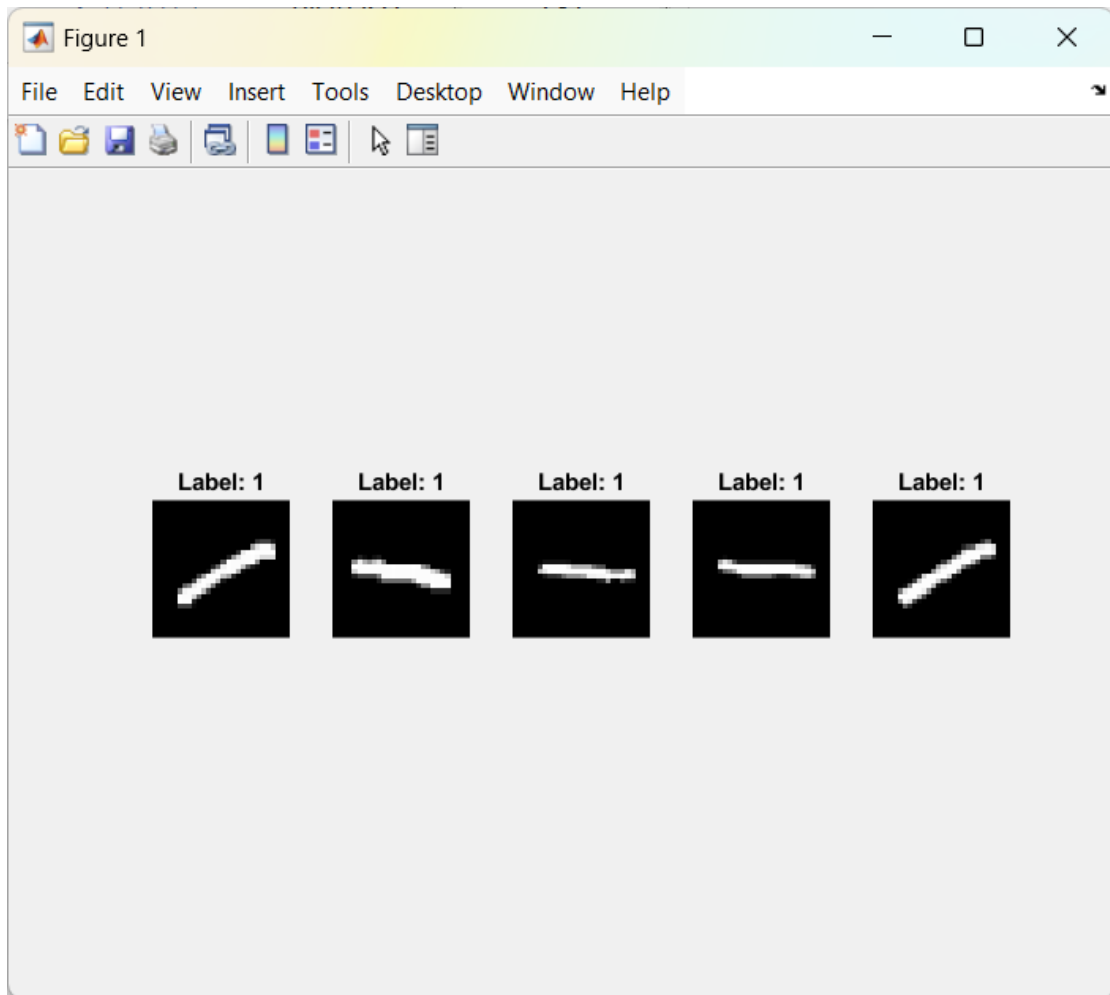


```

targil2.m
1  % Load Data
2  train = [train1; train2];
3  train_labels = [ones(size(train1, 1), 1); zeros(size(train2, 1), 1)];
4  test = [test1; test2];
5  test_labels = [ones(size(test1, 1), 1); zeros(size(test2, 1), 1)];
6  train = double(train);
7  test = double(test);
8  figure;
9  for i = 1:5
10     subplot(1, 5, i);
11     img = reshape(train(i, :), [28, 28]);
12     imshow(img, []);
13     title(['Label: ', num2str(train_labels(i))]);
14 end
15 %Parameters
16 [m, n] = size(train);
17 w = zeros(n, 1);
18 learning_rate = 0.01;
19 num_iterations = 1000;
20 cost_history = zeros(num_iterations, 1);
21 eps = 1e-6;
22 for iter = 1:num_iterations
23     z = train * w;
24     predictions = 1 ./ (1 + exp(-z));
25     predictions = max(min(predictions, 1 - eps), eps);
26     gradient = (1/m) * (train' * (train_labels - predictions));
27     w = w + learning_rate * gradient;
28     cost = (1/m) * sum(train_labels .* log(predictions) + ...
29                     (1 - train_labels) .* log(1 - predictions));
30     cost_history(iter) = cost;
31 end
cost = (1/m) * sum(train_labels .* log(predictions) + ...
                  (1 - train_labels) .* log(1 - predictions));
cost_history(iter) = cost;
end
figure;
plot(1:num_iterations, cost_history, '-b', 'LineWidth', 2);
grid on;
xlabel('Iteration');
ylabel('Cost Function');
title('Cost Function vs. Iterations');
z_test = test * w;
test_predictions = 1 ./ (1 + exp(-z_test));
test_predictions_binary = test_predictions >= 0.5;
success_rate = mean(test_predictions_binary == test_labels) * 100;
disp(['Success Rate: ', num2str(success_rate), '%']);

```





Success Rate: 98.9386%

$$1) \quad g'(x) = g(x) \cdot (1 - g(x))$$

$$g(x) = \frac{1}{1 + e^x}$$

$$g'(x) = \frac{-e^x}{(1 + e^x)^2} = \frac{-e^x}{(1 + e^x)^2}$$

$$g(x) \cdot (1 - g(x)) = \frac{1}{1 + e^x} \cdot \left(1 - \frac{1}{1 + e^x}\right) = \frac{1}{1 + e^x} \cdot \frac{e^x}{1 + e^x} = \frac{e^x}{(1 + e^x)^2}$$

$$\frac{1 + e^x - 1}{1 + e^x} = \frac{e^x}{1 + e^x}$$

$$2) Z(w) = \frac{1}{N} \sum_{t=1}^N \log(p(s_t | x_t))$$

if

$$\frac{\partial Z(w)}{\partial w} = \frac{1}{N} \sum_{t=1}^N s_t - g(w x_t) s_t^*$$

$$\frac{\partial Z(w)}{\partial w} = \frac{\partial}{\partial w} \frac{1}{N} \sum_{t=1}^N \log \left(\frac{g(w x_t)^{s_t}}{(g(w x_t)^{s_t} + (1 - g(w x_t))^{1-s_t})} \right)$$

$$= \frac{\partial}{\partial w} \frac{1}{N} \sum_{t=1}^N s_t \log(g(w x_t)) - (1 - s_t) \log(1 - g(w x_t)) = \frac{1}{N} \sum_{t=1}^N s_t x_t (g(w x_t) - (1 - s_t) x_t g(w x_t))$$

$$p(s_t) = g(w x_t) (g(w x_t))^{s_t-1} (1 - g(w x_t))^{1-s_t}$$

$$= \frac{1}{N} \sum_{t=1}^N s_t x_t (g(w x_t) - (1 - s_t) x_t g(w x_t))$$