$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ -1 & 1 & 2 & 1 \\ 0 & 2 & 1 & 3 \\ 0 & 0 & 1 & 1 \end{bmatrix} = [L] * [U]$$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ -1 & 1 & 2 & 1 \\ 0 & 2 & 1 & 3 \\ 0 & 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} L_{11} & 0 & 0 & 0 \\ L_{21} & L_{22} & 0 & 0 \\ L_{31} & L_{32} & L_{33} & 0 \\ L_{41} & L_{42} & L_{43} & L_{44} \end{bmatrix} \begin{bmatrix} 1 & U_{12} & U_{13} & U_{14} \\ 0 & 1 & U_{23} & U_{24} \\ 0 & 0 & 1 & U_{34} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$1 = [L_{11} \; 0\,0\,0] * \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad L_{11} = 1$

$2 = [L_{11} \; 0\,0\,0] * \begin{bmatrix} U_{12} \\ 1 \\ 0 \\ 0 \end{bmatrix} \quad U_{12} = 2$

$3 = [L_{11} \; 0\,0\,0] * \begin{bmatrix} U_{13} \\ U_{23} \\ 1 \\ 0 \end{bmatrix} \quad U_{13} = 3$

$3 = U_{13} = 0 + 0 + 0$

$4 = [L_{11} \; 0\,0\,0] * \begin{bmatrix} U_{14} \\ U_{24} \\ U_{34} \\ 1 \end{bmatrix}$

$U_{14} = 4$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ -1 & 1 & 2 & 1 \\ 0 & 2 & 1 & 3 \\ 0 & 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ L_{21} & L_{22} & 0 & 0 \\ L_{31} & L_{32} & L_{33} & 0 \\ L_{41} & L_{42} & L_{43} & L_{44} \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 & 4 \\ 0 & 1 & U_{23} & U_{24} \\ 0 & 0 & 1 & U_{34} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$-1 = \begin{bmatrix} L_{21} & L_{22} & 0 & 0 \end{bmatrix} * \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad L_{21} = -1$$

$$1 = \begin{bmatrix} -1 & L_{22} & 0 & 0 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 0 \\ 0 \end{bmatrix} \quad 1 = -2 + L_{22} + 0 + 0$$

$$L_{22} = 3$$

$$2 = \begin{bmatrix} -1 & 3 & 0 & 0 \end{bmatrix} \begin{bmatrix} 3 \\ U_{23} \\ 1 \\ 0 \end{bmatrix} \quad 2 = -3 + 3U_{23} + 0 + 0$$

$$5 = 3U_{23}$$

$$U_{23} = \frac{5}{3}$$

$$1 = \begin{bmatrix} -1 & 3 & 0 & 0 \end{bmatrix} \begin{bmatrix} 4 \\ U_{24} \\ U_{34} \\ 1 \end{bmatrix} \quad 1 = -4 + 3U_{24} + 0 + 0$$

$$5 = 3U_{24}$$

$$U_{24} = \frac{5}{3}$$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ -1 & 1 & 2 & 1 \\ 0 & 2 & 1 & 3 \\ 0 & 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ -1 & 3 & 0 & 0 \\ L_{31} & L_{32} & L_{33} & 0 \\ L_{41} & L_{42} & L_{43} & L_{44} \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 & 4 \\ 0 & 1 & 5/3 & 5/3 \\ 0 & 0 & 1 & U_{34} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$0 = \begin{bmatrix} L_{31} & L_{32} & L_{33} & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad L_{31} = 0$$

$$2 = \begin{bmatrix} 0 & L_{32} & L_{33} & 0 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 0 \\ 0 \end{bmatrix} \quad L_{32} = 2$$

$$1 = \begin{bmatrix} 0 & 2 & L_{33} & 0 \end{bmatrix} \begin{bmatrix} 3 \\ 5/3 \\ 1 \\ 0 \end{bmatrix} \quad 1 = \frac{10}{3} = L_{33}$$

$$L_{33} = -\frac{7}{3}$$

$$3 = \begin{bmatrix} 0 & 2 & -\frac{7}{3} & 0 \end{bmatrix} \begin{bmatrix} 4 \\ \frac{5}{3} \\ u_{34} \\ 1 \end{bmatrix}.$$

$$\frac{7}{3} u_{34} = -3 + \frac{10}{3} \qquad \frac{7}{3} u_{34} = \frac{1}{3}$$

$$u_{34} = \frac{1}{7}$$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ -1 & 1 & 2 & 1 \\ 0 & 2 & 1 & 3 \\ 0 & 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ -1 & 3 & 0 & 0 \\ 0 & 2 & -\frac{7}{3} & 0 \\ L_{41} & L_{42} & L_{43} & L_{44} \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 & 4 \\ 0 & 1 & \frac{5}{3} & \frac{5}{3} \\ 0 & 0 & 1 & \frac{1}{7} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$0 = \begin{bmatrix} L_{41} & L_{42} & L_{43} & L_{44} \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} \qquad L_{41} = 0$$

$$0 = \begin{bmatrix} 0 & L_{42} & L_{43} & L_{44} \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 0 \\ 0 \end{bmatrix} \qquad L_{42} = 0$$

$$1 = \begin{bmatrix} 0 & 0 & L_{43} & L_{44} \end{bmatrix} \begin{bmatrix} 3 \\ \frac{5}{3} \\ 1 \\ 0 \end{bmatrix} \qquad L_{43} = 1$$

$$1 = \begin{bmatrix} 0 & 0 & 1 & L_{44} \end{bmatrix} \begin{bmatrix} 4 \\ \frac{5}{3} \\ \frac{1}{7} \\ 1 \end{bmatrix}$$

$$1 = \frac{1}{7} + L_{44} \qquad L_{44} = \frac{6}{7}$$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ -1 & 1 & 2 & 1 \\ 0 & 2 & 1 & 3 \\ 0 & 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ -1 & 3 & 0 & 0 \\ 0 & 2 & -\frac{7}{3} & 0 \\ 0 & 0 & 1 & \frac{6}{7} \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 & 4 \\ 0 & 1 & \frac{5}{3} & \frac{5}{3} \\ 0 & 0 & 1 & \frac{1}{7} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$