

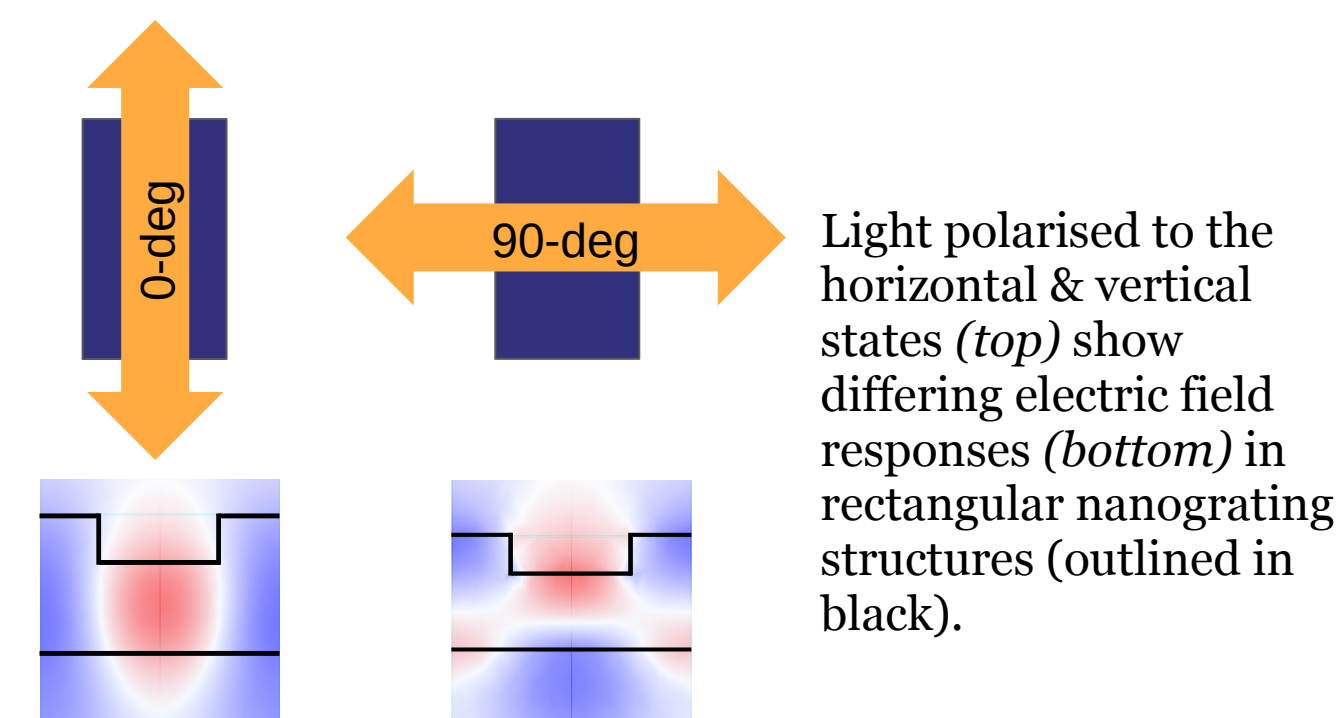
Quantifying symmetry violations for optimising algorithmic designs

Zaid Haddadin¹, Dae Yong Kim², Jiuk Byun³, Lisa V. Poulikakos^{2,3}

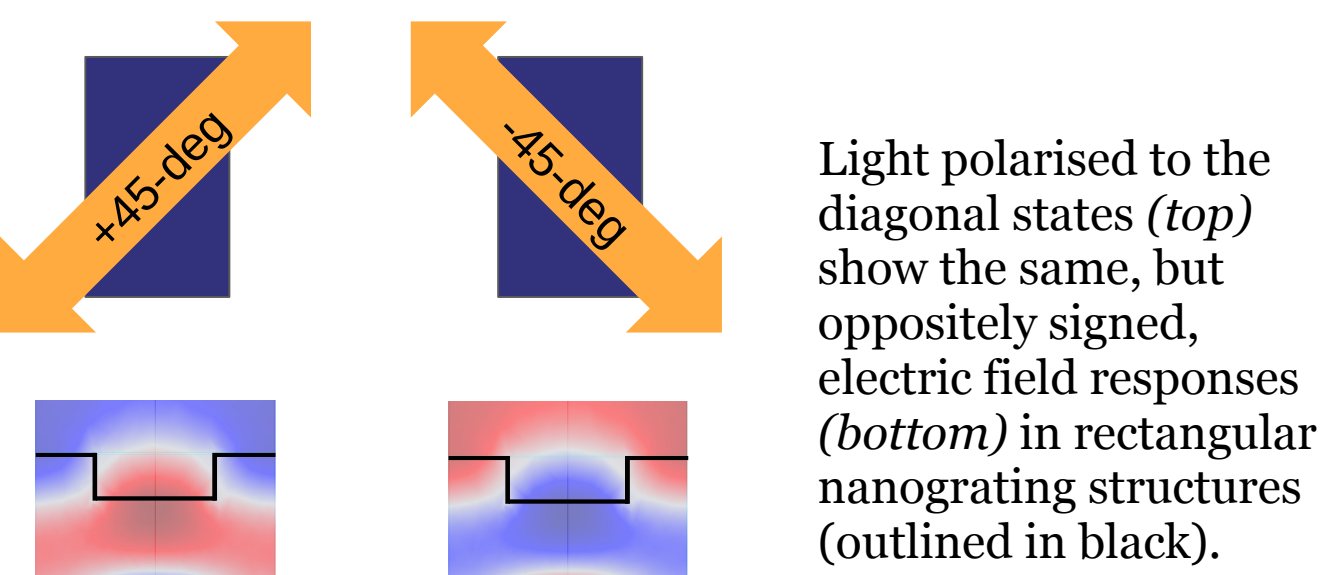
1. *Electrical & Computer Engineering, University of California San Diego*
2. *Mechanical & Aerospace Engineering, University of California San Diego*
3. *Materials Science & Engineering, University of California San Diego*

Introduction

Structures with sufficient **asymmetry** can yield **unique light-matter interactions** under differing polarisations of light (1,2).



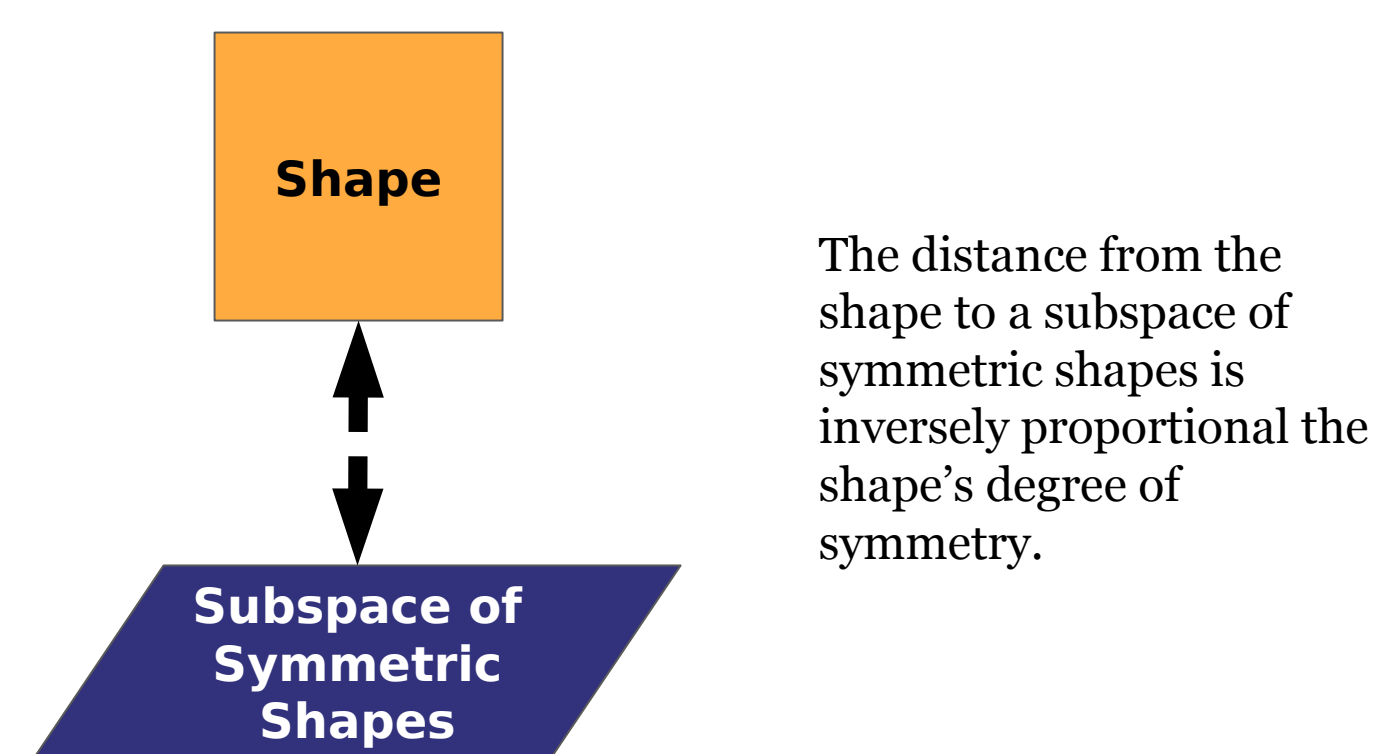
Axes of structures **lacking asymmetry** result in **identical light-matter responses** for varying polarisations of light (1,2).



Designing sufficiently asymmetric structures is vital for creating selective light-matter interactions across a wide arrangement of polarisations of light.

Materials & Methods

The **degree of symmetry of a shape** can be **quantified** by the distance of its projection onto a subspace of symmetric shapes (3).



Averaging the distance across a range of angles provides rotational and reflective symmetry scores:

$$\sum_{\theta_i} (\text{norm}(\text{dot}(\text{Symmetry Operator}(\text{argument: } \theta), \text{Shape})))$$

Number of angles

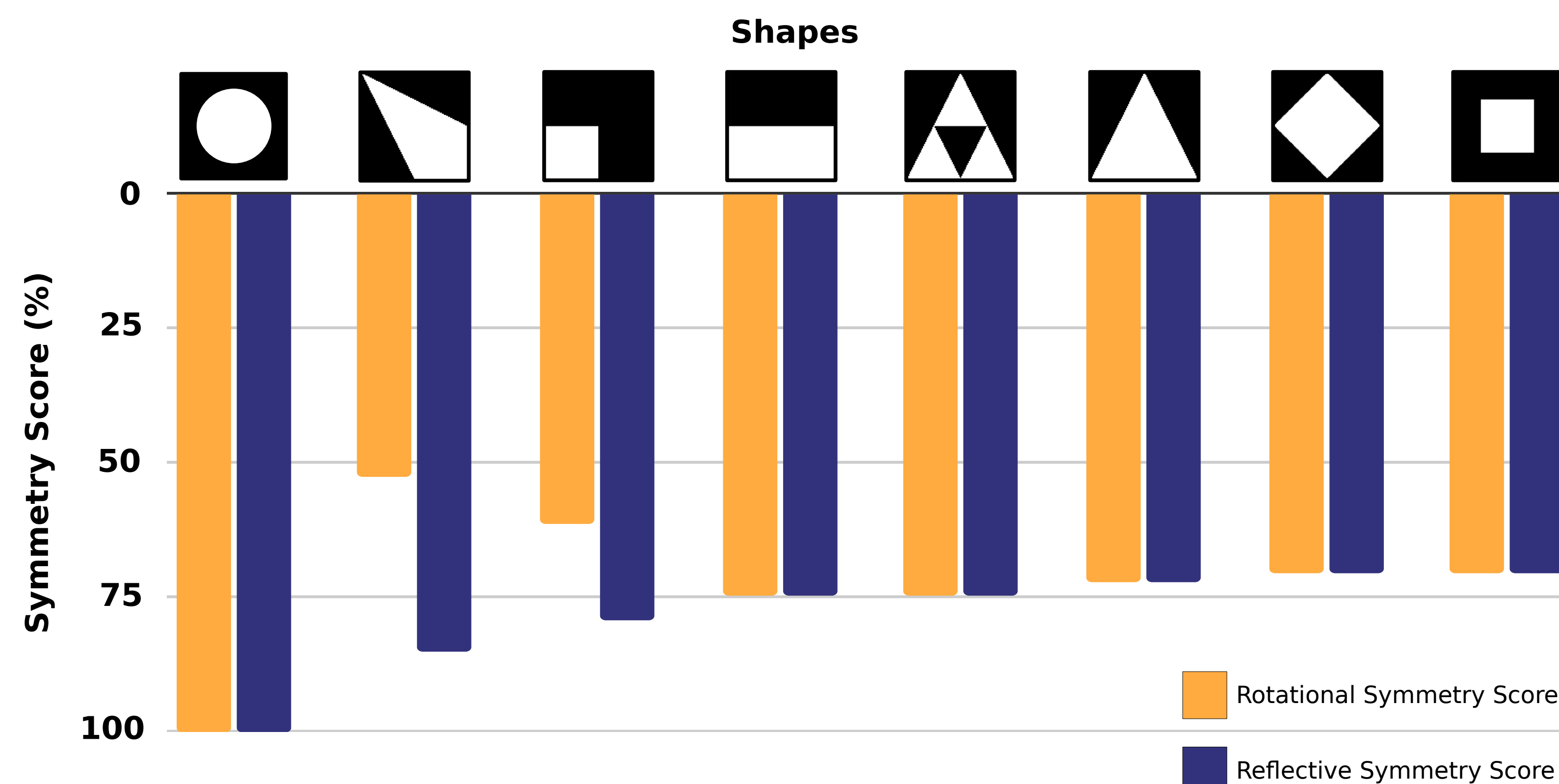
Manipulating the symmetry operator specifies the type of symmetry scored: rotational or reflective.

Results

The **symmetry scores corresponding to the degree of rotational or reflective symmetries were calculated for various shapes**. These calculations transform symmetry from a binary concept – a shape is either symmetrical or asymmetrical – to a continuous spectrum: a shape has a certain degree of symmetry. These shapes were taken from an information security hash visualisation (4) known as identicons (5).

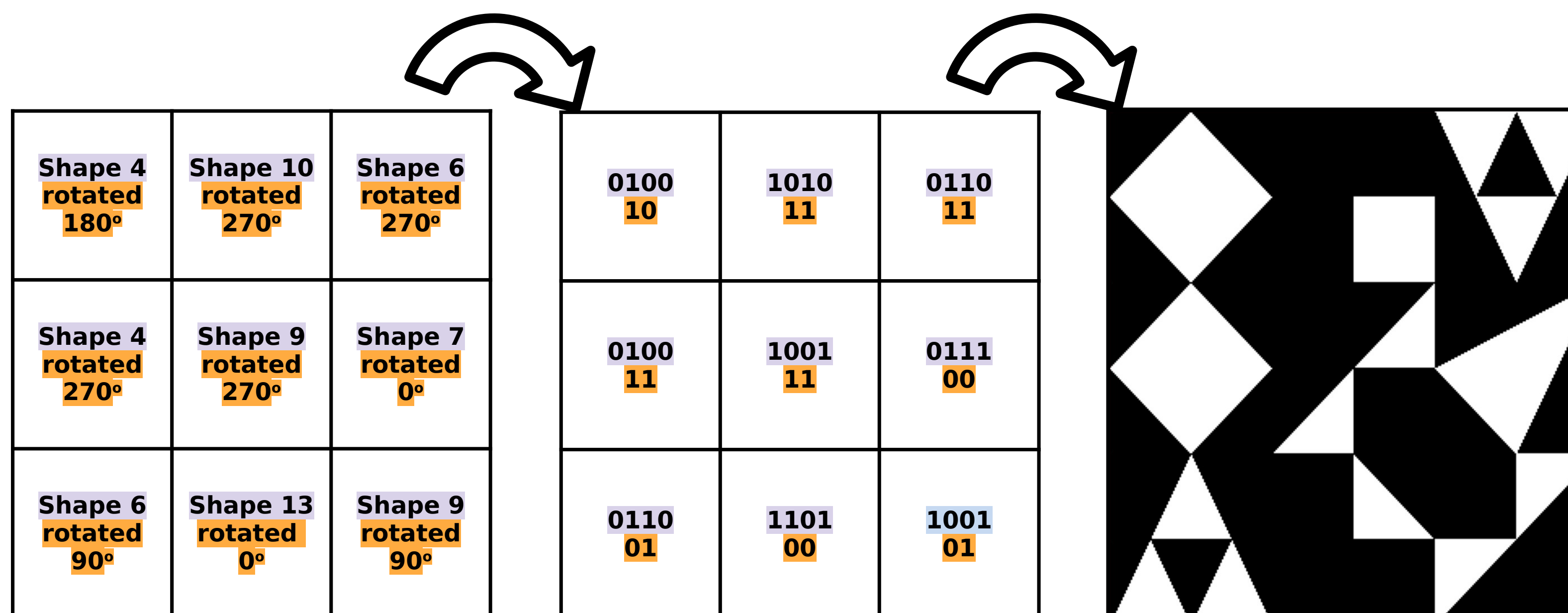
The **symmetry scores below take into account the shape (in white) in the context of the empty space surrounding it (in black)** as light-matter interactions are affected by the empty space around a structure along with the geometry of the structure. The shapes are presented in order of decreasing rotational symmetry score from the left to the right.

Rotational & Reflective Symmetry Scores



First Steps Towards a Genetic Algorithm

The ability to determine the degree of symmetry of a shape can provide future insight towards engineering selective light-matter interactions across differing polarisations of light. To this extent, **an evolution-inspired, genetic-based machine learning model is being constructed that takes advantage of symmetry scoring to construct an idealised asymmetric structure**. Such an algorithm is envisioned to use the aforementioned shapes (among others) as elementary building blocks.



An M-by-N grid acts as a blueprint denoting the building block shape and a respective angle (0, 90, 180, or 270 degrees) for an asymmetric structure.

A decimal-to-binary transformation to create a binary-based “DNA analogue” that can evolve within a machine learning model's parameters.

Each decimal-containing grid square will refer to a building block shape. When put together, the building block shapes will result in a new asymmetric structure.

Conclusions

The asymmetry inherent in a geometric shape affects the expected light-matter interactions. **Quantifying the degree of symmetry paves the path towards correlating the effects of changing specific symmetries to the observed light-matter interactions**. This can open a future where the idealised asymmetry of a structure can be engineered for an intended application.

The ability to select for light-matter interactions through a geometric-tuning of structures can have implications for sensing applications in several fields such as astrobiology (6), geology (7), and medicine (1,2). **Future steps of this work aim to realise the ideal combination of elementary building blocks to create maximal asymmetry.**

Literature Cited

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Further Information

Contact me at zalhadda@ucsd.edu if you have a question or comment. Our lab is at <http://poulikakos.ucsd.edu/>.