



Amirkabir University of Technology
Simulation report on my selected paper
entitled "Energy Cost Optimization in
Dynamic Placement of Virtualized Network
Function Chains"

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1 Introduction

The energy crisis has been a significant issue for years, as most resources are non-renewable such as oil, coal, and gas. The majority of the world's energy comes from non-renewable resources, which, due to the large amounts of greenhouse gases emitted (such as carbon dioxide), lead to global warming. To add to this concern, energy consumption and greenhouse gas emissions resulting from Internet usage have been steadily increasing in recent years. For example, data center web servers, such as those used by Google and Facebook, account for 2% of the greenhouse gas emissions about the same as air travel.

Fortunately, virtualization technology can spur a ——— ogy has a very high migration cost both in terms of time and energy. Most importantly, its management is only limited to the service provider.

we can minimize energy consumption using NFV technology, which can extend virtualization to other PMs, such as routers, switches, etc. Physical machines consume maximum power only during peak demand times, and average servers remain idle over 90% of the time. However, the power consumption of an idle machine is nearly 60% of the peak load power consumption of the machine [18]. By reducing the number of active machines, and turning off the idle machines, we can reduce the energy consumption of the network.

we use the minimum capacity mechanism to minimize the frequent change of the machines' states. According to this mechanism, we required a minimum capacity to transit an OFF node to an ACTIVE node. This helps to increase the utilization of the machine. Fifty percent of the power consumed by the PMs is to reduce heat generated during processing. Hence, depending on the PM load, the cooling load also varies. Therefore, in this paper, we normalize the energy consumption cost of the PMs, and the respective VM instances on those machines, which will help with performing a better analysis of the network's energy consumption issues. We consider the dynamic service chain placement, which is a more realistic scenario than static placement. However, in this work, we do not consider the energy consumption of the link, as the difference of the energy consumption of the link from idle to full utilization is very minimal.

novel contribution is summarized as follows: 1) First, we design an energy-saving model using an M/M/c queuing network for the placement of multiple service chains' functions in the network. 2) We formulate an optimization

problem to minimize the total energy consumption cost of the network with capacity and delay as the constraints and prove that NP-hard. 3) We propose an efficient dynamic placement of VNFs (DPVC) heuristic algorithm for the dynamic placement of VNFs in the network. Via MATLAB experimentation, we demonstrate that our algorithm significantly minimizes the cost of energy consumption.

1.1 Network Function Virtualization

Network Function Virtualization (NFV) technology has emerged as a new alternative, which can overcome the pitfalls. NFV offers a new way to design, deploy, and manage networking services by decoupling the network functions, such as network address translation, firewalls, intrusion detection, domain name service, etc., from dedicated hardware devices so they can run in software. These network functions are called virtualized network functions (VNFs), and they are placed on physical machines as virtual machine (VM) instances. Software provisioning. An example of service chain placement in the network is presented in Figure 1. The network consists of nine nodes considered as the physical machines of the network. We have four different network functions: A, B, C, D , which are available in different nodes of the network, as shown in Figure 1. Table 1 shows four service chain demands, with the source and destination paths of four different flows. The virtual links and physical path of each flow from source to destination are given in the table. The first service chain, $SC1 (B-C-A)$, at source node 1, will be placed in the sequence of nodes 2, 4, 7. That is, the first VNF B will be placed on node 2, then the second VNF C will be placed on node 4, where the function C is available. The final VNF of $SC1$ will be placed on node 7 and the chain will terminate at destination node 6. Similarly, the second service chain, $SC2 (C-A-D)$, will start from source node 5, terminate at destination node 1, and place VNFs on nodes 9, 7, 4. The third service chain, $SC3 (A-D-B)$, will start from source node 6, terminate at destination node 1, and place VNFs on nodes 7, 4, 2. However, for the fourth service chain, $SC4 (B-D-B)$, from the source node 5, after placement of the first VNF B on node 9, the next function D is not available in the neighboring nodes. Therefore, it will be placed on node 4, the last VNF B will be placed on node 2, and finally, it will terminate at destination node 6.

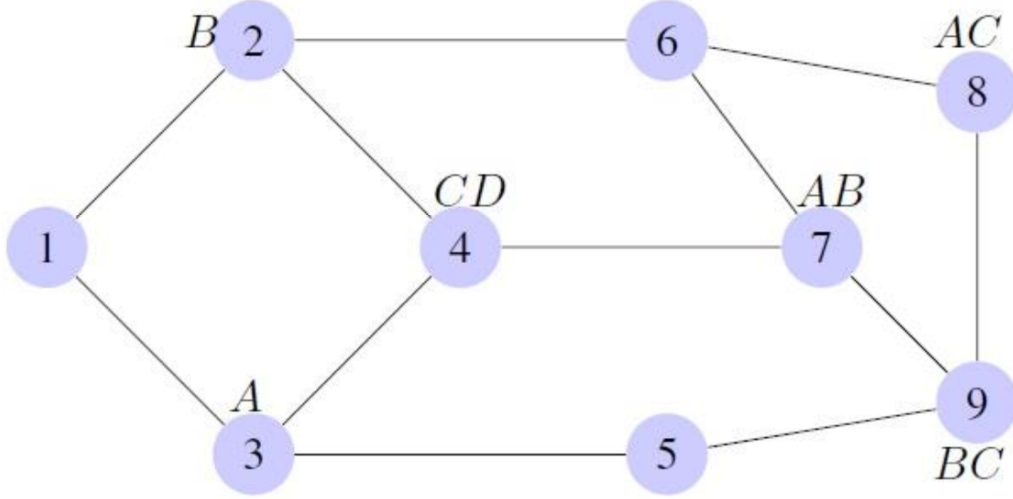


Figure 1: Illustrative example of service chain placement in the network.

Table 1: VNF placement of the service chains.

SC number	Source	Destination	SC Demand	Virtual Path	Physical Path
SC1	1	6	B-C-A	1-2-4-7-6	1-2-4-7-6
SC2	5	1	C-A-D	5-9-7-4-1	5-9-7-4-2-1
SC3	6	1	A-D-B	6-7-4-2-1	6-7-4-2-1
SC4	5	6	B-D-B	5-9-4-2-6	5-9-7-4-2-6

2 Design and modeling

2.1 Off-Idle-Active State Transitionel

Figure 2 illustrates the Off-Idle-Active (OIA) state transition diagram of the PM. Each machine has three states named — nsumption of the machine can be evaluated in each state as well.

(1) OFF→ACT: Initially, the machine is in an OFF state, and it consumes zero power(Z_{power}). The machine will turn ACTIVE when the sum of the capacities of the VNFs in the queue exceeds the minimum capacity, or when the waiting time of any VNF in the queue exceeds the maximum waiting time. We adopted this method to maximize utilization and to avoid the

machine from engaging in the switching state too often. This method also minimizes the waiting time of the VNFs, which were waiting in the queue for a longer time.

(2) ACT→IDL: When all VNFs in the ACTIVE machine finish or migrate to other machines, the machine will go to the IDLE state. In the IDLE state, a machine will consume the basic amount of energy, which can be evaluated as the product of maximum power ($Mpower$) consumed by the machine and the ratio between default capacity ($Dcap$) of the machine to the maximum capacity ($Mcap$) of that machine .

(3) IDL→OFF: If no new VNFs are assigned to the machine in the IDLE state within a predefined time, the machine will turn OFF.

(4) IDL→ACT: If new VNFs are assigned, or if the VNFs migrate from other ACTIVE machines, the machine will turn ACTIVE from the IDLE state. Evaluation of the machine's energy consumption in the ACTIVE state is similar to the IDLE state, only we need to add the summation of the capacities of the deployed VNFs ($\sum Vcap$) in the machine to the default capacity of the machine. Here, the maximum power of the machine represents the maximum computing and cooling power of the machine.

2.2 M/M/c Queuing Network Model

Many analytical models have been presented by various articles using the M/M/1 queuing model. However, in practice, real-world applications are not processed by the single-service node. Therefore, we use the M/M/c queuing network model , where each service chain request can be processed through multiple service nodes, and each service node can process multiple network functions. Our energy-saving model adheres to the following assumptions. The VNFs of the service chain arrivals follow a Poisson process and are served in the order of their arrivals i.e., the $(i+1)$ th VNF of a service chain can start only after completion of the i th VNF of that service chain. In our model, a service node can process a maximum c number of VNFs of different service chains together. We assume all service chains are independent. All service times are independent and exponentially distributed with mean $1/\mu$. The idle time follows the exponential distribution with mean: $1/\theta_1$, and the off time follows exponential distribution with mean: $1/\theta_2$. Both aforementioned variables are independent of each other. Here, the state space is settled by $S = \{(m, n), m = \{0, 1\}, 0 \leq n \leq \inf\}$, where m denotes the machine is ON or OFF, and n denotes the number of VNFs in the machine. The state-

transition-rate diagram for a queuing system is shown in Figure 3. State $(0, 0)$ denotes that the machine is ON, but with no VNF, i.e., the IDLE state, and $(0, n)$ denotes that the machine is ACTIVE with n number of VNFs. State $(1, n)$ shows the OFF state with n number of VNFs in waiting.

Let $P_{m,n}$ denote the steady-state probabilities at state (m, n) , then the following notations are used:

$P_{0,n}$ = Probability that n VNFs exist in the PM in the ACTIVE state.

$P_{0,0}$ = Probability that no VNFs exist in the PM, and it is IDLE.

$P_{1,n}$ = Probability that n VNFs exist in the PM in the OFF state.

Based on Figure 3, the following balanced equations can be given:

$$(\lambda + \theta_1)P_{0,0} = \mu \sum_{n=1}^c n.P_{0,n} \quad (1)$$

$$(\lambda + c\mu)P_{0,n} = \lambda.P_{0,n-1} + c\mu.P_{0,n+c} \quad \text{where } (n = 1, \dots, c-1) \quad (2)$$

$$(\lambda + c\mu)P_{0,n} = \lambda.P_{0,n-1} + c\mu.P_{0,n+c} + \theta_2.P_{1,n} \quad \text{where } (n = c, c+1, \dots, \infty) \quad (3)$$

$$\theta_1.P_{0,0} = \lambda.P_{1,0} \quad (4)$$

$$\lambda.P_{1,n} = \lambda.P_{1,n-1} \quad \text{where } (n = 1, \dots, c-1) \quad (5)$$

$$(\lambda + \theta_2)P_{1,n} = \lambda.P_{1,n-1} \quad \text{where } (n = c, c+1, \dots, \infty) \quad (6)$$

Let P_{ACTIVE} , P_{IDLE} , and P_{OFF} denote the probabilities that a PM is in the ACTIVE, IDLE, and OFF states respectively. With the normalizing equation $\sum_{n=1}^{\infty} P_{0,n} + P_{0,0} + \sum_{n=0}^{\infty} P_{1,n} = 1$, the solutions of these equations can be obtained as:

$$\begin{cases} P_{ACTIVE} = \sum_{n=1}^{\infty} P_{0,n} \\ P_{IDLE} = P_{0,0} \\ P_{OFF} = \sum_{n=0}^{\infty} P_{1,n} \end{cases}$$

Theorem1 : $P_{OFF} = \sum_{n=0}^{\infty} P_{1,n} = [c.\frac{\theta_1}{\lambda} + \frac{\theta_1}{\theta_2}]P_{0,0}$. Assuming, $\alpha = \frac{(\theta_1+\lambda).k.(k+c)}{2c^2}$ for some large integer k , we have,

$$\textit{Theorem2} : P_{ACTIVE} = \sum_{n=1}^{\infty} P_{0,n} = [\frac{\alpha}{c\mu} + \frac{\theta_1}{\lambda+c\mu}].$$

$$\textit{Theorem3} : \text{if } \sum_{n=0}^{\infty} P_{0,n} + \sum_{n=0}^{\infty} P_{1,n} = 1, \text{ then } P_{0,0} = \frac{1}{1+\frac{\theta_1}{\theta_2}+\frac{c\theta_1}{\lambda}+\frac{\alpha}{c\mu}+\frac{\theta_1}{\lambda+c\mu}}$$

By using this value $P_{0,0}$ we can find P_{OFF} , P_{IDLE} , and P_{ACTIVE} of each PM. That is, we can determine what is the state of the machine, and how

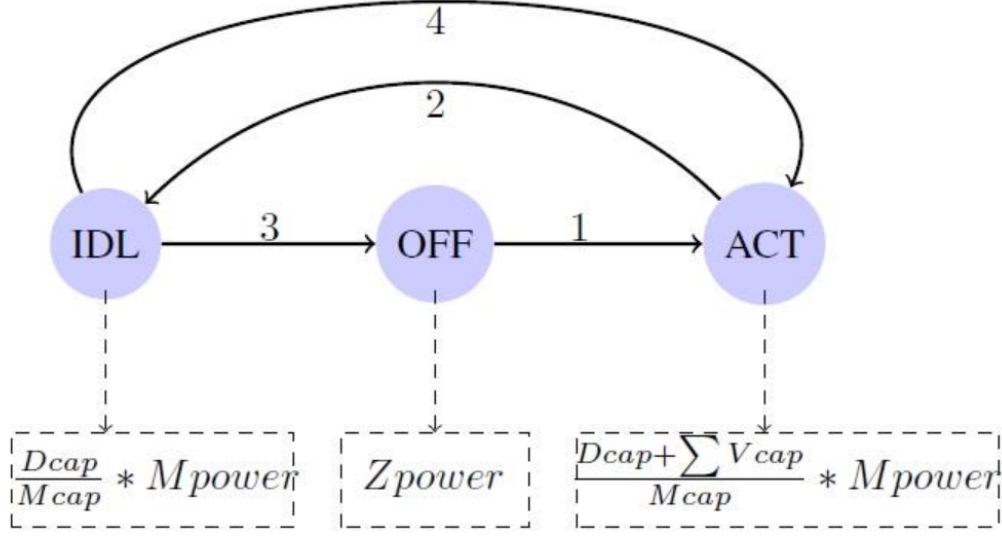


Figure 2: OIA state transition diagram of PM

many VNFs are on the machine. Then, as given in Figure 2, the amount of the power consumed by the machine in different states can be evaluated

3 Problem Formulation

we can get the state of a PM at a particular time and the number of VM instances on the PM at that time. Considering this, we propose an optimization problem to minimize the energy consumption cost in this section.

3.1 Variable Declaration

In Table 2, we declared the variables used to formulate the optimization problems. We classify all variables in four groups. The first group represents the different sets we will use. N and L are the set of nodes and links, respectively. Here, a node means a PM. sC represents the set of all requested service chains and vF is the set of VNFs we have in our network. T is the set of iterations. vM is the set of VM instances on a particular node and K is the set of commodities.

The second group represents the variables and different network parameters we will use. $n(u)$ is the decision variable of the physical machine u ,

3.2 Objective Function and Constraints

By using the notations given in Table 2, we state the energy consumption cost is:

$$e_c = \sum_{u \in \omega} n(u) * \left(\frac{c^I(u) + \sum_{i \in VM(u)} C_i^v(u)}{C^N(u)} \right) \quad (7)$$

$$\text{where } n(u) = \begin{cases} 1, & \text{if node}(u) \text{ is IDLE or ACTIVE} \\ 0, & \text{otherwise} \end{cases}$$

The total energy consumption cost $te_c = \sum_{t \in T} e_c(t)$. Here, $n(u)$ represents the state of the node u . The value is 1 if the node is ACTIVE or IDLE, and 0 otherwise. $C^N(u)$, $C^I(u)$, and $C_i^v(u)$ represent the maximum capacity, default capacity of the machine in the IDLE state, and capacity of the VM instance i (on u) of the node u , respectively. e_u^N is the cost of energy consumed by node u at a utilization of 100%. $e_c(t)$ is the cost of energy consumption by the network at time t . The total cost of energy consumption te_c of the network is the sum of energy consumption of each individual node in various states over a period of time. Our objective is to *Minimize* te_c . The set of operational constraints to be noticed are:

1) *FlowConstraints* :The inequality in Equation (8) ensures that the flow from node u to node v must be positive. Equation (9), ensures that the total flow along each link should not exceed the total capacity of that link. The flow conservation constraint is shown in Equation (10), where r_k unit of traffic is created in its source, and is destroyed in its destination. For a stable system, the limit of the utilization of each node and links lies between $[0, 1]$. Equation (11) ensures the utilization limit of each PM.

$$F_i(u, v) \geq 0, \quad \forall i, F_i \in K, \forall (u, v) \in L \quad (8)$$

$$\sum_{i=1}^k F_i(u, v) \leq C^L(u, v) * L(u, v), \quad \forall (u, v) \in L \quad (9)$$

$$\sum_{(u,v) \in L} F_k(u, v) - \sum_{(v,u)} F_k(v, u) = \begin{cases} r_k, & \text{if } u = s_k \\ -r_k, & \text{if } u = t_k \\ 0, & \text{otherwise} \end{cases} \quad (10)$$

$$0 \leq \frac{\lambda}{c\mu} \leq 1 \quad (11)$$

2)*CapacityConstraints* :The inequality in Equation (12) ensures that the total sum of the capacities of VNFs on node u must be less than or equal to ‘utility capacity’ of node u , i.e., the difference between maximum capacity and default capacity of u . The variable in Equation (13) shows the function f of service chain sc is placed on node u . The Equation (14) inequality ensures that the demand of function f of service chain sc at node u must be less than or equal to the available capacity of node u . The next inequality in Equation (15) presents the demand of function f of service chain sc at node u less than or equal to the capacity of the VM instance i of the node u .

$$\sum_{i \in vM(u)} C_i^V(u) \leq C^N(u) - C^I(u), \quad \forall(u) \in N \quad (12)$$

$$Y_F^{sc}(u) = 1, \quad \forall(u) \in N, f \in vF, sc \in sC \quad (13)$$

$$\sum_{sc \in sC} d_f^{sc}(u) \leq C^N(u) - \sum_{i \in vM(u)} C_i^V(u) - C^I(u), \quad \forall(u) \in N, f \in vF, sc \in sC \quad (14)$$

$$d_f^{sc}(u) \leq C_i^V(u), \quad \forall(u) \in N, f \in vF, sc \in sC \quad (15)$$

3)*PlacementConstraints* :The binary variable in Equation (16) shows the function f placed on the i th VM instance of node u . The inequality in Equation (17) shows the queuing delay of function f of service chain sc must be less than or equal to the maximum delay at node u . Equation (18) ensures that the delay faced by a flow along its path must be less than or equal to the maximum delay the flow can tolerate. Equation (19) checks the status of the node for the placement of the function. It consists of three parts. The first inequality checks whether the node is ACTIVE or not, and the second part checks the node is IDLE or not. The last part checks if the node is OFF or not, and whether the demand on the node exceeds the threshold value.

$$X_i^f(u) = 1, \quad \forall(u) \in N \quad (16)$$

$$qd_f^{sc}(u) \leq d_{MAX}(u), \quad \forall(u) \in N, f \in vF, sc \in sC \quad (17)$$

$$\sum_{(u,v) \in P_k} d_{F_k}(u,v) \leq D_k, \quad \forall(K), F_k \in K \quad (18)$$

4 Solution Approach

In this section, we will propose the dynamic placement of the VNF chains heuristic algorithm. This placement method reduces the number of active nodes in the network. We use a restricted spanning tree mechanism for the placement of the VNF. To reduce the energy cost, we select the path for the flow, which has more active nodes, and fewer hop counts from the source to destination.

We used *NSFNET* topology (matrix A) consisting of a set of nodes and links, of equal weight. We assign different types of VNFs to each node randomly presented by matrix B, i.e., the rows of the matrix present the nodes and columns existing in the network functions. $B(i, j) = 1$, if the i th node of the network has the j th function, else 0. ST is the spanning tree. U_{max} and $U_{i\text{dele}}$ are the arrays presented as the maximum capacity and default capacity of each node in the graph, respectively. vNF is the set of functions, and pt is the processing time of each function. ldl_{time} is the amount of time the node can stay IDLE. If it does not receive any function, during this time limit it will turn OFF. off_{time} is the maximum amount of time a VNF can wait in an OFF PM. If the amount of time is exceeded the limit, the PM will turn ON. VM_{cap} is the capacity of each VM instance. We are using the spanning tree concept in our algorithm. Here, if a machine turns ACTIVE, we will add it to the spanning tree, and if an active machine turns OFF, we will remove it from the spanning tree. We are using two sets of operations (Add and Delete) in our algorithm to handle this. When a machine turns ACTIVE, we use the Add operation to add that machine to the spanning tree, and when a machine turns OFF, we use the Delete operation to remove it from the spanning tree. We are using two more operations such as Assign and Release for the placement of a VNF. When a new VNF is placed on the machine, by the Assign operation, we provide resources to that VM instance. If a running VNF terminates by the Release operation, we release the assigned resources of that VM instance, which can be assigned to a new VNF. The definitions of these operations are as follows:

Definition1 : [Add] if ST is an arbitrary set, u is an arbitrary element, where $ST = U_i : i \in I$, I is an Index set, then we define $Sdd(ST, u) = ST \cup u$.

Definition2: [Delete] if ST is an arbitrary set, $u \in ST$ is an arbitrary element, where $ST = U_i : i \in I$, I is an Index set, then we define $Delete(ST, u) = ST - u$. *Definition 3*: [Assign] if u^i is an arbitrary set and

i is the number of elements in u , and $j \in u$ is an arbitrary element, then we define $Assign(u^i, j) = u^{(i+1)}$.

Definition 4: [Release] if u^i is an arbitrary set and i is the number of elements in u , and $j \in u$ is an arbitrary element, then we define $Realease(u^i, j) = u^{(i-1)}$. The DPVC algorithm works as follows: First, we generate four structures named, *ServiceChain*, *ChainTime*, and *Currlnp*. The structure *VM* consists of five fields. *VM_{flg}* shows whether the VM is ON or OFF, *VM_{exp}* presents the termination time of the VM, and *VM_{fun}* presents the network function running in the VM. *VM_{wait}* shows the waiting time, and *VM_{flow}* shows a number of flows are sharing that VNF. The structure *ServiceChain* consists of five fields, i.e., the *Chain* presents the service chain. The *Source*, *destination*, *FLOW_{len}*, and *FLOW_{num}* represent the source, destination, length, and number of the flows, respectively. The structure *ChainTime* consists of six fields. The first field *startTime* holds the start time of each VNF of the service chain and the second field *pTime* shows the processing time of each VNF of the service chain, and the third one is the *presource*, i.e., the node where the previous VNF of the service chain was placed. Initially, *preSource* is the chain source. *chainDest* shows the destination of the flow. *hop* and *endTime* present the end-to-end number of hop and termination time of the flow, respectively. *Currlnp* is the structure, which holds a set of VNFs for the current iteration for placement. After placement, the structure will discard all values of the structure. This structure consists of seven fields, i.e., *currVNF* shows the VNF name, *currSource* shows its source, *currDest* shows its destination, *chainNum* shows which service chain the VNF belongs to, *currFLOW_{len}* shows the flow length, *FLOW_{no}* shows the flow number, and *Etime* shows the termination time of the flow. After creation of the structure for each iteration, we do the following: We take as a maximum one flow and its service chain as an input and set its service time by *setchainTime* function. By *currVNFinput()*, we select the VNFs from different existing service chains for placement. Then, we call the placement function for the Placement of the selected VNFs. We check the termination time of all the VM instances of each active node. If any VNF terminates, we Release them. We also check the idle-time of each IDLE node, if the idle-time exceeds the maximum idletime, we turn that node OFF. We calculate the energy consumption cost of the system for each iteration by considering the status (ACTIVE, IDLE, OFF) of each node and the number of VNFs on them. After each loop iteration, we update the structure *VM*. In the Placement algorithm, we retrieve each VNF (*nf*) and their current

source node (s), i.e., where the previous function of that service chain has been placed and their destination node(d). Then, we call the RDFST function for the placement of each VNF. After placement of the VNF, the chain time of the service chain gets updated. After placement of all VNFs, the Placement function returns the values to the DPVC algorithm. The RDFST algorithm works as follow. First, we retrieve the nodes that contain the required service function (fun) using *nodeWithfun()*. We assign priority to these nodes by the function, *assignPriorityNodes* . Here, if the same node has availability for the new function, then it will be given the highest priority. Second priority will be given to the other active nodes with availability. Third priority will be given to the non-empty OFF nodes, and fourth priority will be allocated to empty OFF nodes. If two nodes have the same priority, then preference will be given to the node with the minimum shortest path distance *spd*. Here *spd* is calculated by adding the shortest path from the current source (s) to the node and from the node to the destination (d). By using structural sorting, we sort the nodes based on their priority, retrieve the most suitable node (nN) for the placement of the VNF from the sorted structure (*nodes_{stored}*), and Assign the VNF (fun) to that node and add the boot time if the VM is OFF. If the node is not ACTIVE, we check to see if the assigned capacity of that node exceeds the minimum capacity (min-cap) or not. If the minimum capacity has been exceeded, then we turn that node ACTIVE. Then, by the Add operation, we add the node to the spanning tree (*ST*). Otherwise, we check the waiting time of all the VMs. If the waiting time of any VM exceeds the maximum waiting time (*off_iime*), we turn that node ACTIVE. After successful placement of a VNF, the RDFST function returns the value to the Placement algorithm.

5 Experiment Setup

We used MATLAB to compare the performance of the algorithms. I considered the *NSFNET* network. However, in this paper considered the randomly generated partially meshed networks. The length of flow is 10-100 packets, and all packets are of equal size. The three service chains are generated of length consisting of 4 VNFs. I considered 10 different types of network functions. Table 3 shows the details of the experimental parameter used in the simulated scenario for this work.

Table 2: List of commonly used variables and notations

Variables	Descriptions
Sets	
N	Set of PMs/nodes
L	Set of links
vF	Set of VNFs
sC	Set of service chains
T	Set of iterations
$vM(i)$	Set of VM instances on a node i
K	Set of commodities
Variables and Network Parameters	
u	Node u
$l(u, v)$	Link (u, v)
s_k, t_k	Source and destination of commodity $f_k \in K$
$F_k(u, v)$	Flow of commodity k along link (u, v)
P_k	Path of flow k
sc	Service chain sc
$n(u)$	Decision variable of physical node u , showing node is OFF/IDLE/ACTIVE
e_u^N	Energy consumed by physical node u
e_c	Energy consumption cost
te_c	Total energy consumption cost
Delay, Demand and Capacity Parameters	
$C^N(u)$	Maximum capacity of the node u
$C^L(u, v)$	Capacity of the link (u, v)
$C^I(u)$	Default load of node u at IDLE state
$C_i^V(u)$	Capacity of i th VM of node u
$d_k(u, v)$	Delay faced by the flow k at link (u, v)
$d_f^{sc}(u)$	Demand of function f of service chain sc at node u
$qd_f^{sc}(u)$	Queuing delay of function f of service chain sc at node u
$d_{MAX}(u)$	Maximum delay at node u
D_k	Maximum delay that the flow can tolerate
Binary Variables	
$X_i^f(u)$	Instance i of function f mapped to node u
$Y_f^{sc}(u)$	Function f of service chain sc placed on node u

Algorithm 1: DPVC Algorithm

```
1  Input:  $A, B, ST, VM_{cap}, Total_{cost}, Idl_{max}, U_{max}, U_{idl},$   
    $vNF, pt, Idl_{time}, min_{cap}, E_c, NumFlow, boot.$   
   Algorithm:  
2   $VM = struct(VM_{flg}, VM_{fun}, VM_{exp}, VM_{wait}, VM_{flow})$   
3   $ServiceChain =$   
    $struct(source, chain, destination, FLOW_{len}, FLOW_{num})$   
4   $ChainTime = struct(startTime, pTime,$   
    $preSource, chainDest, hop, endTime)$   
5   $CurrInp = struct(chainNum, currSource, currVNF,$   
    $currDest, currFLOW_{len}, FLOW_{no}, ETime)$   
6  for each iteration  $t$   
7      $ServiceChain = ServiceChainIP(ServiceChain, t)$   
8      $ChainTime = setChainTime(CurrInp,$   
    $ServiceChain, ChainTime, t)$   
9      $CurrInp = CurrVNFinp(CurrInp,$   
    $ServiceChain, ChainTime, t)$   
10     $Placement(CurrInp, ChainTime, nodes, A, B,$   
    $ST, VM, t)$   
11    for each node  $i$  in  $ST$   
12       for each  $VM$   $j$  in node  $i$   
13          if  $t > VM_{exp}(i, j)$   
14             Release( $VM, i, j$ )  
15          end  
16       end  
17       if  $(i \in ST) \& (U_{ass}(i) == 0)$   
18           $Idl_{time}(i) = Idl_{time}(i) + 1;$   
19          if  $Idl_{time}(i) \geq Idl_{max}$   
20             Delete( $ST, i$ )  
21          end  
22       end  
23    end for  
24     $VM = updateVM(VM)$   
25     $cost = \sum_{i=1, i \in ST}^N E_c(i) \delta^{\frac{U_{idl}(i) + \sum VM_{cap}(i, j) \cdot VM_{flg}(i, j)}{U_{max}(i)}}$   
26  end for  
27  Output:  $Total_{cost} = \sum cost$ 
```

Algorithm 1.1: Placement Algorithm

```
1  Placement(CurrInp, ChainTime, nodes, A, B, ST,  
   VM, t)  
2  for  $i = 1 \rightarrow |CurrInp|$  do  
3     $s = CurrInp(i).currSource$ ;  
     $d = CurrInp(i).destination$ ;  
4     $nf = CurrInp(i).currVNF$ ;  
5     $RDFST(nodes, A, B, ST, VM_{flg}, VM_{exp}, s, d, nf, t)$   
6     $ChainTime = updateChainTime(ChainTime,$   
     $CurrInp, newNode)$   
7  end for  
8  Return:  $ST, VM, ChainTime$ 
```

Table 3: VNF placement of the service chains.

Item	Description/Value
Graph type	<i>NSFNET</i>
Service chain demand	<i>Random</i>
Flow length	10-100 Pakets
Pakets length	Equal
Type of VNFs	10l

Algorithm 1.1.1: RDFST Algorithm

```
1  RDFST(nodes, A, B, ST, VM, s, d, fun, t)  
   Index = nodeWithfun(B, fun)  
2  nodes = struct(num, CapAct, sNode, spd)  
3  nodes = assignPrioritytoNodes(nodes, VM, s, d)  
   x = totalVMInstances(VM)  
   y = x - 1;  
4  While y < x do  
5     nodessorted = nestedSortStructure(nodes, {  
       CapAct, sNode, spd})  
6     for i = 1 → |Index| do  
7         if nodessorted(i).num ≤ 0 then  
8             Display ('Error!');  
9         else  
10            nN = nodessorted(i).num;  
11            Assign(ST, nN, VM, fun, NumFlow, boot)  
12            if nN ∈ ST  
13                exit;  
14            else if Uass(nN) ≥ mincap  
15                Add(ST, nN)  
16                exit;  
17            else if max(VMwait(nN, 1),  
                VMwait(nN, 2), ... ) ≥ offtime  
18                Add(ST, nN)  
19                exit;  
20            else  
21                Display('Wait!');  
22                exit;  
23            end  
24        end  
25    end  
26    end if  
27    end for  
28    y = totalVMInstances(VM)  
29 end while  
30 Return: ST, VM, nN
```
