Statistical learning: Second assignment

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#### 0.1 Visualize dataset

In this project I use creditcard dataset The dataset contains transactions made by credit cards in September 2013 by European cardholders over a two day period. There are 492 frauds out of a total 284,807 examples. Thus, the dataset is highly unbalanced, with the positive class (frauds) accounting for only 0.172% of all transactions. You can imagine that any such dataset would be highly unbalanced, as expected fraud or anomalous cases would only make up for a small percentage of the total transactions. Let's have look at our dataset. I used seaborn and matplotlib to visualize dataset.

#### 0.1.1 Import packages and dataset

```
1 #!/usr/bin/env python3
2 # -*- coding: utf-8 -*-
  Created on Fri Dec 14 13:06:00 2018
6 @author: ali(zamanilai1995@gmail.com)
8 #%Imort packages
9 import numpy as np # linear algebra
10 import seaborn as sns
sns.set(style='whitegrid')
import pandas as pd # data processing, CSV file I/O (e.g. pd.
      read_csv)
13 import matplotlib.pyplot as plt
14 #%Check datasret
15 import os
print (os. listdir ("../dataSet"))
17 #%Read the data
print ('Loading the dataset .....')
19 credit_card = pd.read_csv('../dataSet/creditcard.csv')
print('Dataset shape: ', credit_card.shape)
print('Dataset was loaded!!!')
```

#### Output:

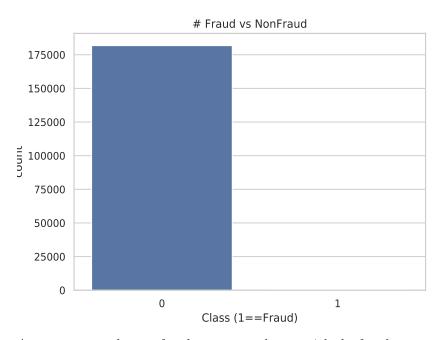
```
['creditcardfraud.rip', 'creditcard.csv', 'creditcard1.csv']
Loading the dataset....
Dataset shape: (182131, 31)
Dataset was loaded!!!
```

#### 0.1.2 Balance of Data Visualization

Let's get a visual confirmation of the unbalanced data in this fraud dataset.

```
1 #%Plot fraud vs nonfraud
2 f, ax = plt.subplots(figsize=(7, 5))
3 sns.countplot(x='Class', data=credit_card)
4 _ = plt.title('# Fraud vs NonFraud')
5 _ = plt.xlabel('Class (1==Fraud)')
6 plt.savefig("fraudvsnonfraud"+".pdf")
7 plt.show()
```

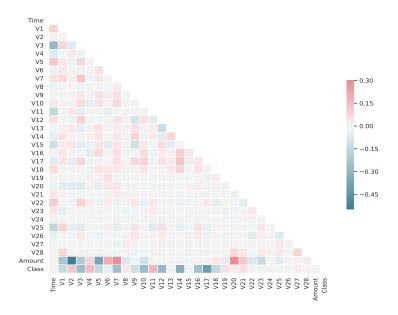
#### Output:



As you can see, the non-fraud cases strongly outweigh the fraud cases.

#### 0.1.3 Heatmap

Output:



#### 0.1.4 Fraud and non-fraud data describe

We will cut up the dataset into two data frames, one for non-fraud transactions and the other for fraud.

```
1 #%Fraud and non-fraud data describe
_{2} non_fraud = credit_card[credit_card.Class == 0]
3 fraud = credit_card [credit_card.Class == 1]
```

Let's look at some summary statistics and see if there are obvious differences between fraud and non-fraud transactions.

```
non_fraud.Amount.describe()
```

#### Output:

fraud.Amount.describe()

#### Output:

```
Count 365.000000
mean 116.533205
std 249.276178
min 0.000000
25% 1.000000
55% 11.400000
75% 104.030000
max 2125.870000
Name: Amount, dtype: float64
```

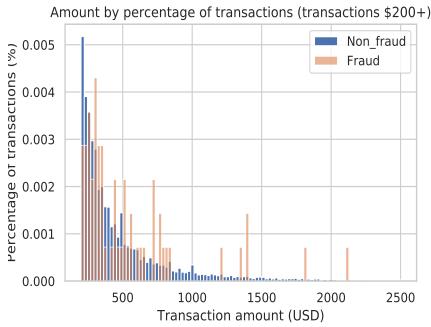
Although the mean is a little higher in the fraud transactions, it is certainly within a standard deviation and so is unlikely to be easy to discriminate in a highly precise manner between the classes with pure statistical methods. I could run statistical tests (e.g. t-test) to support the claim that the two samples likely come from populations with similar means and deviations. However, such statistical methods are not the focus of this article on autoencoders.

#### 0.1.5 Visual Exploration of the Transaction Amount Data

We are going to get more familiar with the data and try some basic visuals. In anomaly detection datasets it is common to have the areas of interest "washed out" by abundant data. The most common method is to simply 'slice and dice' the data in a couple different ways until something interesting is found. Although this practice is common, it is not a scientifically sound way to explore data. There are always non-meaningful quirks to real data, so just looking until you "find something interesting" is likely going to result in you finding false positives. In other words, you find a random pattern in the current data set that will never be seen again. As a famous economist wrote, "If you torture the data long enough, it will confess."

In this dataset, I expect a lot of low-value transactions that will be generally uninteresting (buying cups of coffee, lunches, etc). This abundant data is likely to wash out the rest of the data, so I decided to look at the data in a number different \$100 and \$1,000 intervals. Since it would be tedious to show reader these graphs, I will only show the final graph that only visualizes the transactions above \$200.

Output:

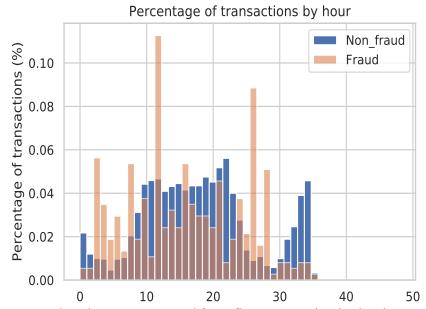


Since the fraud cases are relatively few in number compared to bin size, we see the data looks predictably more variable. In the long tail, especially, we are likely observing only a single fraud transaction. It would be hard to differentiate fraud from non-fraud transactions by transaction amount alone.

#### 0.1.6 Visual Exploration of the Data by Hour

With a few exceptions, the transaction amount does not look very informative. Let's look at the time of day next.

Output:



Fransaction time as measured from first transaction in the dataset (hour Hour "zero" corresponds to the hour the first transaction happened and not necessarily 12-1am. Given the heavy decrease in non-fraud transactions from hours 1 to 8 and again roughly at hours 24 to 32, I am assuming those time correspond to nighttime for this dataset. If this is true, fraud tends to occur at higher rates during the night. Statistical tests could be used to give evidence for this fact, but are not in the scope of this article. Again, however, the potential time offset between normal and fraud transactions is not enough to make a simple, precise classifier. Next, we will explore the potential interaction between transaction amount and hour to see if any patterns emerge.

#### 0.1.7 Visual Exploration of Transaction Amount vs. Hour

#### Output:

Again, this is not enough to make a good classifier. For example, it would be

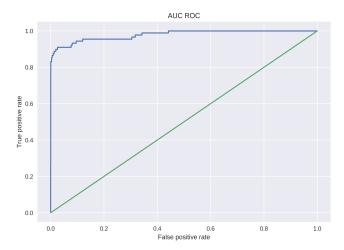
hard to draw a line that cleanly separates fraud and normal transactions. For the experienced Data Scientists in the readership, I am excluding more advanced techniques such as the kernel trick.

### 0.2 Logistic model with sklearn

```
#!/usr/bin/env python3
2 # -*- coding: utf-8 -*-
  Created on Thu Dec 6 13:10:34 2018
6 @author: ali
8 #7%
9 import numpy as np
10 import pandas as pd
from sklearn.model_selection import train_test_split
12 from sklearn.preprocessing import StandardScaler
13 from sklearn.linear_model import LogisticRegression
14 from sklearn.pipeline import Pipeline
15 from sklearn.metrics import roc_curve, roc_auc_score,
       classification_report, accuracy_score, confusion_matrix
16 import matplotlib.pyplot as plt
17 import os
print (os. listdir ("../dataSet"))
19 credit_card = pd.read_csv('../dataSet/creditcard.csv')
X = credit_card.drop(columns='Class', axis=1)
y = credit_card. Class. values
23 #%%
np.random.seed(42)
X_{train}, X_{test}, Y_{train}, Y_{test} = train_{test\_split}(X, Y)
27 scaler = StandardScaler()
28 lr = LogisticRegression()
model1.fit(X_train, y_train)
32 y_test_hat = model1.predict(X_test)
y_test_hat_probs = model1.predict_proba(X_test)[:,1]
{\tt 14test\_accuracy = accuracy\_score(y\_test, y\_test\_hat)*100}
{\tt 35 test\_auc\_roc = roc\_auc\_score(y\_test, y\_test\_hat\_probs)*100}
print('Confusion matrix:\n', confusion_matrix(y_test, y_test_hat))
print('Training accuracy: %.4f %%' % test_accuracy)
print ('Training AUC: %.4f %%' % test_auc_roc)
print(classification_report(y_test, y_test_hat, digits=6))
40 fpr, tpr, thresholds = roc_curve(y_test, y_test_hat_probs,
      drop_intermediate=True)
f, ax = plt.subplots(figsize = (9, 6))
42 _ = plt.plot(fpr, tpr, [0,1], [0, 1])
43 _ = plt.title('AUC ROC')
44 _ = plt.xlabel('False positive rate')
45 _ = plt.ylabel('True positive rate')
plt.style.use('seaborn')
```

```
48 plt.savefig('auc_roc.png', dpi=600)
49 y_hat_90 = (y_test_hat_probs > 0.90 )*1
50 print('Confusion matrix for 90%:\n', confusion_matrix(y_test, y_hat_90))
51 print('Report for 90%', classification_report(y_test, y_hat_90, digits=6))
52 y_hat_10 = (y_test_hat_probs > 0.05)*1
53 print('Confusion matrix for 5%:\n', confusion_matrix(y_test, y_hat_10))
54 print('Report for 5%', classification_report(y_test, y_hat_10, digits=4))
```

#### Results:



```
| Confusion matrix | Confusion | Confusion matrix |
```

## 0.3 Logistic model with tensorflow

```
1 #!/usr/bin/env python3
2 # -*- coding: utf-8 -*-
```

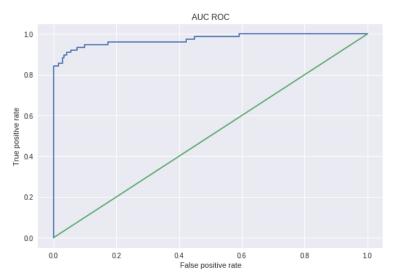
```
Created on Fri Dec 7 05:47:51 2018
6 @author: ali
8 #%Parameters
9 train_set_num = .8
seed=5
11 #% Define the learning rate batch_size etc.
learning_rate = 0.0003
batch\_size = 1000
_{14} \text{ epoch\_num} = 600
15 #%Imort packages
import numpy as np # linear algebra
import seaborn as sns
  sns.set(style='whitegrid')
  import pandas as pd # data processing, CSV file I/O (e.g. pd.
       read_csv)
20 import matplotlib.pyplot as plt
  import tensorflow as tf
21
  from sklearn.metrics import roc_curve, roc_auc_score,
       classification_report , accuracy_score , confusion_matrix
23 #% Define the normalized function
  def min_max_normalized(data):
24
       col_max = np.max(data, axis=0)
25
       col_min = np.min(data, axis=0)
       col_mean = np.mean(data, axis=0)
27
       return np. divide (data - col_mean, col_max - col_min)
28
29 #%Check datasret
30 import os
print(os.listdir("../dataSet"))
32 #%Read the data
print ('Loading the dataset....')
34 credit_card = pd.read_csv('../dataSet/creditcard.csv')
print('Dataset shape: ',credit_card.shape)
print ('Dataset was loaded!!!')
37 #%%
38 # set replace=False, Avoid double sampling
_{39} X = credit_card.drop(columns='Class', axis=1).values.reshape(-1,30)
y = credit_card.Class.values.reshape(-1,1)
{\tt train\_index} = {\tt np.random.choice}({\tt len}(X) \;,\; {\tt round}({\tt len}(X) \;*\; {\tt train\_set\_num})
                                   replace=False)
{\tt test\_index} = {\tt np.array(list(set(range(len(X))) - set(train\_index)))}
44 train_X = X[train_index
train_y = y[train_index]
test_X = X[test_index]
test_y = y[test_index]
48 #7% Normalized processing
49 train_X = min_max_normalized(train_X)
test_X = min_max_normalized(test_X)
51 #%Build the model framework
52 # Begin building the model framework
53 # Declare the variables that need to be learned and initialization
_{54} # There are 30 features here, A's dimension is (30, 1)
w = tf. Variable(tf.random_normal(shape=[30, 1]))
b = tf. Variable(tf.random\_normal(shape=[1, 1]))
```

```
init = tf.global_variables_initializer()
sess = tf. Session()
sess.run(init)
60 # Define placeholders
{\scriptstyle \text{61}}\ x = \text{tf.placeholder}\left(\,\text{dtype=tf.float32}\;,\;\; \text{shape=[None}\,,\;\;30]\,,\;\; \text{name="x"}\right)
62 y = tf.placeholder(dtype=tf.float32, shape=[None, 1], name="y")
63 # Define logistic Regression
\log it = tf.matmul(x, w) + b
y_{\text{-predicted}} = 1.0 / (1.0 + \text{tf.exp}(-\log it))
66 # Declare loss function
loss = -1 * tf.reduce_sum(y * tf.log(y_predicted) +
                                (1 - y) * tf.log(1 - y\_predicted))
69 # Define optimizer: GradientDescent
70 optimizer = tf.train.GradientDescentOptimizer(
           learning_rate=learning_rate).minimize(loss)
71
72 # Define the accuracy
73 # The default threshold is 0.5, rounded off directly
74 prediction = tf.round(tf.sigmoid(logit))
75 # Bool into float32 type
correct = tf.cast(tf.equal(prediction, y), dtype=tf.float32)
77 # Average
78 accuracy = tf.reduce_mean(correct)
79 # End of the definition of the model framework
80 #label=[tf.count_nonzero(y), tf.subtract(tf.size(y),tf.
       count_nonzero(y))]
   \#confusion\_matrix\_tf = tf.confusion\_matrix(labels = [10, 100],
                                                   predictions = [2, 108]
  #
82
83 #FN=tf.metrics.false_negatives(labels=y, predictions=tf.round(
       y_predicted))
sa confiution=np.zeros(shape=[2,2])
86 print ("Parameters were initialized, Session is runing ...")
87 train_error_list = []
train_acc_list = []
test_acc_list = []
   test_error_list = []
   with tf. Session() as sess:
91
92
       sess.run(tf.global_variables_initializer())
93
        for epoch in range (epoch_num):
94
            train_loss = 0
            for idx in range(len(train_X)//batch_size):
95
                input\_list = \{x: train\_X [idx*batch\_size:(idx+1)*
96
       batch_size],
                               y: train_y[idx*batch_size:(idx+1)*
97
       batch_size ] }
                   train_loss1 = sess.run([optimizer, loss], feed_dict=
98
       input_list)
                train_loss += train_loss1
            train_error_list.append(train_loss/len(train_X))
100
            train_acc_list.append(sess.run(
101
                     \label{eq:curacy} \verb|accuracy|, feed_dict= \{x: train_X, y:
                         train_y }) *100)
104
            test_acc_list.append(sess.run(accuracy
                                             , feed\_dict=\{x: test\_X,
106
                                                           y: test_y)
       *100)
            test_error_list.append(sess.run(loss,
```

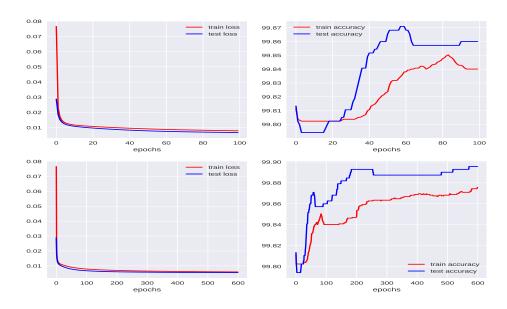
```
feed_dict={x: test_X,
108
                                                       y: test_y \})/len(
109
       test_y))
           if (epoch + 1) \% 50 = 0:
110
                print('epoch: {:4d} loss: {:5f} train_acc: {:5f}%
       test_acc: \{:5f\}\%
                      .format(epoch + 1, train_loss/len(train_X),
                              train_acc_list[epoch], test_acc_list[
113
       epoch]))
114
       w_{value}, b_{value} = sess.run([w, b])
       for i in range(len(train_X)):
           logit1 = np.matmul(train_X[i], w_value) + b_value
116
           if (np.round(1.0 / (1.0 + np.exp(-logit1)))):
117
118 #
            if (sess.run(tf.round(y_predicted), feed_dict={x:train_X[i
       ]})):
                if train_y[i]:
119
120
                   confiution [1,1]+=1
                else:
121
                    confiution[0,1]+=1
122
           else:
123
                if train_y[i]:
124
                    confiution[1,0]+=1
                else:
127
                    confiution[0,0]+=1
       print ('Confution matrix:', confiution)
128
   #%%
129
   train_y-hat=np.round(1.0/(1.0 + np.exp(-(np.matmul(train_X,w_value))))
130
       +b_value))))
   test_y hat = np.round(1.0/(1.0 + np.exp(-(np.matmul(test_X, w_value) +
131
       b_value))))
   test_accuracy = accuracy_score(test_y, test_y_hat)*100
   test\_auc\_roc \ = \ roc\_auc\_score \, (\, test\_y \,\, , \ test\_y\_hat \,) *100
  print('Confusion matrix for train data:\n', confusion_matrix(test_y
134
       test_y_hat))
  print('Confusion matrix for test data:\n', confusion_matrix(train_y
136
       train_y_hat))
   print('Training accuracy: ', test_accuracy)
   print('Training AUC: ', test_auc_roc)
139
   print(classification_report(test_y, test_y_hat, digits=6))
fpr, tpr, thresholds = roc\_curve(test\_y, 1.0/(1.0 + np.exp(-(np. model))))
       matmul(test_X, w_value)+b_value)))
                                        drop_intermediate=True)
142
#select_tereshold=np.zeros_like(thresholds)
\#recall=tpr/(tpr+fpr)
145 #precision=
  \#select_tereshold = 2*(tpr*fpr)/(tpr+fpr)
#select_tereshold.append
f, ax = plt.subplots(figsize=(9, 6))
_ = plt.xlabel('False positive rate')
152 _ = plt.ylabel('True positive rate')
plt.style.use('seaborn')
```

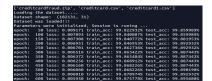
```
plt.savefig('auc_roc.png', dpi=600)
  test_y-hat_10 = (1.0/(1.0 + np.exp(-(np.matmul(test_X, w_value)+
       b_{value}))) > 0.05)*1
   train_y hat_10 = (1.0/(1.0 + np.exp(-(np.matmul(train_X, w_value) +
       b_value))) > 0.05)*1
  test_accuracy_10 = accuracy_score(test_y, test_y_hat_10)*100
157
   test\_auc\_roc\_10 = roc\_auc\_score(test\_y, test\_y\_hat\_10)*100
  print ('Confusion matrix for train data (0.05):\n', confusion_matrix
       (test_y,
160
       test_y_hat_10)
   print('Confusion matrix for test data(0.05):\n', confusion_matrix(
       train_y ,
       train_y_hat_10))
  print('Training accuracy (0.05): ',test_accuracy_10)
print('Training AUC (0.05): ', test_auc_roc_10)
163
print(classification_report(test_y, test_y_hat_10, digits=6))
166 #%%
fig, ax = plt.subplots(2, 2, figsize=(10, 10))
  fig.suptitle("test accuracy = " + str(test_acc_list[epoch]))
for a in ax.reshape(-1,1):
       a[0]. set_xlabel("epochs")
170
  ax[0][0].plot(train_error_list[:100], color='red', label='train
       loss')
  ax[0][0].plot(test_error_list[:100], color='blue', label='test loss
173 ax [0][0]. legend()
ax[1][0].plot(train_error_list, color='red', label='train loss')
  ax[1][0]. plot(test_error_list, color='blue', label='test loss')
  ax [1] [0]. legend()
ax [0][1]. plot(train_acc_list[:100], color='red', label='train
       accuracy')
ax[0][1].plot(test_acc_list[:100], color='blue', label='test
       accuracy')
  ax [0][1]. legend()
ax[1][1].plot(train_acc_list, color='red', label='train accuracy')
ax[1][1].plot(test_acc_list, color='blue', label='test accuracy')
ax [1][1].legend()
plt.savefig("trainandtest"+".pdf")
184 #End main program
```

Results:



test accuracy = 99.89567995071411





## 0.4 compare sklearn and tensorflow results for logistic model

Accuracy model of sklearn and tensorflow are 99.9% and 99.89% but we know because of unbalance data, accuracy is not suitable criteria hence we compare recall(percentage of one data is fraud and our model predict it fraud) and precision(percentage of one data is non-fraud and our model predicts it non-fraud) and f1-score(recall and precision) of two packages.

Recall:

sklearn:82%

tensorflow:84%

Precision:

sklearn:76%

tensorflow:85%

F1-score:

sklearn:79%

tensorflow:85%

We see that tensorflow predict better.

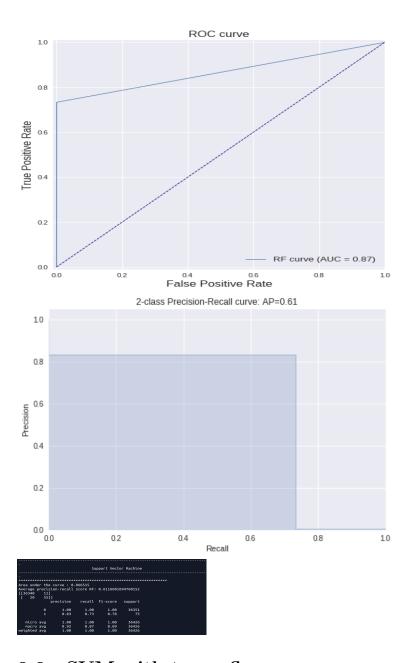
#### 0.5 SVM with sklearn

```
1 #%Parameters
2 train_set_num = .8
₃ seed=5
4 #%Imort packages
5 import numpy as np # linear algebra
  import pandas as pd # data processing, CSV file I/O (e.g. pd.
      read_csv)
  import matplotlib.pyplot as plt
  from sklearn import svm
9 from sklearn.svm import SVC
10 from sklearn.metrics import classification_report
11 from sklearn.metrics import confusion_matrix
12 from sklearn.metrics import fl_score
13 from sklearn.metrics import accuracy_score
14 from sklearn.metrics import recall_score
15 from sklearn.metrics import precision_score, precision_recall_curve
```

```
16 from sklearn.metrics import roc_auc_score, roc_curve, auc,
       average_precision_score
17 from sklearn.preprocessing import StandardScaler
18 from sklearn.model_selection import train_test_split
19 from mlxtend.plotting import plot_confusion_matrix
20 import seaborn as sns
  import warnings
warnings.filterwarnings('ignore')
24 #% Define the normalized function
25
  def min_max_normalized(data):
26
       col_{max} = np.max(data, axis=0)
       col_min = np.min(data, axis=0)
27
       col_mean = np.mean(data, axis=0)
       return np. divide (data - col_min, col_max - col_min)
29
30 #%Check datasret
31 import os
print(os.listdir("../dataSet"))
33 #%Read the data
print('Loading the dataset.....')
credit_card = pd.read_csv('.../dataSet/creditcard.csv')
print('Dataset shape: ', credit_card.shape)
print('Dataset was loaded!!!')
38 #%%
39 # set replace=False, Avoid double sampling
40 X = credit_card.drop(columns='Class', axis=1).values.reshape(-1,30)
y = credit_card.Class.values.reshape(-1,1)
42 train_index = np.random.choice(len(X), round(len(X) * train_set_num
                                   replace=False)
43
44 test_index = np.array(list(set(range(len(X))) - set(train_index)))
45 train_X = X[train_index]
46 train_y = y[train_index]
test_X = X[test_index]
48 \text{ test_y} = y[\text{test_index}]
49 #% Normalized processing
train_X = min_max_normalized(train_X)
51 test_X = min_max_normalized(test_X)
52 #%%
53 # Applying SVM Algorithm
54 print ("
55 print ("
                                            Support Vector Machine
                               ")
56 print ("-
57
58 #Using the rbf kernel to build the initail model.
59 classifier= svm.SVC(C= 1, kernel= 'linear', random_state= 0)
61 #Fit into Model
  classifier.fit(train_X, train_y)
64 #Predict the class using X_test
65 y_pred = classifier.predict(test_X)
66
con_mat = confusion_matrix(test_y, y_pred)
average_precision = average_precision_score(test_y, y_pred)
69 cls_report = classification_report(test_y, y_pred)
```

```
70
71 print ("
72 print("Area under the curve : %f" % (roc_auc_score(test_y, y_pred))
   print("Average precision-recall score RF: {}".format(
       average_precision))
74 print (con_mat)
75 print (cls_report)
76 print ('
77 #%%
78 precision, recall, _ = precision_recall_curve(test_y, y_pred)
79 plt.step(recall, precision, color='b', alpha=0.2, where='post')
80 plt.fill_between(recall, precision, step='post', alpha=0.2, color='
       b')
81
plt.xlabel('Recall')
plt.ylabel('Precision')
84 plt.ylim([0.0, 1.05])
85 plt.xlim([0.0, 1.0])
plt.title('2-class Precision-Recall curve: AP = \{0:0.2f\}'.format(
       average_precision))
ss fpr_rf, tpr_rf, _= roc_curve(test_y, y_pred)
89 roc_auc_rf = auc(fpr_rf, tpr_rf)
plt.figure(figsize = (8,8))
91 plt.xlim([-0.01, 1.00])
92 plt.ylim([-0.01, 1.01])
93 plt.plot(fpr_rf, tpr_rf, lw=1, label='{} curve (AUC = {:0.2 f})'.
       format('RF', roc_auc_rf))
94
plt.xlabel('False Positive Rate', fontsize=16)
plt.ylabel('True Positive Rate', fontsize=16)
plt.title('ROC curve', fontsize=16)
98 plt.legend(loc='lower right', fontsize=13)
99 plt.plot([0, 1], [0, 1], color='navy', lw=1, linestyle='--')
plt.axes().set_aspect('equal')
101 plt.show()
```

Results:



## 0.6 SVM with tensorflow

# 0.7 Compare sklearn and tensorflow results for ${\rm SVM}$