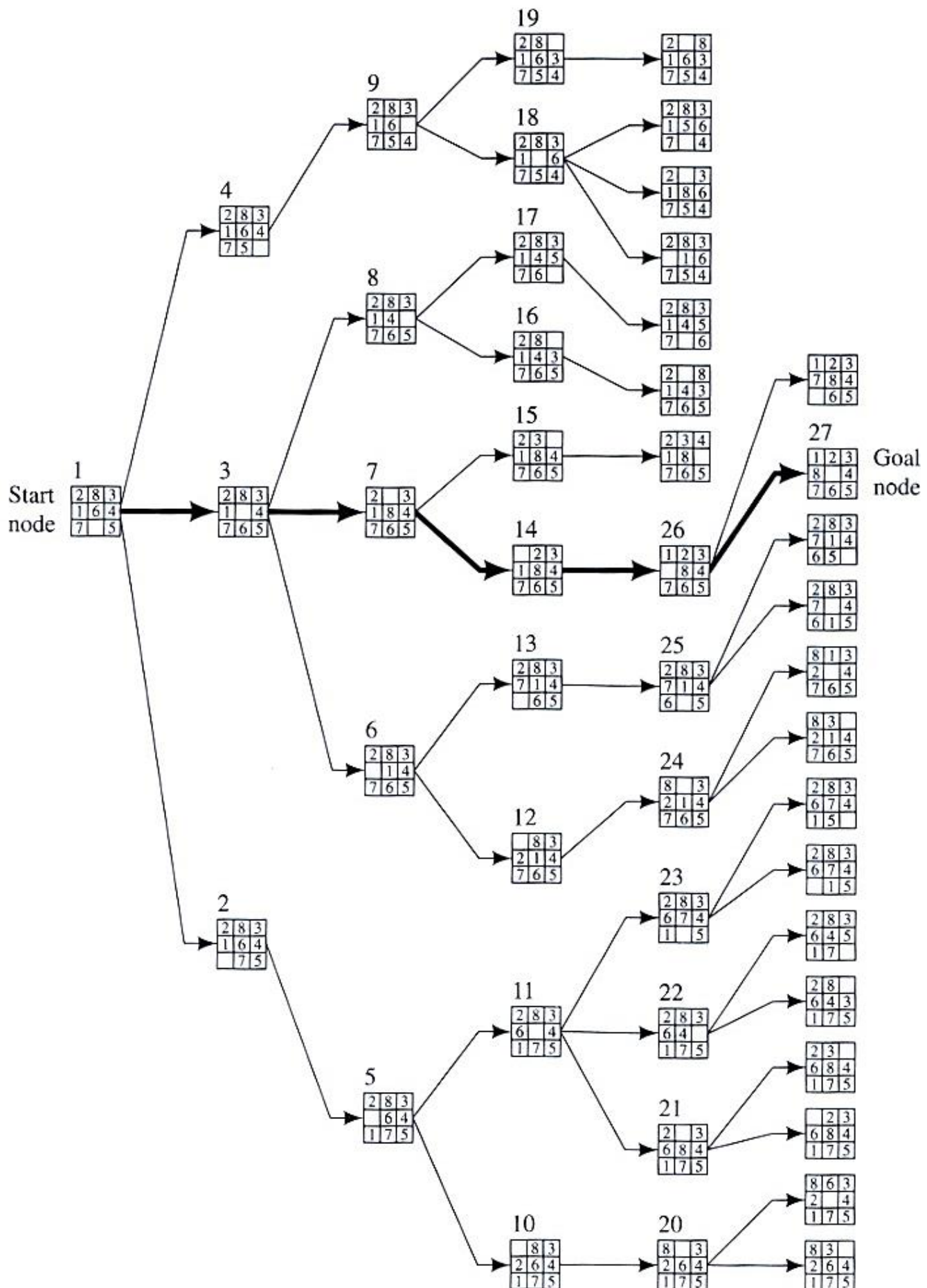


Search – The process of looking for a sequence of actions (i.e. solution) that reaches the goal state.

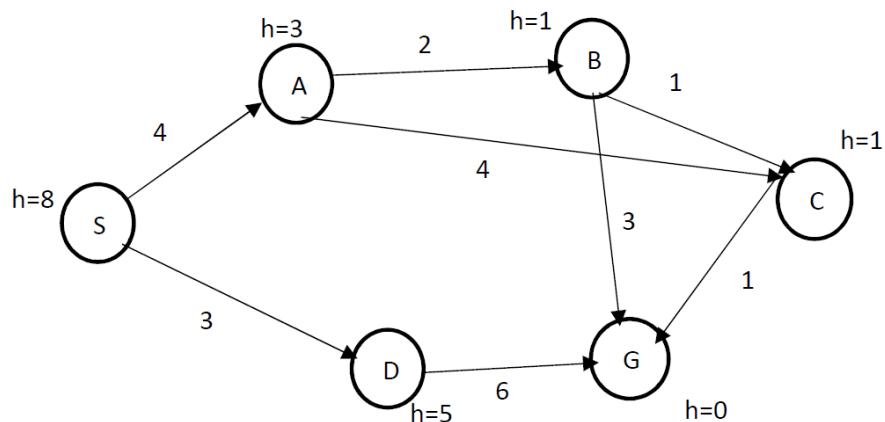


Search Strategy:

- 1) **Uninformed/Blind Search:** It has *no additional information* about the states beyond the problem definition.
 - Breadth-first search (BFS)
 - Uniform-cost search (UCS)
 - Depth-first search (DFS)
 - Depth-limited search (DLS)
 - Iterative deepening depth-first search (ID DFS)
 - Bidirectional search etc.

Uniform-cost search (UCS) – evaluation function, $f(n) = g(n) = \text{cost to reach node } n \text{ from root}$

- Expands the node with the lowest path cost, $g(n)$.
- Goal test is applied to a node when it is selected for expansion.
- Extra checkpoint is added in case a better path is found to a node currently on the queue (frontier).



Step 1: (Initialization)

$E = \{ \}$

$Q = \{ (S, 0, \text{NIL}) \}$

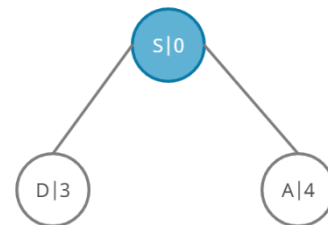


Step 2:

popped_node = (S, 0, NIL) != Goal, G

$E = \{ (S, 0, \text{NIL}) \}$

$Q = \{ (D, 3, S), (A, 4, S) \}$

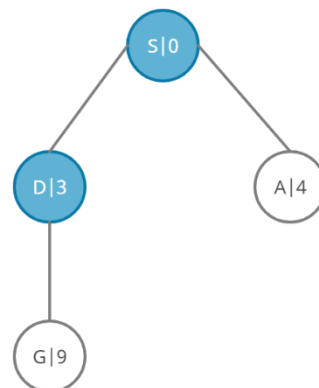


Step 3:

popped_node = (D, 3, S) != Goal, G

$E = \{ (S, 0, \text{NIL}), (D, 3, S) \}$

$Q = \{ (A, 4, S), (G, 9, D) \}$

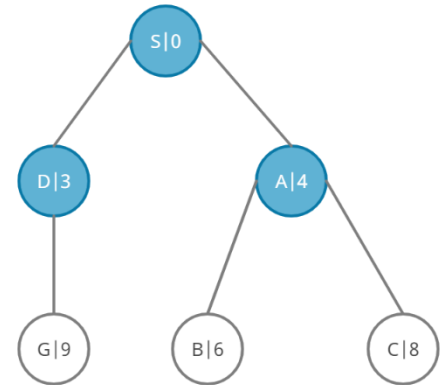


Step 4:

popped_node = (A, 4, S) != Goal, G

E = { (S, 0, NIL), (D, 3, S), (A, 4, S) }

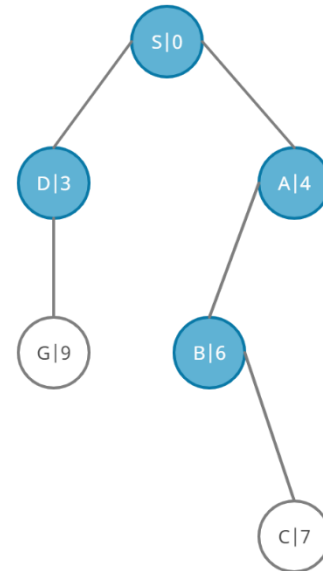
Q = { (B, 6, A), (C, 8, A), (G, 9, D) }

**Step 5:**

popped_node = (B, 6, A) != Goal, G

E = { (S, 0, NIL), (D, 3, S), (A, 4, S), (B, 6, A) }

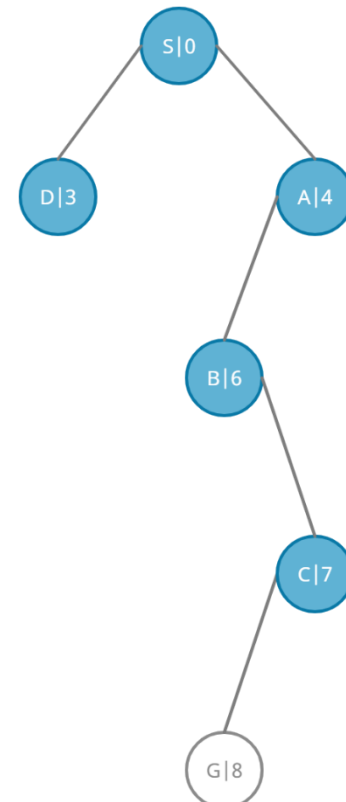
Q = { (C, 7, B), (G, 9, D) }

**Step 6:**

popped_node = (C, 7, B) != Goal, G

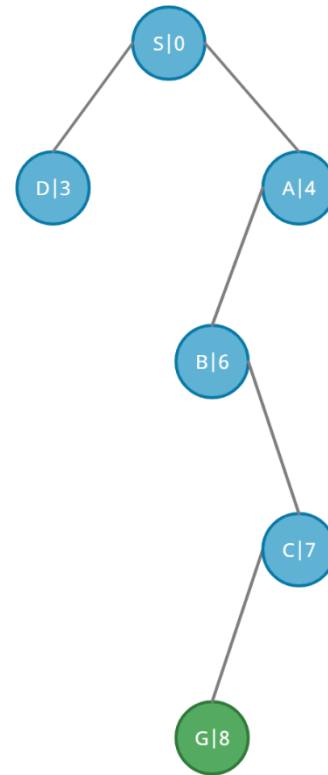
E = { (S, 0, NIL), (D, 3, S), (A, 4, S), (B, 6, A), (C, 7, B) }

Q = { (G, 8, C) }



Step 7:

popped_node = (G, 8, C) = Goal, G (**STOP**)



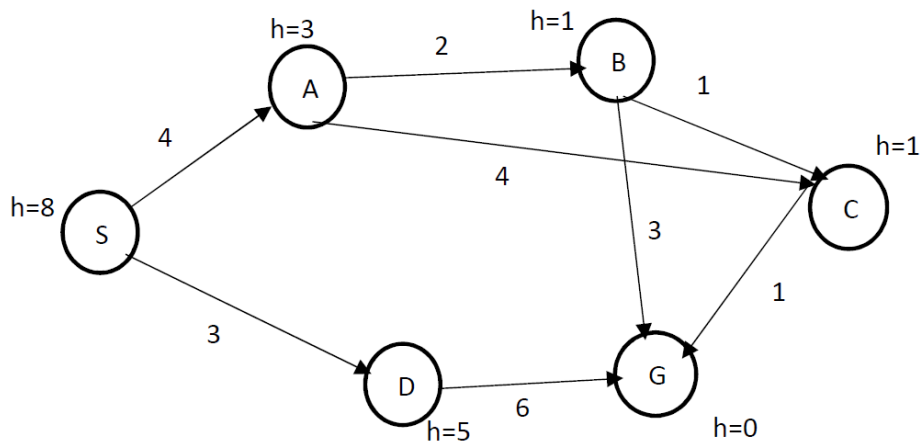
Optimal Path: (G, 8, C) \leftarrow (C, 7, B) \leftarrow (B, 6, A) \leftarrow (A, 4, S) \leftarrow (S, 0, NIL)

2) **Informed/Heuristic Search:** It uses *problem-specific knowledge* beyond the definition of the problem itself.

- Greedy best-first search
- A* search

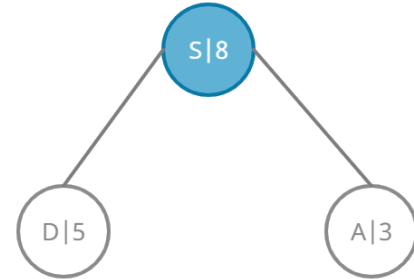
Greedy best-first search – evaluation function $f(n) = h(n)$ = estimated cost of the cheapest path from n to G

- Tries to expand the node that is closest to the goal.
- Identical to UCS except it evaluates nodes by using the heuristic function, $h(n)$. Heuristic functions are the most common form in which additional knowledge of the problem is imparted to the search algorithm.
- Final solution can be optimal or not.

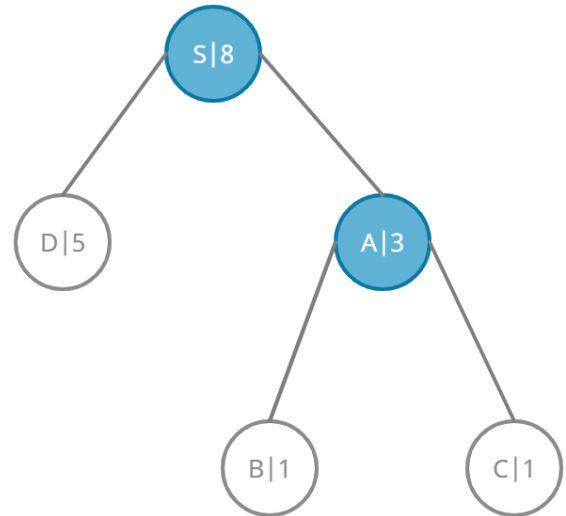


Step 1: (Initialization) $E = \{ \}$ $Q = \{ (S, 8, NIL) \}$ **Step 2:**

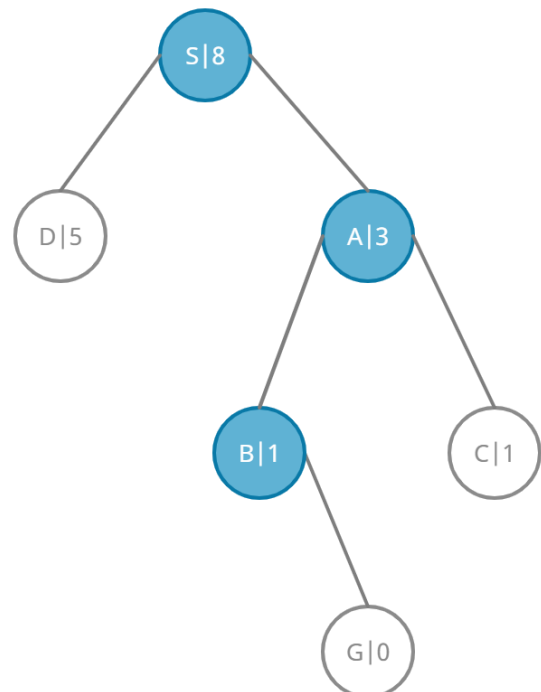
popped_node = (S, 8, NIL) != Goal, G

 $E = \{ (S, 8, NIL) \}$ $Q = \{ (A, 3, S), (D, 5, S) \}$ **Step 3:**

popped_node = (A, 3, S) != Goal, G

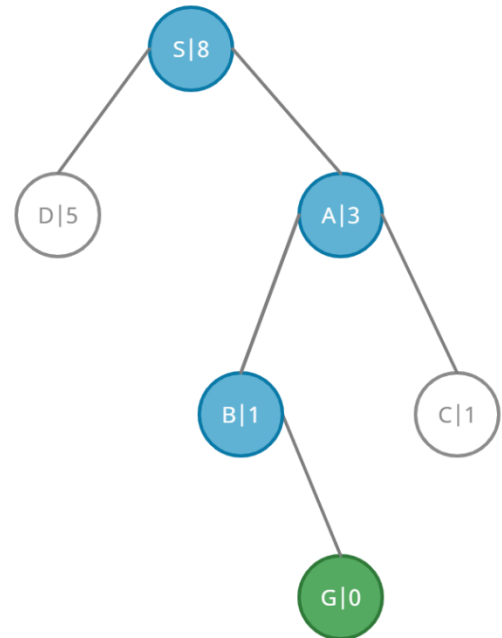
 $E = \{ (S, 8, NIL), (A, 3, S) \}$ $Q = \{ (B, 1, A), (C, 1, A), (D, 5, S) \}$ **Step 4:**

popped_node = (B, 1, A) != Goal, G

 $E = \{ (S, 8, NIL), (A, 3, S), (B, 1, A) \}$ $Q = \{ (G, 0, B), (C, 1, A), (D, 5, S) \}$ 

Step 5:

popped_node = (G, 0, B) = Goal, G (STOP)



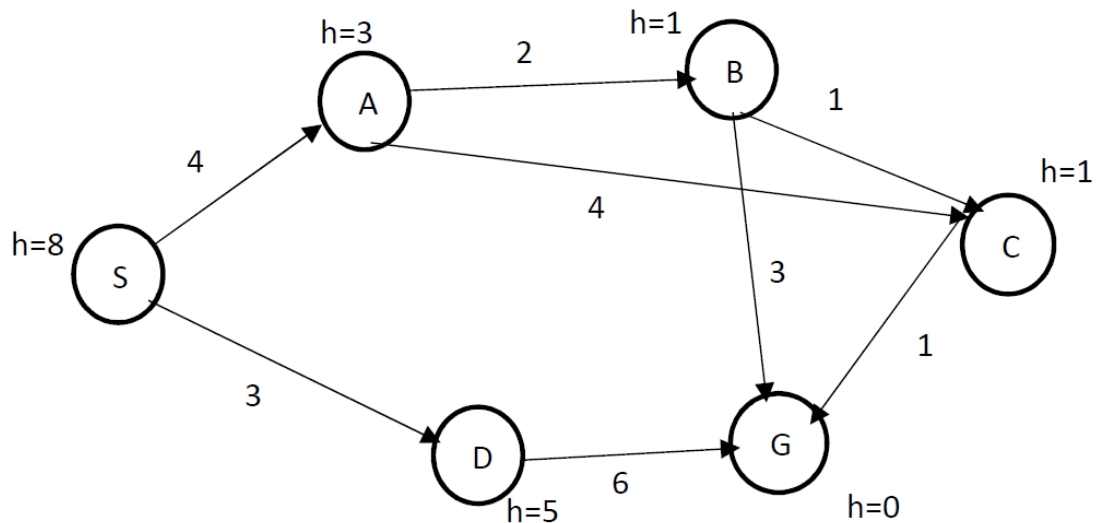
Sub-optimal Path: (G, 0, B) \leftarrow (B, 1, A) \leftarrow (A, 3, S) \leftarrow (S, 8, NIL)

A* Search - evaluation function, $f(n) = g(n) + h(n)$

= actual cost to reach node n from the root

+ estimated cost of the cheapest path from node n to goal G

- Evaluates nodes by combining the actual cost to reach the node, $g(n)$ and the estimated cost to reach the goal from the node, $h(n)$
- Identical to UCS except it uses $g(n) + h(n)$ instead of $g(n)$.
- Optimality condition:
 - For tree search, $h(n)$ needs to be admissible i.e. $h(n) \leq$ true minimum cost from n to goal, $h^*(n)$
 - For graph search, $h(n)$ needs to be consistent i.e. $h(n) \leq c(n, a, n') + h(n')$, n' a successor or n.

**Step 1: (Initialization)**

$E = \{ \}$

$Q = \{ (S, t=8, a=0, NIL) \}$

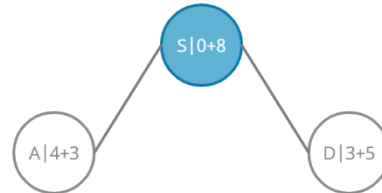


Step 2:

popped_value = (S, t=8, a=0, NIL)

E = { (S, t=8, a=0, NIL) }

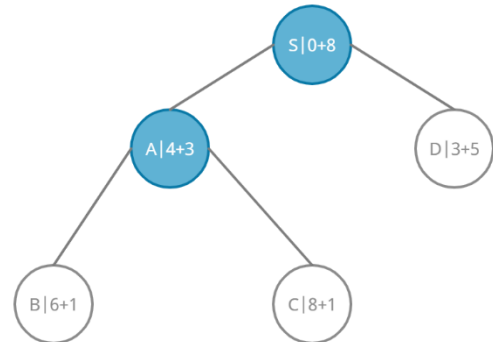
Q = { (A, t=7, a=4, S), (D, t=8, a=3, S) }

**Step 3:**

popped_value = (A, t=7, a=4, S)

E = { (S, t=8, a=0, NIL), (A, t=7, a=4, S) }

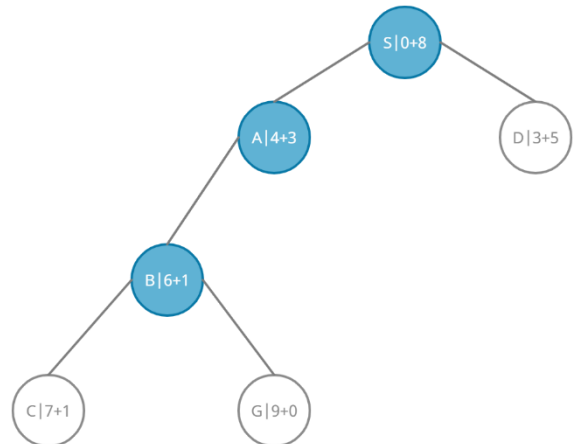
Q = { (B, t=7, a=6, A), (D, t=8, a=3, S), (C, t=9, a=8, A) }

**Step 4:**

popped_value = (B, t=7, a=6, A)

E = { (S, t=8, a=0, NIL), (A, t=7, a=4, S), (B, t=7, a=6, A) }

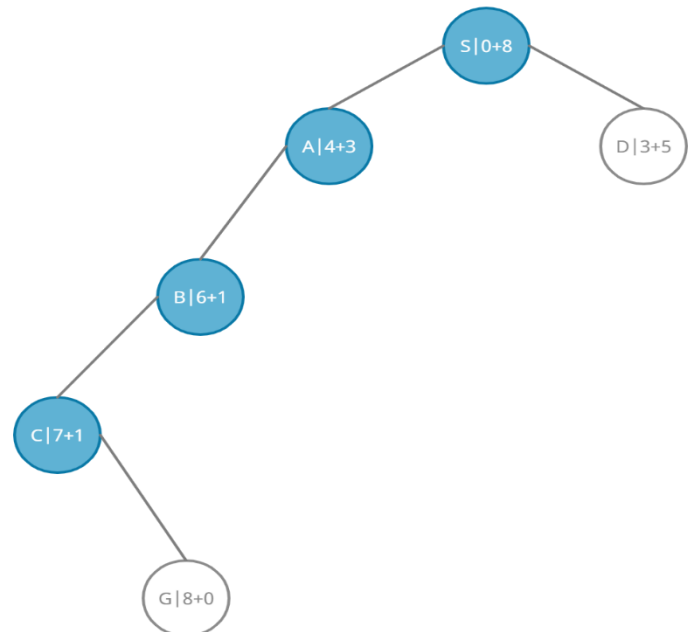
Q = { (C, t=8, a=7, B), (D, t=8, a=3, S), (G, t=9, a=9, B) }

**Step 5:**

popped_value = (C, t=8, a=7, B)

E = { (S, t=8, a=0, NIL), (A, t=7, a=4, S),
(B, t=7, a=6, A), (C, t=8, a=7, B) }

Q = { (D, t=8, a=3, S), (G, t=8, a=8, C) }

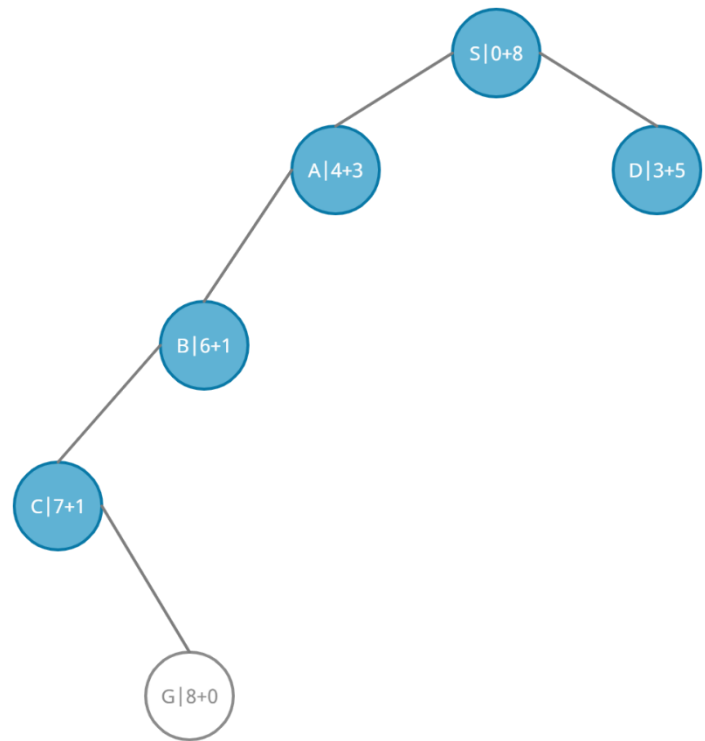


Step 6:

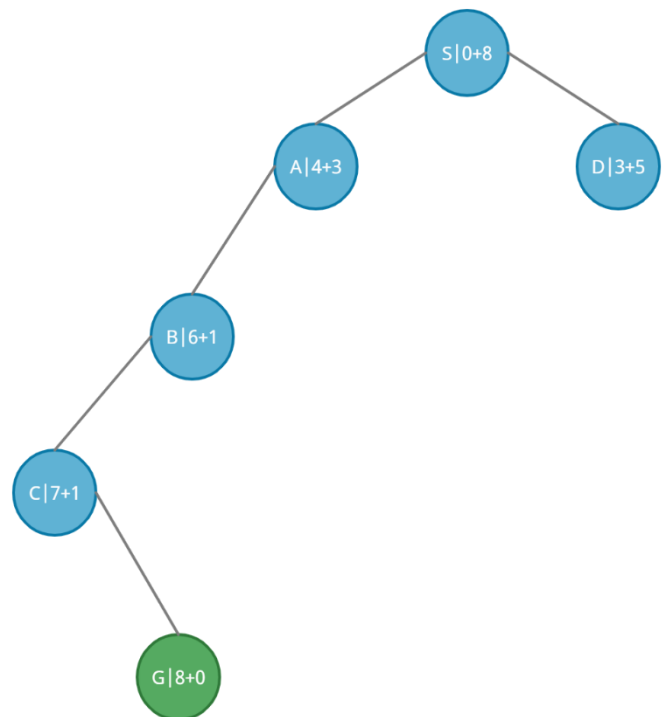
popped_value = (D, t=8, a=3, S)

E = { (S, t=8, a=0, NIL), (A, t=7, a=4, S),
(B, t=7, a=6, A), (C, t=8, a=7, B),
(D, t=8, a=3, S) }

Q = { (G, t=8, a=8, C) } **#no change**

**Step 7:**

popped_value = (G, t=8, a=8, C) = Goal, G (STOP)



Optimal Path: (G, t=8, a=8, C) \leftarrow (C, t=8, a=7, B) \leftarrow (B, t=7, a=6, A) \leftarrow (A, t=7, a=4, S) \leftarrow (S, t=8, a=0, NIL)