

Lab 4

To Simplify Boolean Expressions and Implement Respective Digital Circuits Using Karnaugh Map

Note: For examples, refer to the following link: <https://www.geeksforgeeks.org/introduction-of-k-map-karnaugh-map>

Tasks

1. **Construct K-Map for the function given below. Show the simplified output expression and verify the output with the help of software simulation.**

$$Z = f(A,B) = \bar{A}\bar{B} + A\bar{B} + \bar{A}B$$

K-Map

Q no 1

Construct K-maping table

$$Z = f(A, B) = \bar{A}\bar{B} + A\bar{B} + \bar{A}C$$

K-Map

		B	
A	0	0	1
	0	$\bar{A}\bar{B}$	$\bar{A}B$
1	0	$A\bar{B}$	

Group # 1

Group # 2

$$\text{Group 1} = A$$

$$\text{Group 2} = B$$

So, $F = A + B$

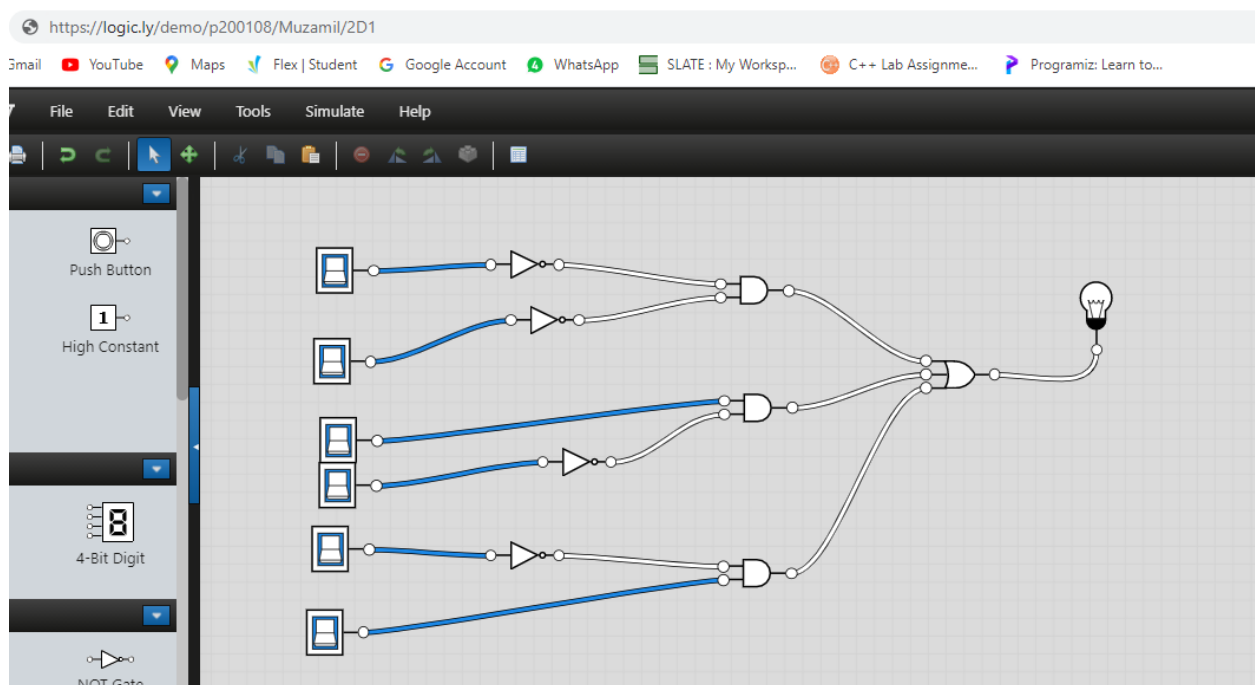
Simplified Output Function

$$F=A+B$$

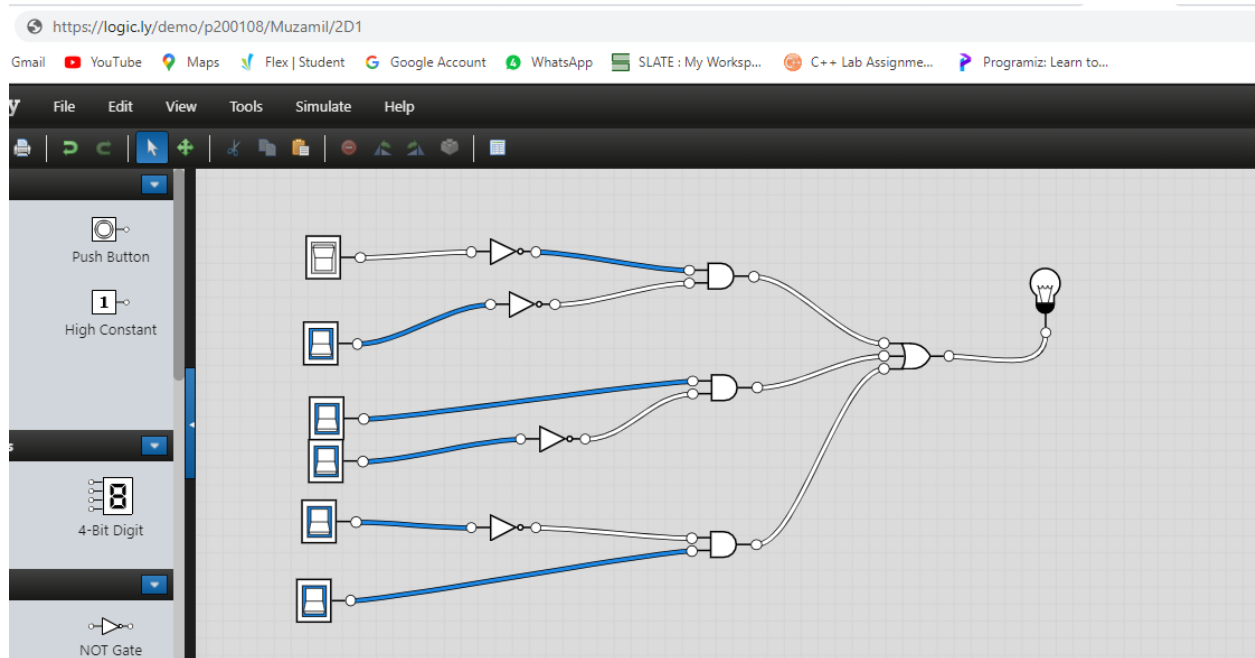
Software Simulation of Logic Circuit From Simplified Function

(Show here your results for each combination)

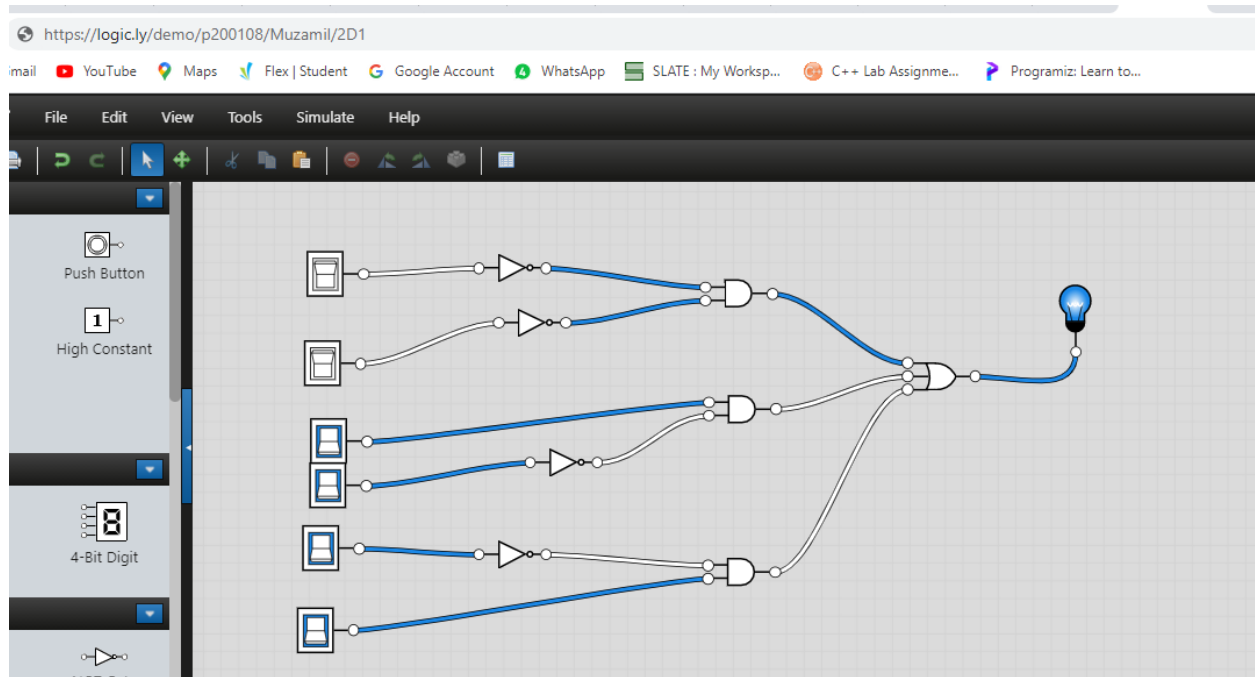
inPUts are 111111 and output is 0



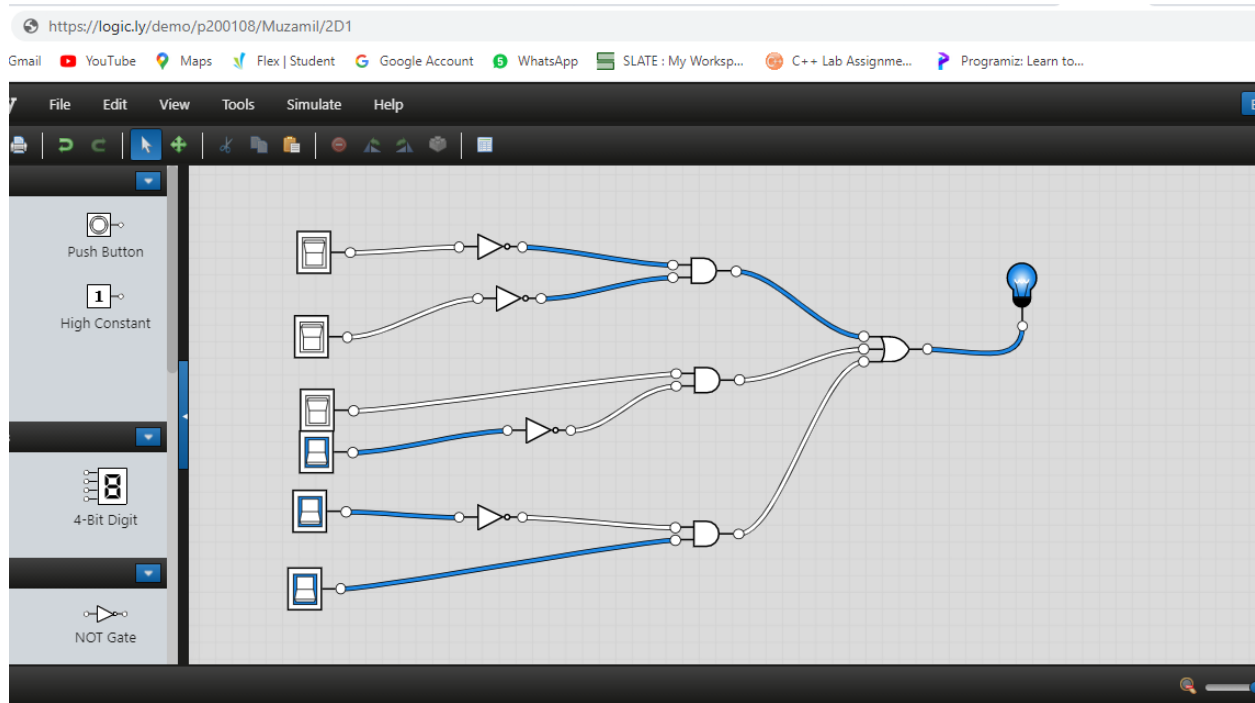
Inputs are 011111 and output is 0



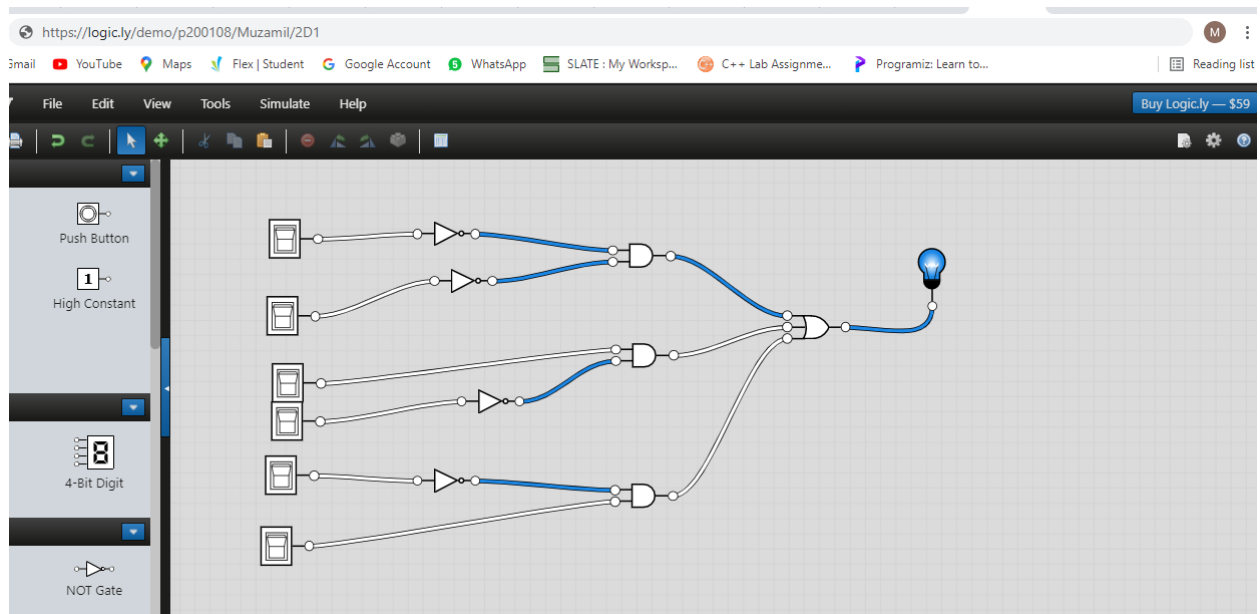
Inputs are 001111 and output is 1



Inputs are 000111 and output is 1



Inputs are 000000 and output is 1



2. Minimize the following function using K-Map. Verify the output expression with the help of simulation.

$$f(a,b,c,d) = \sum m(3,7,11,12,13,14,15)$$

K-Map

Question # 2

$$f(a, b, c, d) = \sum m(3, 7, 11, 12, 13, 14, 15)$$

		CD			
		00	01	11	10
AB	00			1	
	01			1	
	11	1	1	1	1
	10			1	

group II

group I

$$F = AB + CD$$

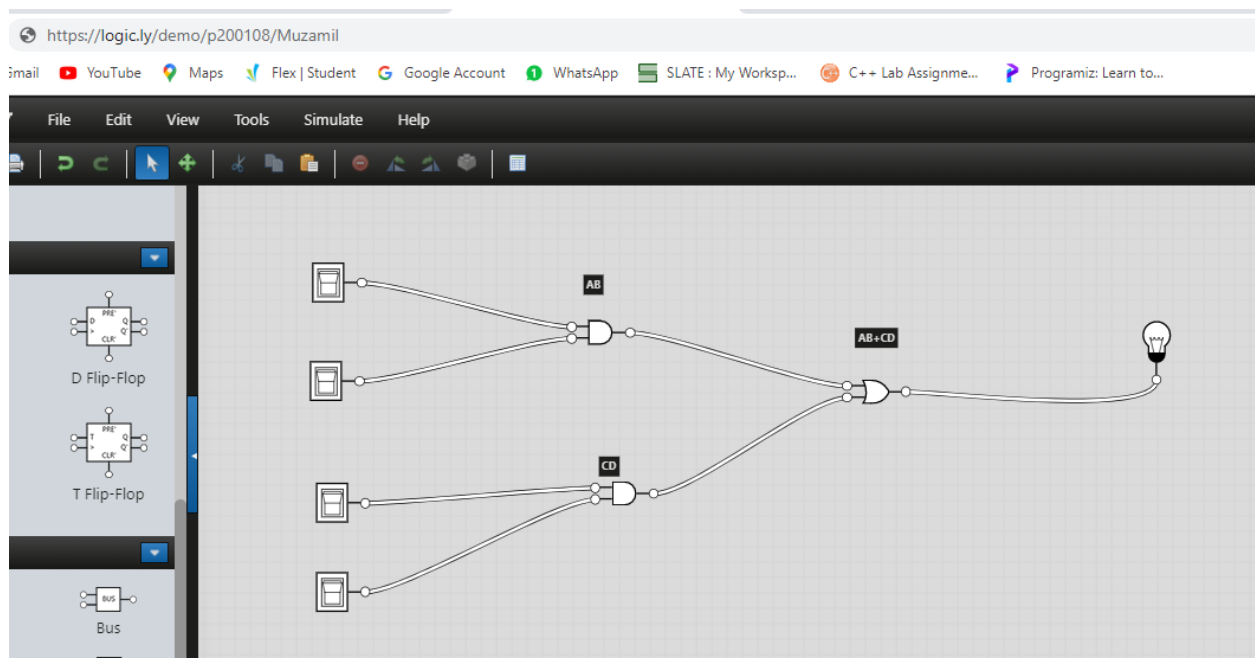
$$F = \bar{A}\bar{B}CD + \bar{A}B\bar{C}D + A\bar{B}CD + AB\bar{C}D + ABC\bar{D} + ABCD$$

Simplified Output Function

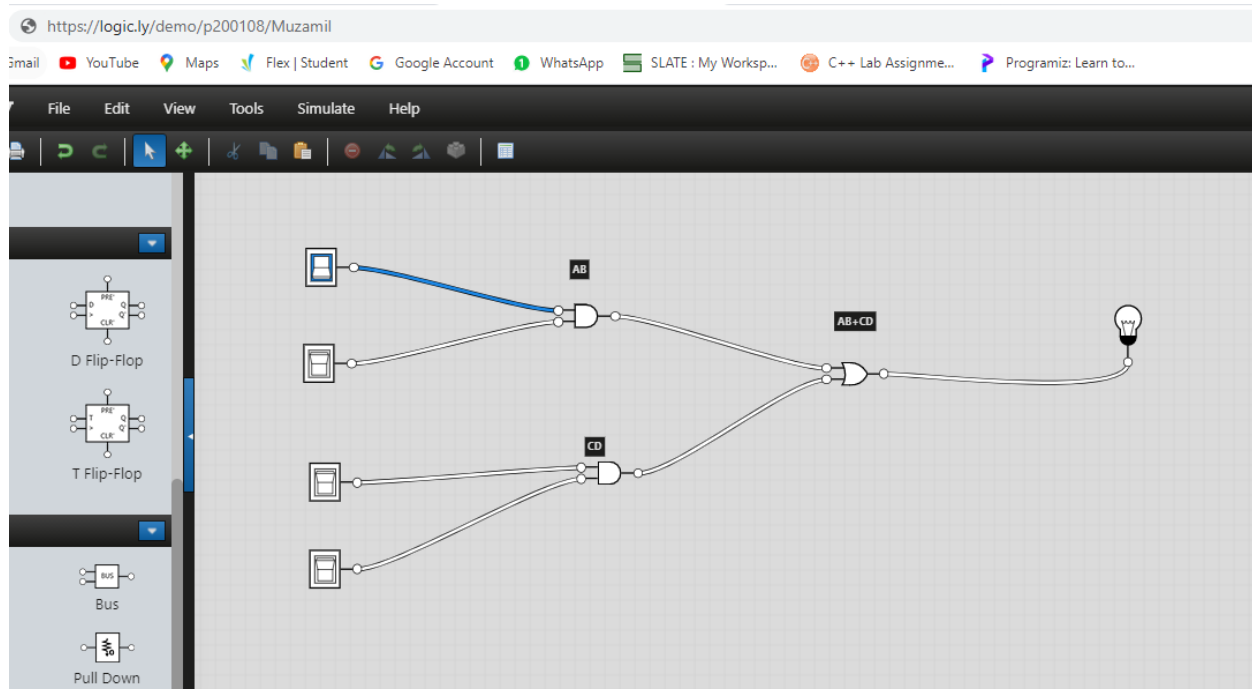
$$F = AB + CD$$

Software Simulation of Logic Circuit From Simplified Function

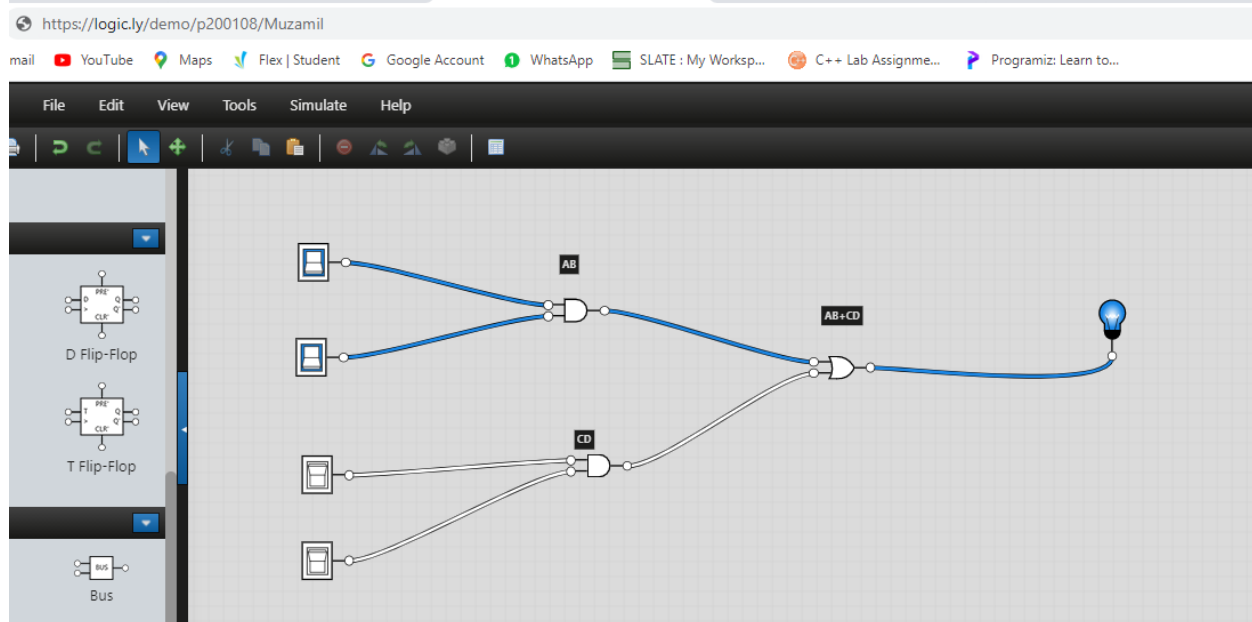
Inputs are 0000 and output is 0



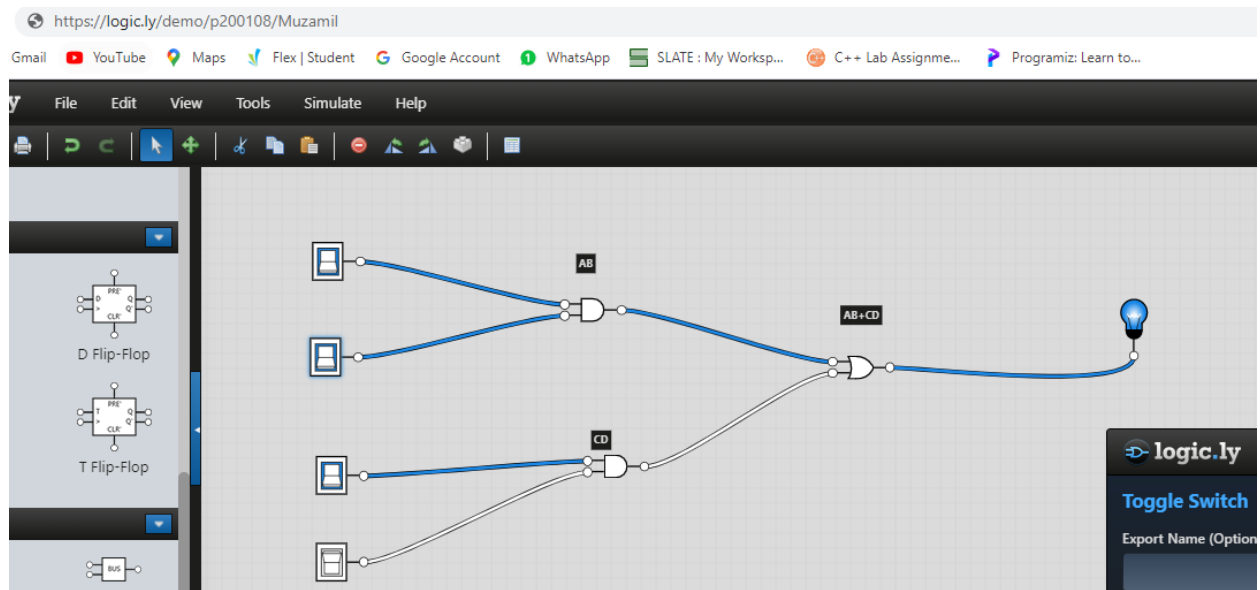
Inputs are 1000 and output is 0



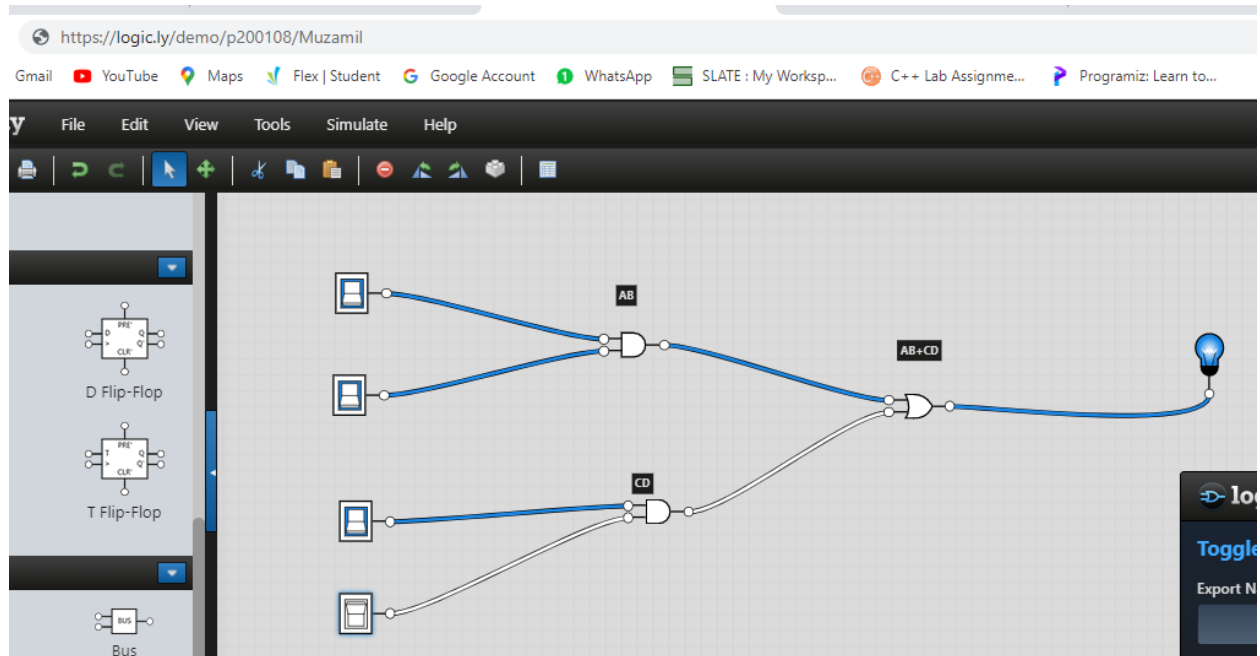
Inputs are 1100 and output is 1



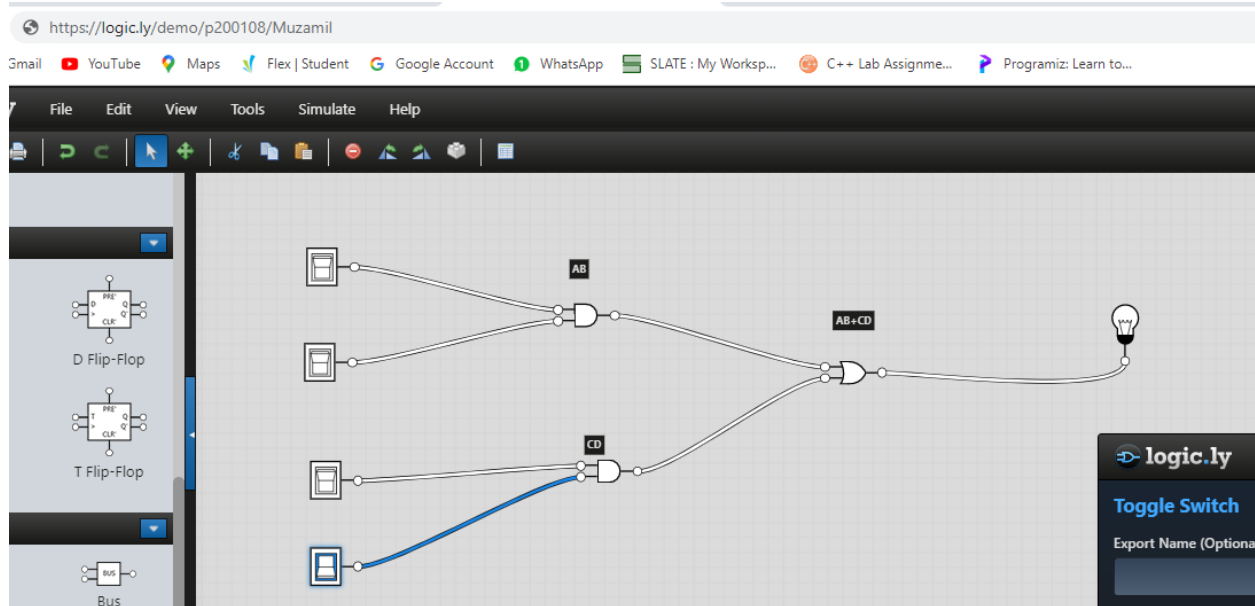
Inputs are 1110 and output is 1



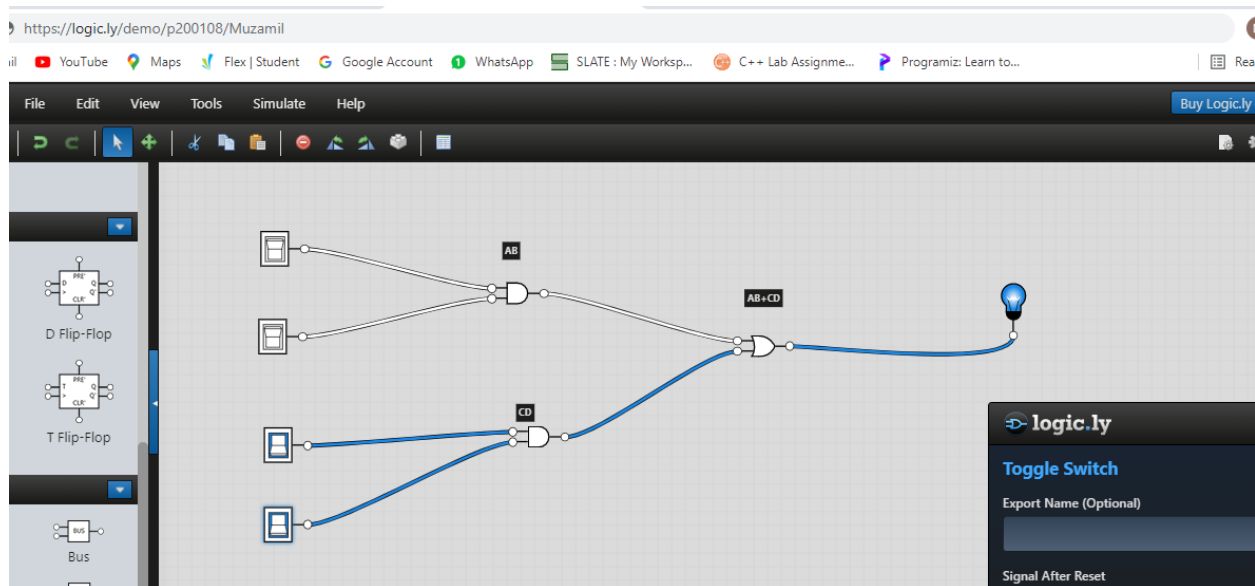
Inputs are 1111 and output is 1



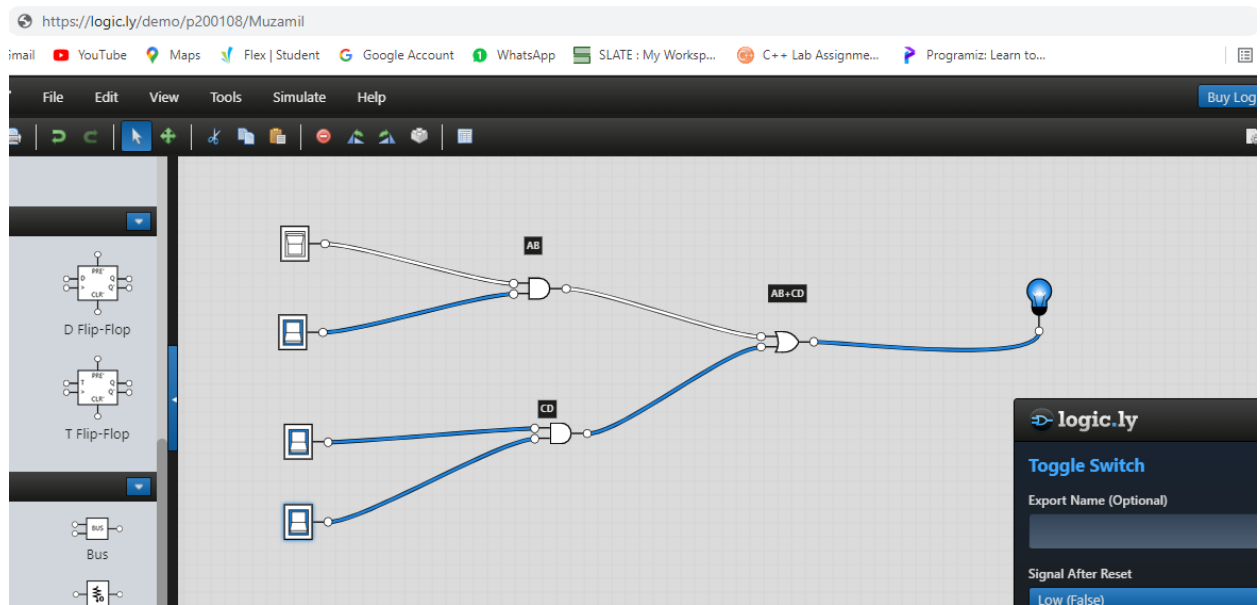
Inputs are 0001 and output is 0



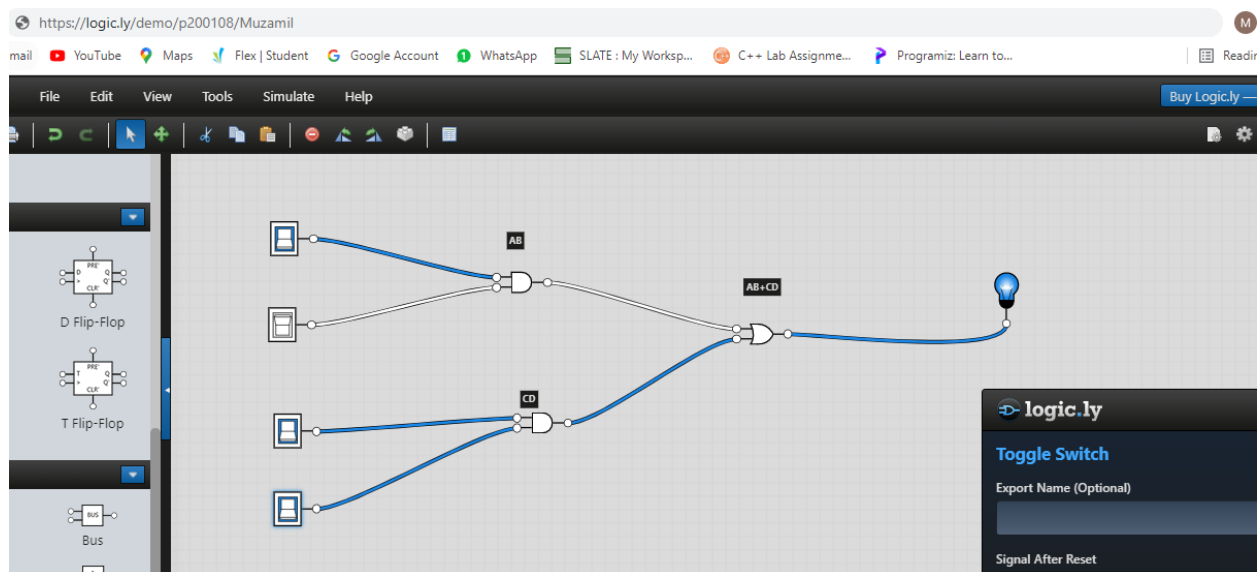
Inputs are 0011 and output is 1



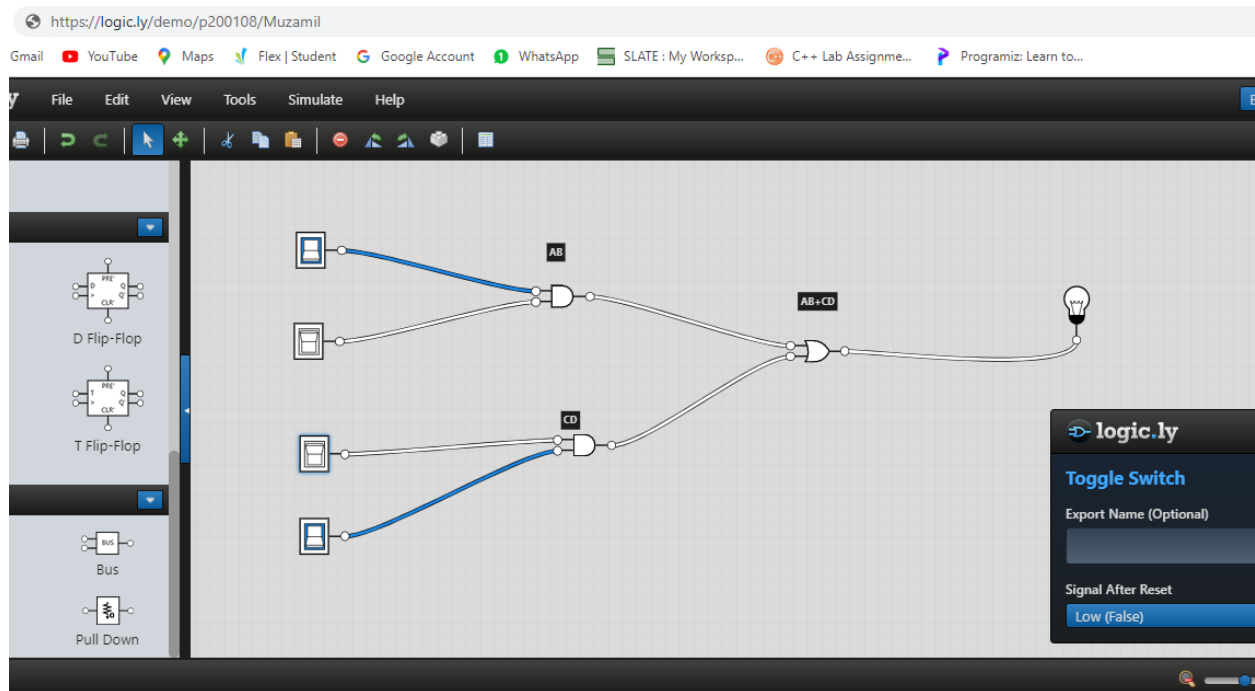
Inputs are 0111 and output is 1



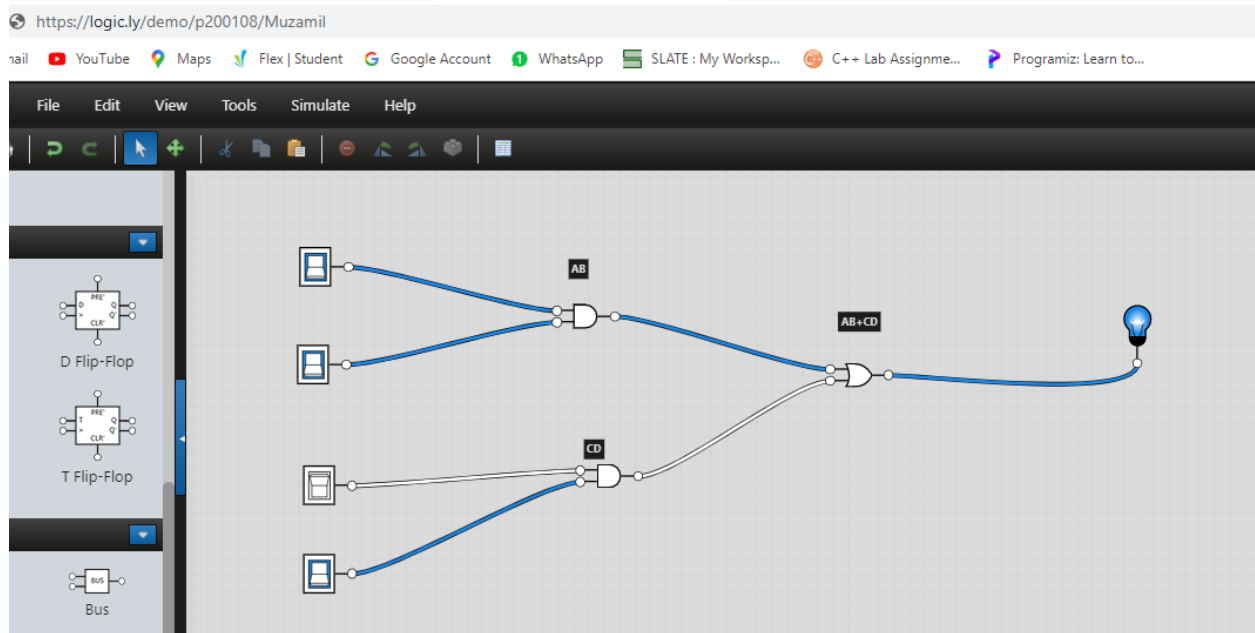
Inputs are 1011 and output is 1



Inputs are 1001 and output is 0



Inputs are 1101 and output is 1



Etc...

3. Construct K-Map for the given POS form given below. Simulate your final expression (reduced) and show the results.

$$F(A,B,C,D)=\pi(3,5,7,8,10,11,12,13)$$

K-Map

Question # 3

By using POS form

$$F(A, B, C, D) = \bar{A}(3, 5, 7, 8, 10, 11, 12, 13)$$

K. map

AB \ CD				
	00	01	11	10
00			0	
01		0	0	
11	0	0		
10	0		0	0

Annotations on the K-map:

- Group-5: A vertical group of two cells (00, 11) in column CD=11.
- Group-1: A horizontal group of two cells (01, 11) in row AB=01.
- Group-3: A horizontal group of two cells (00, 01) in row AB=11.
- Group-4: A horizontal group of two cells (11, 10) in row AB=10.

From group-1

$\Rightarrow CDA$ take complement and add them

$$(C' + D' + A)$$

Group-11

~~$$(C' + D' + A)$$~~

$B'CD$

$$\Rightarrow (B' + C + D')$$

Group 3

$AB'D$

$$\Rightarrow (A' + C + D)$$

Group - IV

$AB'C$

$$\Rightarrow (A' + B + C')$$

$$F = (C' + D' + A) \cdot (B' + C + D') \cdot (A' + C + D) \cdot (A' + B + C')$$

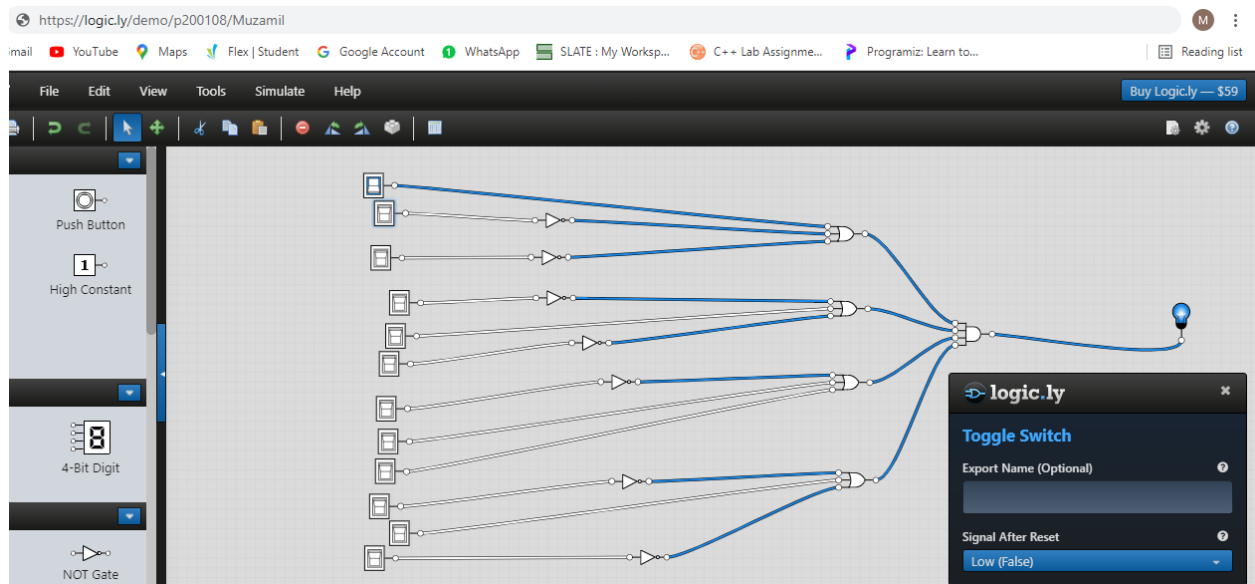
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Simplified Output Function

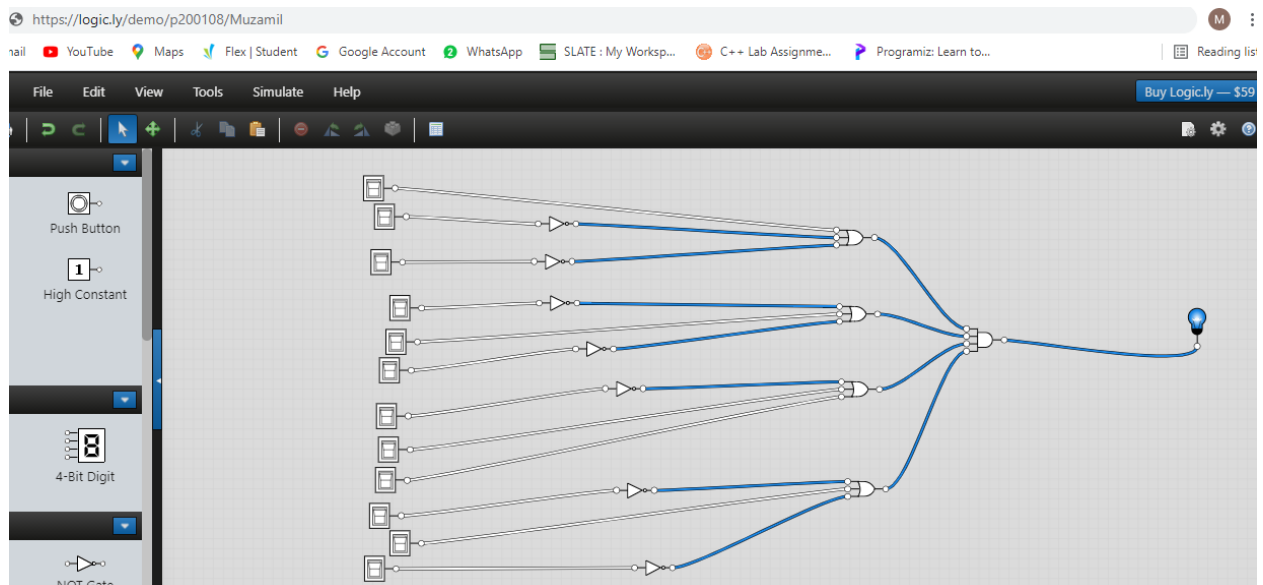
$$F = (C' + D' + A) \cdot (B' + C + D') \cdot (A' + C + D) \cdot (A' + B + C')$$

Software Simulation of Logic Circuit From Simplified Function

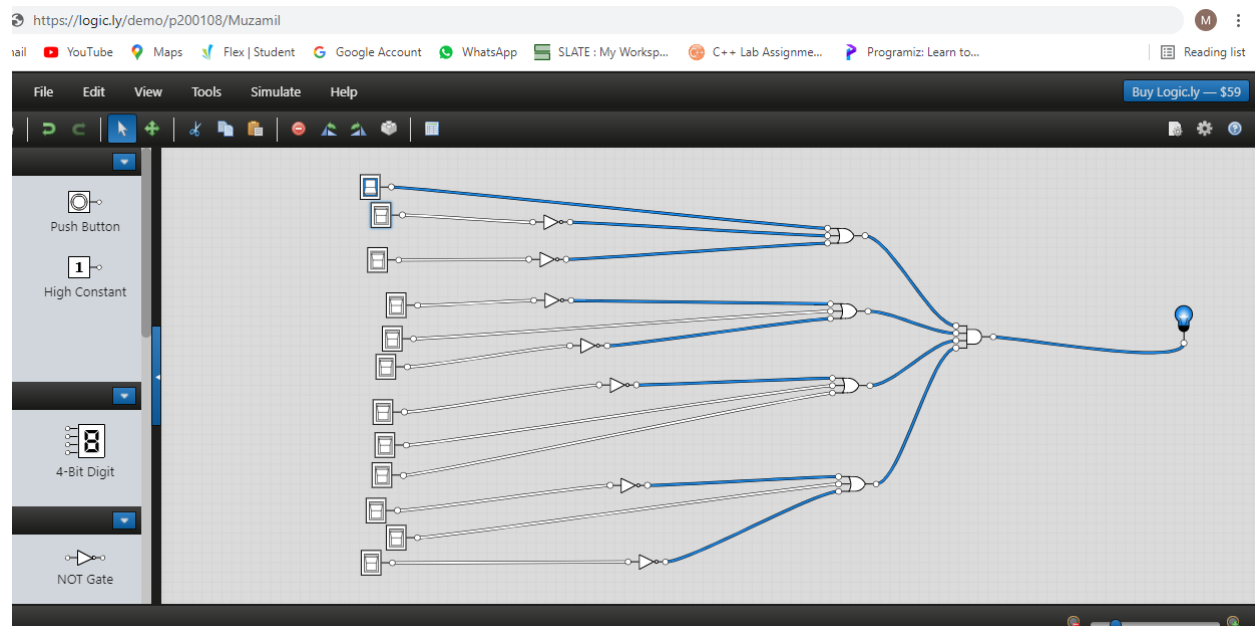
INPUTS Are 100000000000 and Output is 1



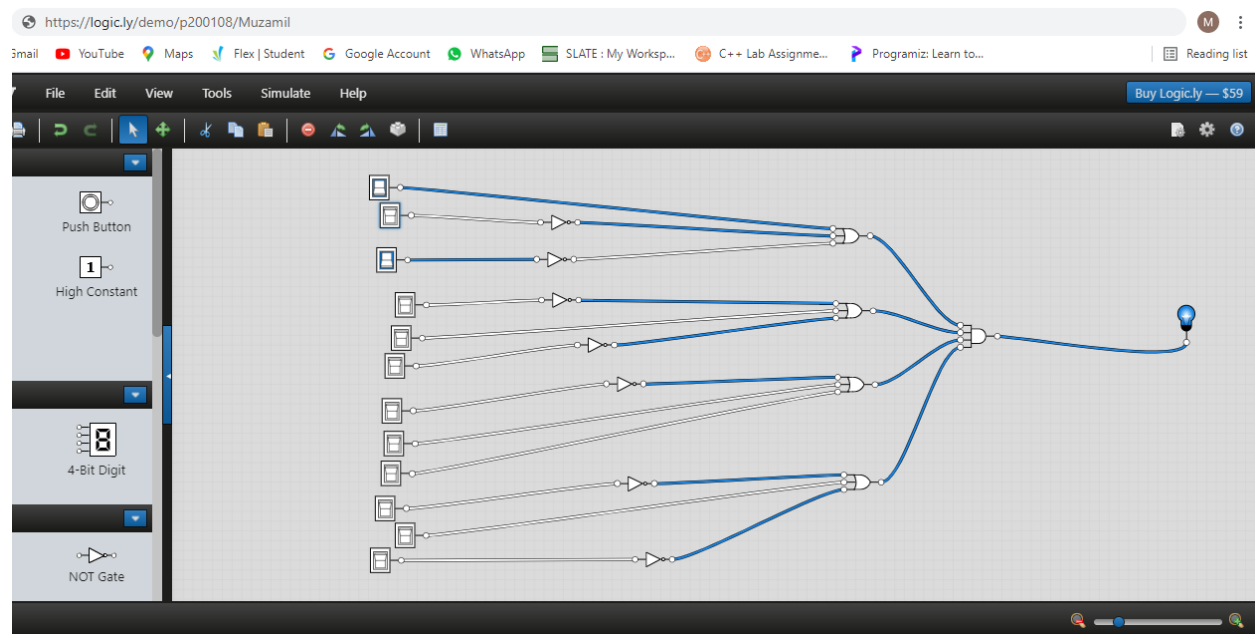
INPUTS Are 000000000000 and Output is 1



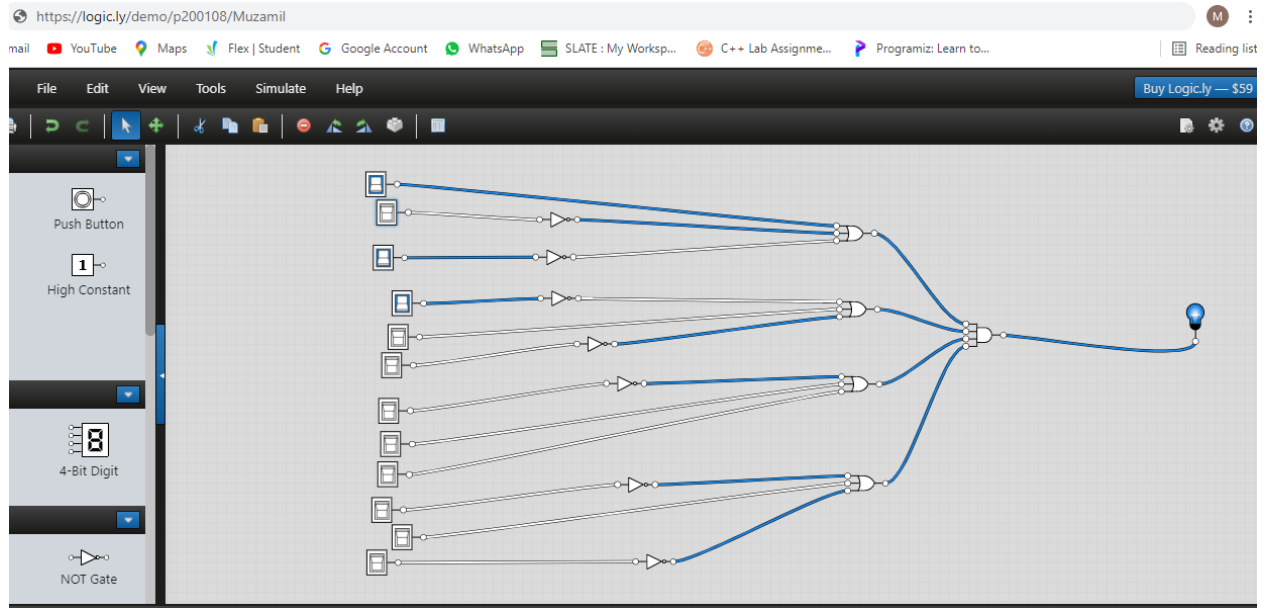
INPUTS Are 100000000000 and Output is 1



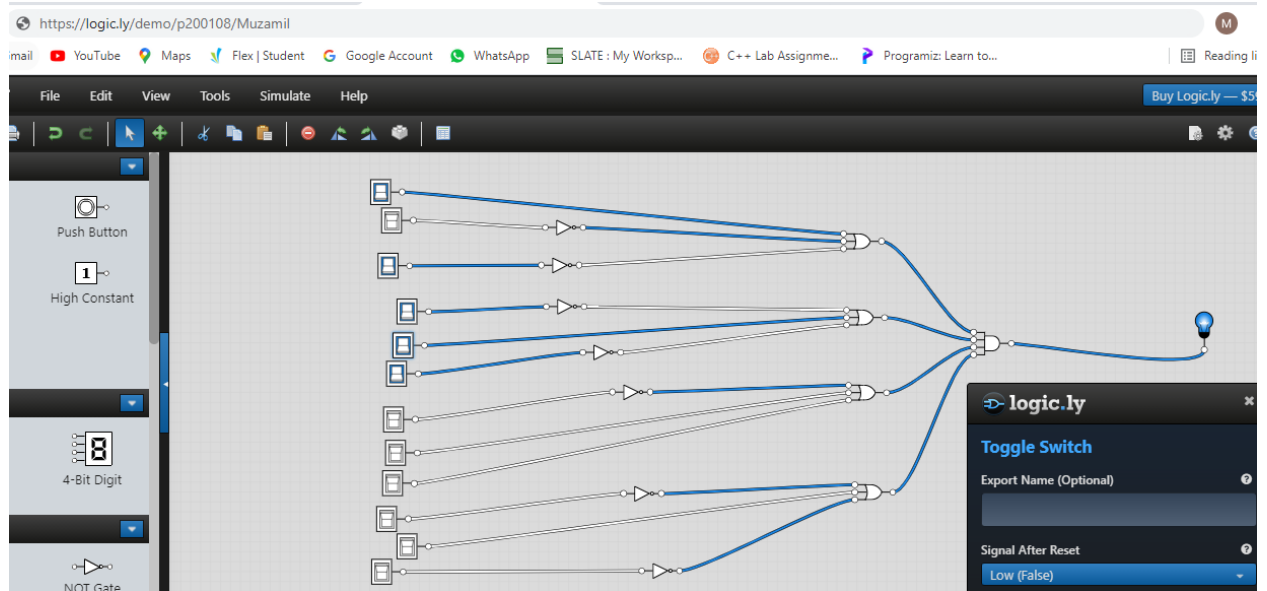
INPUTS Are 11100000000 and Output is 1



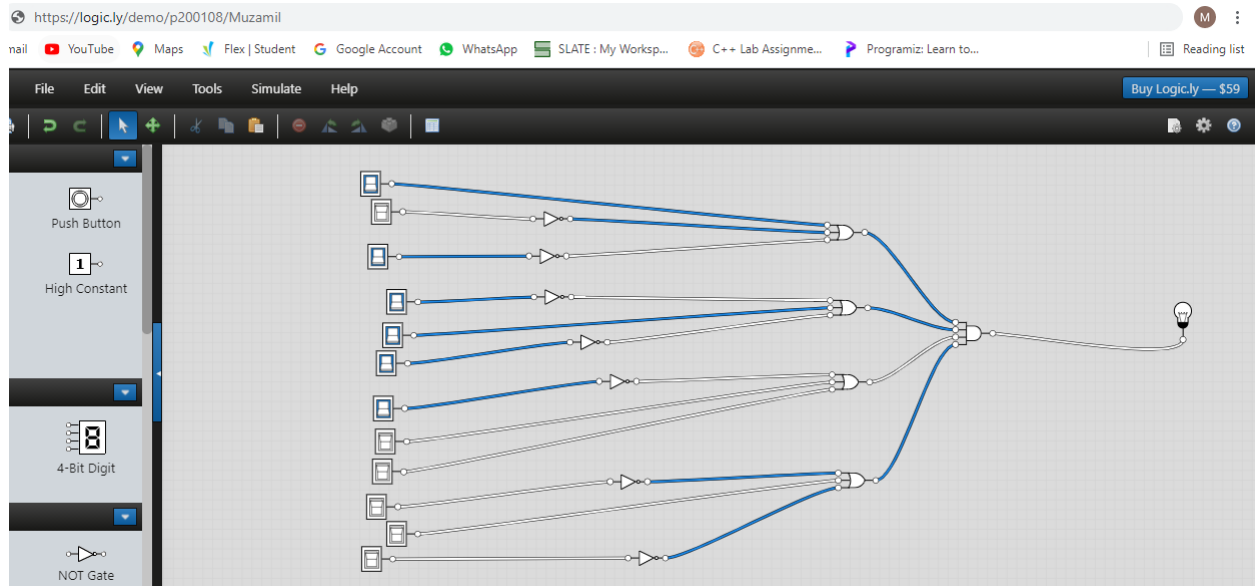
INPUTS Are 11110000000 and Output is 1



INPUTS Are 111111000000 and Output is 1



INPUTS Are 1111111000000 and Output is 0



4. Devise a minimized expression for the given truth table using K-Map (SOP form).
- a)

A	B	C	Out
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	0

K-Map

k-map

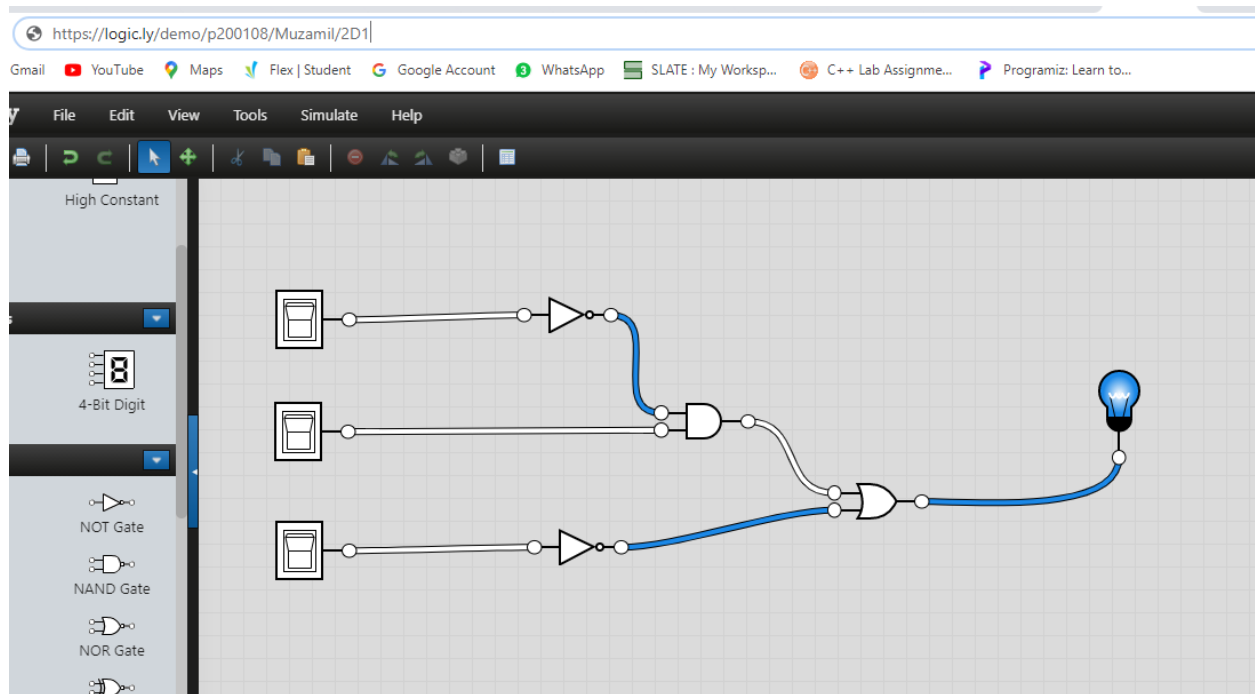
A	B	C	x
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	0

	00	01	11	10
00	1	1	1	
01		1		

$$F = A + \bar{B}C$$

Expression

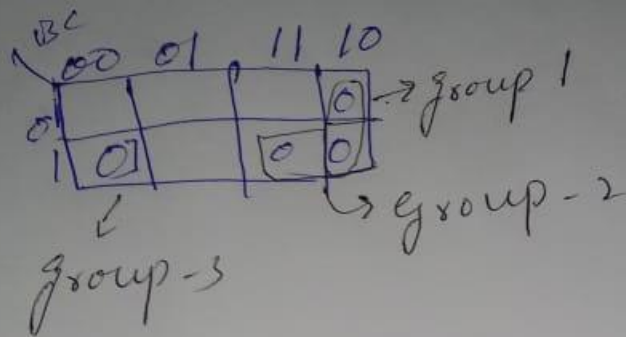
Output = $F = A + B'C$



b) For the above truth table, devise an expression in POS form using KMap.

K-Map

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P20-0108.



$$\text{Group-1} = BC'$$

take complement and add them

$$= \bar{B} + C$$

$$\text{Group-2} = AB$$

$$= \bar{A} + \bar{B}$$

$$\text{Group-3} = AC'$$

$$= \bar{A} + C$$

$$\therefore F = (B' + C) \cdot (\bar{A} + B') \cdot (\bar{A} + C)$$

Expression

Expression

$$F = (B' + C)(A' + B')(A' + C)$$

c) Devise a truth table and Boolean expression for the given K-Map.

		CD			
		00	01	11	10
AB	00		1		
	01		1		
	11		1		
	10	1	1		1

Truth Table

Truth Table

A	B	C	D	OUTPUT
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

<u>1</u>	<u>0</u>	<u>0</u>	<u>1</u>	<u>1</u>
<u>1</u>	<u>0</u>	<u>1</u>	<u>0</u>	<u>1</u>
<u>1</u>	<u>0</u>	<u>1</u>	<u>1</u>	<u>0</u>
<u>1</u>	<u>1</u>	<u>0</u>	<u>0</u>	<u>0</u>
<u>1</u>	<u>1</u>	<u>0</u>	<u>1</u>	<u>1</u>
<u>1</u>	<u>1</u>	<u>1</u>	<u>0</u>	<u>0</u>
<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>0</u>

Expression

F = AB'C + C'D + AB'D

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