

Automata practice Question and solutions by saba sumreen

Q:No.1) All words in which a appears tripled, if at all. This means that every clump of a's contains 3 or 6 or 9 or 12... a's.

$$(aaa^+)^*$$

Q:No.2) All words that contain exactly three b's in total.

$$(a^*ba^*ba^*ba^*)$$

Q:No.3) All words that contain exactly two b's or exactly three b's, not more

$$(a^*ba^*ba^*) + (a^*ba^*ba^*ba^*)$$

Q:No.4) All strings that end in a double letter.

$$(a+b)^*(aa+bb)$$

Q:No.5) All strings that have exactly one double letter in them.

$$(b^+)(ab)^*aa(ba)^*(b^+)+(a^+)(ba)^*bb(ab)^*(a^+)$$

Q:No.6) All strings in which the letter b is never tripled. This means that no word contains the substring bbb.

$$(a^+b+bb)(a+ab+abb)^*$$

Q:No.7). All words in which a is tripled or b is tripled, but not both. This means each word contains the substring aaa or the substring bbb but not both.

$$(A + b + bb)(a + ab + abb)^*aaa(A + b + bb)(a + ab + abb)^* +$$

$$(A + a + aa)(b + ba + baa)^*bbb(A + a + aa)(b + ba$$

Q:No.8) (i) All strings that do not have the substring ab

$$b^*a^*$$

(ii) All strings that do not have both the substrings bba and abb.

$$a^*(baa^*)^*b^* + b^*(a^*ab)^*a^*$$

- LHS: If there's a double b, it's not followed by an a.
- RHS: If there's a double b, it's not preceded by an a.

Q:No.10) All strings in which any b's that occur are found in clumps of an odd number at a time, such as abaabbbab.

$$a^*(b(bb)^*a)^*(\Lambda + b(bb)^*)$$

(ii) All strings that have an even number of a's and an odd number of b's.

$$(aa + bb + (ab + ba)(aa + bb)^*(ab + ba))^*$$

(iii) All strings that have an odd number of a's and an odd number of b's.

$$(aa + bb + (ab + ba)(aa + bb)^*(ab + ba))^*$$

$$(ab + ba)(aa + bb + (ab + ba)(aa + bb)^*(ab + ba))^*$$

The smallest string is ab or ba

- . Even letters can be added to the left, right, or both.