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The kNN classifier consists of two stages:

    During training, the classifier takes the training data and simply remembers it

           • During testing, kNN classifies every test image by comparing to all training images and transfering the labels of the k most similar training examples

    The value of k is cross-validated

          In this exercise you will implement these steps and understand the basic Image Classification pipeline, cross-validation, and gain proficiency in writing efficient,
          vectorized code.
In [28]: # Run some setup code for this notebook.
          from __future__ import print function
          import random
          import numpy as np
          from cs682.data_utils import load_CIFAR10
          import matplotlib.pyplot as plt
          # This is a bit of magic to make matplotlib figures appear inline in the notebook
          # rather than in a new window.
          %matplotlib inline
          plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
          plt.rcParams['image.interpolation'] = 'nearest'
          plt.rcParams['image.cmap'] = 'gray'
          # Some more magic so that the notebook will reload external python modules;
          # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
          %load ext autoreload
          %autoreload 2
          The autoreload extension is already loaded. To reload it, use:
            %reload_ext autoreload
In [29]: # Load the raw CIFAR-10 data.
          cifar10 dir = 'cs682/datasets/cifar-10-batches-py'
          # Cleaning up variables to prevent loading data multiple times (which may cause memory issue)
          try:
             del X_train, y_train
             del X test, y test
             print('Clear previously loaded data.')
          except:
            pass
          X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
          # As a sanity check, we print out the size of the training and test data.
          print('Training data shape: ', X train.shape)
          print('Training labels shape: ', y_train.shape)
          print('Test data shape: ', X_test.shape)
          print('Test labels shape: ', y_test.shape)
          Clear previously loaded data.
          Training data shape: (50000, 32, 32, 3)
          Training labels shape: (50000,)
          Test data shape: (10000, 32, 32, 3)
          Test labels shape: (10000,)
In [30]: # Visualize some examples from the dataset.
          # We show a few examples of training images from each class.
          classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 'ship', 'truck']
          num classes = len(classes)
          samples_per_class = 7
          for y, cls in enumerate(classes):
              idxs = np.flatnonzero(y train == y)
              idxs = np.random.choice(idxs, samples_per_class, replace=False)
              for i, idx in enumerate(idxs):
                  plt idx = i * num classes + y + 1
                  plt.subplot(samples_per_class, num_classes, plt_idx)
                  plt.imshow(X_train[idx].astype('uint8'))
                  plt.axis('off')
                  if i == 0:
                      plt.title(cls)
          plt.show()
                                                      frog
                                                            horse
                                 cat
          In [31]: # Subsample the data for more efficient code execution in this exercise
          num training = 5000
          mask = list(range(num training))
          X_train = X_train[mask]
          y train = y train[mask]
          num test = 500
          mask = list(range(num_test))
          X_{\text{test}} = X_{\text{test}}[\text{mask}]
          y_test = y_test[mask]
In [32]: # Reshape the image data into rows
          X_train = np.reshape(X_train, (X_train.shape[0], -1))
          X test = np.reshape(X test, (X test.shape[0], -1))
          print(X_train.shape, X_test.shape)
          (5000, 3072) (500, 3072)
In [33]: from cs682.classifiers import KNearestNeighbor
          # Create a kNN classifier instance.
          # Remember that training a kNN classifier is a noop:
          # the Classifier simply remembers the data and does no further processing
          classifier = KNearestNeighbor()
          classifier.train(X train, y train)
          We would now like to classify the test data with the kNN classifier. Recall that we can break down this process into two steps:
          1. First we must compute the distances between all test examples and all train examples.
          2. Given these distances, for each test example we find the k nearest examples and have them vote for the label
          Lets begin with computing the distance matrix between all training and test examples. For example, if there are Ntr training examples and Nte test examples,
          this stage should result in a Nte x Ntr matrix where each element (i,j) is the distance between the i-th test and j-th train example.
          First, open cs682/classifiers/k_nearest_neighbor.py and implement the function compute_distances_two_loops that uses a (very
          inefficient) double loop over all pairs of (test, train) examples and computes the distance matrix one element at a time.
In [34]: # Open cs682/classifiers/k_nearest_neighbor.py and implement
          # compute distances two loops.
          # Test your implementation:
          dists = classifier.compute_distances_two_loops(X_test)
          print(dists.shape)
          (500, 5000)
In [11]: # We can visualize the distance matrix: each row is a single test example and
          # its distances to training examples
          plt.imshow(dists, interpolation='none')
          plt.show()
           250
                          1000
                                       2000
                                                     3000
                                                                   4000
          Inline Question #1: Notice the structured patterns in the distance matrix, where some rows or columns are visible brighter. (Note that with the default color
          scheme black indicates low distances while white indicates high distances.)

    What in the data is the cause behind the distinctly bright rows?

    What causes the columns?

          Your Answer:

    distinctly bright rows are caused by a particular test image being similar to most training images.

    distinctly bright columns are caused by a particular training image being similar to many test images.

In [35]: # Now implement the function predict_labels and run the code below:
          # We use k = 1 (which is Nearest Neighbor).
          y test pred = classifier.predict labels(dists, k=1)
          # Compute and print the fraction of correctly predicted examples
          num correct = np.sum(y test pred == y test)
          accuracy = float(num correct) / num test
          print('Got %d / %d correct => accuracy: %f' % (num_correct, num_test, accuracy))
          Got 137 / 500 correct => accuracy: 0.274000
          You should expect to see approximately 27\% accuracy. Now lets try out a larger k, say k = 5:
In [36]: y test pred = classifier.predict labels(dists, k=5)
          num correct = np.sum(y test pred == y test)
          accuracy = float(num_correct) / num_test
          print('Got %d / %d correct => accuracy: %f' % (num_correct, num_test, accuracy))
          Got 139 / 500 correct => accuracy: 0.278000
          You should expect to see a slightly better performance than with k = 1.
          Inline Question 2 We can also other distance metrics such as L1 distance. The performance of a Nearest Neighbor classifier that uses L1 distance will not
          change if (Select all that apply.):
          1. The data is preprocessed by subtracting the mean.
           2. The data is preprocessed by subtracting the mean and dividing by the standard deviation.
           3. The coordinate axes for the data are rotated.
           4. None of the above. (Mean and standard deviation in (1) and (2) are vectors and can be different across dimensions)
          Your Answer: A KNN Classifier that uses L1 norm's performance will not change if (3) the axes are rotated.
          Your explanation: This is because for L1 norm the absolute value of the values for each axis are just added, so it shouldn't matter which axis is which.
In [22]: # Now lets speed up distance matrix computation by using partial vectorization
          # with one loop. Implement the function compute distances one loop and run the
          # code below:
          dists_one = classifier.compute_distances_one_loop(X_test)
          # To ensure that our vectorized implementation is correct, we make sure that it
          # agrees with the naive implementation. There are many ways to decide whether
          # two matrices are similar; one of the simplest is the Frobenius norm. In case
          # you haven't seen it before, the Frobenius norm of two matrices is the square
          # root of the squared sum of differences of all elements; in other words, reshape
          # the matrices into vectors and compute the Euclidean distance between them.
          difference = np.linalg.norm(dists - dists one, ord='fro')
          print('Difference was: %f' % (difference, ))
          if difference < 0.001:</pre>
              print('Good! The distance matrices are the same')
          else:
              print('Uh-oh! The distance matrices are different')
          Difference was: 0.000000
          Good! The distance matrices are the same
In [46]: # Now implement the fully vectorized version inside compute distances no loops
          # and run the code
          dists two = classifier.compute distances no loops(X test)
          # check that the distance matrix agrees with the one we computed before:
          difference = np.linalg.norm(dists - dists_two, ord='fro')
          print('Difference was: %f' % (difference, ))
          if difference < 0.001:</pre>
              print('Good! The distance matrices are the same')
          else:
              print('Uh-oh! The distance matrices are different')
          Difference was: 0.000000
          Good! The distance matrices are the same
In [48]: # Let's compare how fast the implementations are
          def time function(f, *args):
              Call a function f with args and return the time (in seconds) that it took to execute.
              import time
              tic = time.time()
              f(*args)
              toc = time.time()
              return toc - tic
          two_loop_time = time_function(classifier.compute_distances_two_loops, X_test)
          print('Two loop version took %f seconds' % two loop time)
          one_loop_time = time_function(classifier.compute_distances_one_loop, X_test)
          print('One loop version took %f seconds' % one_loop_time)
          no_loop_time = time_function(classifier.compute_distances_no_loops, X_test)
          print('No loop version took %f seconds' % no loop time)
          # you should see significantly faster performance with the fully vectorized implementation
          Two loop version took 21.526645 seconds
          One loop version took 33.403456 seconds
          No loop version took 0.247977 seconds
         Cross-validation
          We have implemented the k-Nearest Neighbor classifier but we set the value k = 5 arbitrarily. We will now determine the best value of this hyperparameter with
          cross-validation.
In [47]: num folds = 5
          k choices = [1, 3, 5, 8, 10, 12, 15, 20, 50, 100]
          X_train_folds = []
          y train folds = []
          # Split up the training data into folds. After splitting, X train folds and
          # y_train_folds should each be lists of length num_folds, where
          # y_train_folds[i] is the label vector for the points in X train folds[i].
          # Hint: Look up the numpy array split function.
          X_train_folds = np.array(np.array_split(X_train, num_folds))
          y_train_folds = np.array(np.array_split(y_train, num_folds))
          END OF YOUR CODE
          # A dictionary holding the accuracies for different values of k that we find
          # when running cross-validation. After running cross-validation,
          # k to accuracies[k] should be a list of length num folds giving the different
          # accuracy values that we found when using that value of k.
          k_to_accuracies = {}
          # TODO:
          # Perform k-fold cross validation to find the best value of k. For each
          # possible value of k, run the k-nearest-neighbor algorithm num folds times,
          # where in each case you use all but one of the folds as training data and the #
          # last fold as a validation set. Store the accuracies for all fold and all
          # values of k in the k to accuracies dictionary.
          for fold in range(num folds):
              x_te = X_train_folds[fold]
             y_te = y_train_folds[fold]
             x_tr = np.concatenate(np.array([x for i, x in enumerate(X_train_folds) if i != fold]), axis=0)
              y_tr = np.concatenate(np.array([y for i, y in enumerate(y_train_folds) if i != fold]), axis=0)
              classifier = KNearestNeighbor()
              classifier.train(x_tr, y_tr)
              for k_choice in k_choices:
                  y_test_pred = classifier.predict(x_te, k=k_choice)
                  num_correct = np.sum(y_test_pred == y_te)
                  accuracy = float(num_correct) / y_te.shape[0]
                  if k_choice in k_to_accuracies.keys():
                      k_to_accuracies[k_choice].append(accuracy)
                  else:
                      k_to_accuracies[k_choice] = [accuracy]
          END OF YOUR CODE
          # Print out the computed accuracies
          for k in sorted(k_to_accuracies):
              for accuracy in k_to_accuracies[k]:
                  print('k = %d, accuracy = %f' % (k, accuracy))
          k = 1, accuracy = 0.263000
          k = 1, accuracy = 0.257000
          k = 1, accuracy = 0.264000
          k = 1, accuracy = 0.278000
          k = 1, accuracy = 0.266000
          k = 3, accuracy = 0.239000
          k = 3, accuracy = 0.249000
          k = 3, accuracy = 0.240000
          k = 3, accuracy = 0.266000
          k = 3, accuracy = 0.254000
          k = 5, accuracy = 0.248000
          k = 5, accuracy = 0.266000
          k = 5, accuracy = 0.280000
         k = 5, accuracy = 0.292000
         k = 5, accuracy = 0.280000
         k = 8, accuracy = 0.262000
         k = 8, accuracy = 0.282000
         k = 8, accuracy = 0.273000
         k = 8, accuracy = 0.290000
         k = 8, accuracy = 0.273000
         k = 10, accuracy = 0.265000
         k = 10, accuracy = 0.296000
         k = 10, accuracy = 0.276000
         k = 10, accuracy = 0.284000
         k = 10, accuracy = 0.280000
         k = 12, accuracy = 0.260000
         k = 12, accuracy = 0.295000
         k = 12, accuracy = 0.279000
         k = 12, accuracy = 0.283000
         k = 12, accuracy = 0.280000
         k = 15, accuracy = 0.252000
         k = 15, accuracy = 0.289000
         k = 15, accuracy = 0.278000
         k = 15, accuracy = 0.282000
         k = 15, accuracy = 0.274000
         k = 20, accuracy = 0.270000
         k = 20, accuracy = 0.279000
         k = 20, accuracy = 0.279000
         k = 20, accuracy = 0.282000
         k = 20, accuracy = 0.285000
         k = 50, accuracy = 0.271000
         k = 50, accuracy = 0.288000
         k = 50, accuracy = 0.278000
         k = 50, accuracy = 0.269000
         k = 50, accuracy = 0.266000
         k = 100, accuracy = 0.256000
         k = 100, accuracy = 0.270000
         k = 100, accuracy = 0.263000
         k = 100, accuracy = 0.256000
         k = 100, accuracy = 0.263000
In [26]: # plot the raw observations
          for k in k_choices:
              accuracies = k to accuracies[k]
              plt.scatter([k] * len(accuracies), accuracies)
          # plot the trend line with error bars that correspond to standard deviation
          accuracies_mean = np.array([np.mean(v) for k,v in sorted(k_to_accuracies.items())])
          accuracies_std = np.array([np.std(v) for k,v in sorted(k_to_accuracies.items())])
          plt.errorbar(k choices, accuracies mean, yerr=accuracies std)
          plt.title('Cross-validation on k')
          plt.xlabel('k')
          plt.ylabel('Cross-validation accuracy')
          plt.show()
                                          Cross-validation on k
            0.29
            0.28
          Cross-validation accuracy
            0.27
            0.26
            0.25
            0.24
                              20
                                                                                100
                                                       60
                                                                    80
In [27]: \# Based on the cross-validation results above, choose the best value for k,
          # retrain the classifier using all the training data, and test it on the test
          # data. You should be able to get above 28% accuracy on the test data.
          best_k = 10
          classifier = KNearestNeighbor()
          classifier.train(X_train, y_train)
          y_test_pred = classifier.predict(X_test, k=best_k)
          # Compute and display the accuracy
          num correct = np.sum(y test pred == y test)
          accuracy = float(num_correct) / num_test
          print('Got %d / %d correct => accuracy: %f' % (num_correct, num_test, accuracy))
          Got 141 / 500 correct => accuracy: 0.282000
          Inline Question 3 Which of the following statements about k-Nearest Neighbor (k-NN) are true in a classification setting, and for all k? Select all that apply.
          1. The training error of a 1-NN will always be better than or equal to that of 5-NN.
          True for training error on 1-NN it will always find the distance to itself == 0. With a higher k, other different class neighbors around it could increase error.
          1. The test error of a 1-NN will always be better than that of a 5-NN.
          False depends on layout of training and test data
```

1. The decision boundary of the k-NN classifier is linear.

False arbitrary boundaries depending on closest neighbors at all points. Not necessarily linear

True As training data increases, you need to compute distances and compare for more points.

1. The time needed to classify a test example with the k-NN classifier grows with the size of the training set.

k-Nearest Neighbor (kNN) exercise

more details see the assignments page on the course website.

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For