A SIMD Programming Model for Dart, JavaScript, and other dynamically typed scripting languages

John McCutchan
Google Inc.
johnmccutchan@google.com

Haitao Feng
Intel Corp.
haitao.feng@intel.com

Zachary Anderson
Google Inc.
zra@google.com

Abstract

It has not been possible to take advantage of the SIMD coprocessors available in all x86 and most ARM processors shipping today in dynamically typed scripting languages. Web browsers have become a mainstream platform to deliver large and complex applications with feature sets and performance comparable to native applications, programmers must choose between Dart and JavaScript when writing web programs. This paper introduces an explicit SIMD programming model for Dart and JavaScript, we show that it can be compiled to efficient x86/SSE or ARM/Neon code by both Dart and JavaScript virtual machines achieving a 300%-600% speed increase across a variety of benchmarks. The result of this work is that more sophisticated and performant applications can be built to run in web browsers. The ideas introduced in this paper can also be used in other dynamically typed scripting languages to provide a similarly performant interface to SIMD coprocessors.

1. Introduction

All x86 and many ARM processors shipping today include a dedicated single instruction multiple data (SIMD) co-processor. On x86 the SSE instruction set allows for computing on 128-bit wide registers. ARM has the Neon instruction set which allows for computing on 128-bit wide registers. Both SSE and Neon have instructions for computing on 4 single precision floating point numbers (Float32x4) and 4 signed integers (Int32x4) stored in 128-bit registers. There are also instructions available for operating on 2 double precision floating point numbers (Float64x2) as well as algorithm specific instructions for operating on sound or pixel data.

Web browsers as a platform to deliver complex applications with feature sets and performance that are comparable to native desktop applications have become mainstream. All major browsers (Chrome, Firefox, Safari, and IE) include support for displaying 3D graphics through WebGL, playing 3D positional audio through WebAudio. These applications are written directly in JavaScript, Dart, or compiled to JavaScript from C/C++ code through the LLVM based Emscripten [2] compiler. Starting in 2008 with the advent of the V8 JavaScript virtual machine (VM) performance

```
// double average(Float32List data) {
// var sum = 0.0;
// for (var i = 0; i < data.length; i++) {
// sum += data[i];
// }
// return sum / data.length;
// }</pre>
```

Figure 1. Finding the average of an array of numbers in Dart.

of JavaScript execution has increased dramatically with browser vendors competing for the fastest JavaScript VM. Dart is a new web programming language designed for performance with a custom VM.

Despite the dramatic increase in performance it has not been possible for web programs to access the dedicated SIMD coprocessors. JavaScript is limited to scalar operations on double precision floating point values and Dart is limited to scalar operations on double precision floating point values and integers. In this paper we introduce:

- A SIMD programming model for Dart and JavaScript languages. The programming model is high level but allows for explicit control over the SIMD co-processors. It supports comparisons, branchless selection based on comparison results, and efficient shuffling of scalar values within a SIMD value. The programming model does not rely on compiler optimization passes like auto vectorization.
- Three (Float32x4, Int32x4, and Float64x2) new numeric value types for Dart and JavaScript.
- Efficient array storage of the new numeric value types.
- How we generate performant machine code that is free of high level abstraction in Dart and JavaScript VMs.
- An implementation of the programming model for the Dart VM that has shipped and is used in production today.
- An implementation of the programming model for the V8 JavaScript VM.
- Benchmarks that show (depending on the algorithm) a speedup of 300-600% across problem domains including real-time 3D graphics, numerical computation, ray tracing, and cryptography.

2. Lack of SIMD programmability for web applications

Many algorithms can be sped up by taking advantage of SIMD co-processors. A simple example is the averaging of an array of numbers, as shown in Figure 1 written in Dart.

 $[Copyright\ notice\ will\ appear\ here\ once\ 'preprint'\ option\ is\ removed.]$

```
// double average(Float32x4List data) {
  var sum = new Float32x4.zero();
  for (var i = 0; i < data.length; i++) {
    sum += data[i];
  }
  var total = sum.x + sum.y + sum.z + sum.w;
  return total / (data.length * 4);
  }
}</pre>
```

Figure 2. Finding the average of an array of numbers in Dart using SIMD.

The algorithm simply accumulates all the data points and computes the average by dividing by the number of data points. This algorithm can trivially take advantage of SIMD co-processors by adding 4 numbers at the same time, as shown in Figure 2, also in Dart

The bulk of the work is done in parallel and only after exiting the loop does the program need to fall back to scalar computation when computing the final sum and average.

If the Float32x4 type were available to web programmers and the optimizing compiler is successful in generating code that is free of memory allocation and allows for temporary values to stay in CPU registers, the algorithm can be sped up by 500%. In the following section, we provide more details on the programming model and how it can be efficiently compiled for x86 and ARM processors.

3. Bringing SIMD to the Web

The SIMD programming model for Dart and JavaScript is designed to give direct control to the programmer (or the Dart or C++ compiler generating JavaScript). It introduces three new 128-bit wide value types: Float32x4, Int32x4, and Float64x2. Each value type stores scalar values in multiple "lanes". For example, Float32x4 has four single precision floating point numbers in lanes labelled: x, y, z, and w. Note that w is the fourth lane and not the first. Each instance is immutable and all operations result in a new instance.

3.1 Primitive Operations

This section will focus on the Float32x4 type. The other types offer similar operations but can be limited by a lack of actual instructions in SSE or Neon. For example, there is no Int32x4 divide instruction in either SSE or Neon instruction sets. Emulation of missing instructions is discussed in future work.

Float32x4 supports standard arithmetic operations (+, -, *, /) as well as approximate square root, reciprocal square root, and reciprocal. It also supports absolute value, minimum, maximum, and clamp operations. All of these operations are performed for each lane. For example, the minimum value of two Float32x4 is the Float32x4 with the minimum value of each individual lane.

3.2 Type Conversion

Value cast operations between Float32x4 and Int32x4 as well as Float32x4 and Float64x2 are available. In the conversion between Float32x4 and Float64x2 only the x and y lanes are used.

Bit-wise cast operations between Float32x4, Int32x4, and Float64x2 are available. These do not interpret the lane values but provide a mechanism to directly convert the 128-bit value between all type pairs.

3.3 Comparison and Branchless Selection

When comparing SIMD values the result is not a single boolean value but a boolean value for each lane. Consider the example of

Figure 3. The scalar (top) and SIMD (bottom) minimum function.

Figure 4. The copy function copies an array of SIMD values.

computing the minimum value of two values. Figure 3 shows the scalar and SIMD algorithms written in Dart:

The comparison results in an Int32x4 value with lanes containing 0xFFFFFFFF or 0x0 when the lane comparison is true or false respectively. The resulting mask is used to pick which value's lane should be used.

3.4 Lane Access and Shuffling

Direct access to each lane of a Float32x4 can be had by accessing the x, y, z, or w instance properties. An example of this is shown in the average algorithm. Shuffling the order of lanes can also be done. Reversing the order of the lanes, in Dart:

```
Float32x4 reverse(Float32x4 v) {
  return v.shuffle(Float32x4.WZYX);
```

The shuffle method uses an integer mask to reorder the lane values in v. All 256 combinations are supported.

Because each instance is immutable it is not possible to change the value stored in one of the lanes. Methods, for example, withX allow for constructing new instances that are copies of an existing instance with an individual lane value changed. For example, in Dart:

```
var x = new Float32x4(1.0, 2.0, 3.0, 4.0);
var y = x.withX(5.0);
```

3.5 Memory I/O

Up until this point we have only discussed individual values but in order to be a generally useful programming model, compact and cache-friendly array storage of each type is introduced. Float32x4List, Int32x4List, and Float64x2List offer contiguous storage of Float32x4, Int32x4, and Float64x2 values. Figure 4 shows loading and storing SIMD values in Dart.

Note that on the load on line 5 a new instance of Float32x4 is constructed. In Sections 4.3 and 4.5 we discuss how the memory allocation and instance construction is avoided in optimized code.

3.6 Mapping from high level to low level

The programming model is high level with each operation requiring a method call on a heap allocated object and results in a new heap allocated object holding the resulting value. Each value is immutable and storage of temporary values cannot be reused. The

2 2014/1/10

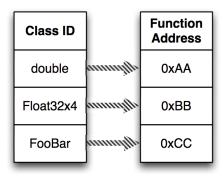


Figure 5. A call-site's type-cache.

design of the programming model was done with care so that when optimized code is generated, the overhead of the high level programming model can be removed. Almost all method calls will be mapped directly to a single CPU instruction. Some operations require slightly longer instruction sequences but so would a hand written assembly programming performing the same operation. Instances will be stored directly inside CPU registers avoiding the cost of memory allocation and object creation. The following section covers how this is accomplished.

4. Dart VM and V8 implementation

We will now discuss the implementation details of the programming model in the Dart VM. Section 4.11 discusses the implementation for the V8 VM.

4.1 Unoptimized Code

When a function is first compiled by the Dart VM the generated code is completely generic. Every method call is looked up in the receiving object's class's function table. Every temporary value is allocated in the heap as a full object under control of the GC.

4.2 Type Collection

Using techniques developed by Hölzle et al. [4] and other researchers, the unoptimized code collects important type information that is used later by the optimizing compiler. At each method call the unoptimized code maintains a cache mapping from receiver class id to address of the class's corresponding function, as shown in Figure 5.

This data has two important uses:

- Future execution of the unoptimized code will be faster if the
 receiving object has a class id already seen at the call site. Execution is faster because looking up the function for the method
 on the receiving object will result in a cache hit, avoiding the
 expensive lookup and cache update.
- Types seen at a method call site are fed into the optimizing compiler and code that optimistically expects to see the same type can be generated.

4.3 Boxed and Unboxed Values

The Dart compiler makes a distinction between boxed and unboxed [5] values. Boxed values are pointers to objects which are allocated in the heap whose life cycle is managed by the GC. Unboxed values are stored in CPU registers. Operations on unboxed values are much more efficient because the values are already contained in CPU registers. Figure 6 shows the in-memory layout of an instance of Float32x4. The object header contains information used for type collection and GC.



Figure 6. A boxed SIMD value.

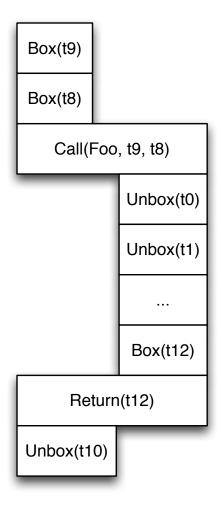


Figure 7. A SIMD value being boxed and unboxed for parameter passing and function return.

4.4 Parameter Passing

The Dart VM passes all method parameters and return value as boxed instances. This can have a negative performance impact as unboxed values will be boxed for the method call which will immediately unbox them again, as shown in Figure 7.

4.5 Inlining

3

Both the Dart VM and V8 make heavy use of inlining to avoid method call invocation and unnecessary boxing of values. The first form of inlining is similar to the inlining done in many compilers, the bodies of small functions are copied into the calling function, replacing the method call. The second form of inlining, replacement of runtime provided functions with compiler intermediate representation (IR) instructions is the key to achieving high

```
1 Float32x4 compute(Float32x4 a, Float32x4 b) {
2   var c = a + b;
3   var d = a * a;
4   var e = b * b;
5   return c + d + e;
6 }

1 t0 \(
Call(+, a, b);
2 t1 \(
Call(*, a, a);
3 t2 \(
Call(*, b, b);
4 t3 \(
Call(+, t0, t1);
5 t4 \(
Call(+, t3, t2);
6   return t4:
```

Figure 8. A Dart function (top) and its compiled, but unoptimized code (bottom). Call here indicates an expensive call into the Dart runtime.

```
1 if (TypeMatch(a, Float32x4)) {
2    deoptimize();
3 }
4 if (TypeMatch(b, Float32x4)) {
5    deoptimize();
6 }
7 t0 ← unbox(a);
8 t1 ← unbox(b);
9 t2 ← BinaryFloat32x40p+(t0, t1);
10 t3 ← BinaryFloat32x40p*(t0, t0);
11 t4 ← BinaryFloat32x40p*(t1, t1);
12 t5 ← BinaryFloat32x40p+(t2, t3);
13 t6 ← BinaryFloat32x40p+(t5, t4);
14 return box(t6);
```

Figure 9. The compute function after optimizing compilation. Here, BinaryFloat32x40p{+,*} indicate fast, inlined machine code routines.

performance with this programming model. Consider the code in Figure 8.

So long as the function compute has only ever been given Float32x4 instances, the compiler will recognize all of the call sites are monomorphic, in other words, each call site has a single receiver class id and target function. The type data collected in unoptimized code at each method call site is used to determine whether this is the case or not. The function targets Float32x4_Add and Float32x4_Mul are both provided by runtime and the compiler knows how to replace them with IR instructions. As mentioned above, the functions only accept and return boxed instances but the Float32x4 IR instructions only accept and return unboxed values.

4.6 Optimized Code

When inlining is successful the optimized code will be free of object construction and method call invocations. Figure 9 shows the compute function from Figure 8 after optimization.

The optimized code first validates the class of each input value. If any of the types do not match the expected type, the function is deoptimized. For more details on deoptimization see Section 4.9. After being validated the values are unboxed directly into CPU registers (tN) and the remaining operations are performed directly in CPU registers with no memory I/O. The final step is to box the result so it can be returned. Figure 10 shows the final assembled result using Intel SSE SIMD instructions.

For readers unfamiliar with SSE, the following list describes the instructions used in the example:

- movups Unaligned load or store of 128-bit value.
- movaps Register move.

```
;; CheckClass:14(v2)
0x107822533 testb rdx,0x0x1
0x107822536 jz 0x107822607
0x10782253c movzxwq rbx,[rdx+0x1]
0x107822541 cmpl rbx,0x37
0x107822544 jnz 0x107822607
       ;; CheckClass:14(v3)
0x10782254a testb rcx,0x0x1
0x10782254d iz 0x107822612
0x107822553 movzxwq rbx,[rcx+0x1]
0x107822558 cmpl rbx,0x37
0x10782255b jnz 0x107822612
        ;; v11 <- UnboxFloat32x4:14(v2)
0x107822561 movups xmm1, [rdx+0x7]
        ;; v14 <- UnboxFloat32x4:14(v3)
0x107822565 movups xmm2, [rcx+0x7]
        ;; ParallelMove xmm3 <- xmm1
0x107822569 movaps xmm3, xmm1
        ;; v4 <- BinaryFloat32x40p:14(+, v11, v14)
0x10782256c addps xmm3, xmm2
        ;; ParallelMove xmm4 <- xmm1
0x10782256f movaps xmm4, xmm1
        ;; v5 <- BinaryFloat32x40p:26(*, v11, v11)
0x107822572 mulps xmm4, xmm1
        ;; ParallelMove xmm1 <- xmm2
0x107822575 movaps xmm1, xmm2
       ;; v6 <- BinaryFloat32x40p:38(*, v14, v14)
0x107822578 mulps xmm1, xmm2
       ;; v7 <- BinaryFloat32x40p:50(+, v4, v5)
0x10782257b addps xmm3, xmm4
        ;; v8 <- BinaryFloat32x40p:58(+, v7, v6)
0x10782257e addps xmm3, xmm1
        ;; v15 <- BoxFloat32x4:112(v8)
0x107822581 movq r11,[r15+0x47]
0x107822588 movq rax,[r11]
0x10782258b addq rax,0x20
0x10782258f movq r11,[r15+0x4f]
0x107822596 cmpq rax,[r11]
0x107822599 jnc 0x1078225eb
0x10782259f movq r11,[r15+0x47]
0x1078225a6 movq [r11],rax
0x1078225a9 subq rax,0x1f
0x1078225ad movq [rax-0x1],0x370200
0x1078225b5 movups [rax+0x7], xmm3
```

Figure 10. Optimized machine code generated by the Dart VM for the compute function, SSE instructions bolded.

- addps Add 4 single precision floating point numbers.
- mulps Multiply 4 single precision floating point numbers.

4.7 Register Allocation

The Dart VM already supported unboxed double values which on x86 used the xmm registers. The xmm registers are also needed for Float32x4, Int32x4, and Float64x2 values. The register allocator was extended to support both 8 and 16 byte values stored in xmmN registers as well as allocate the appropriate range of memory to spill values from registers to the stack when register pressure requires spilling.

4.8 Alignment

4

SIMD instruction sets provide preferred memory I/O instructions that require the memory address to be aligned on 16-byte boundaries. These instructions are typically faster than the unaligned memory I/O instructions. All memory I/O instructions emitted by the Dart VM are for unaligned addresses because the Dart VM GC cannot guarantee object alignment.

```
1 compute(var a, var b) {
2  var c = SIMD.float32x4.add(a, b);
3  var d = SIMD.float32x4.mul(a, a);
4  var e = SIMD.float32x4.mul(b, b);
5  var t = SIMD.float32x4.add(c, d);
6  return SIMD.float32x4.add(t, e);
7 }
```

Figure 11. Our compute function translated to JavaScript using our experimental SIMD module.

4.9 Deoptimization

After a function has been optimized if one of the values it uses violates the optimistic type expectations, a deoptimization occurs resulting in the following process:

- Execution of optimized code stops.
- Optimized code is invalidated and disconnected from the function.
- Live unboxed values are boxed.
- Pointers to boxed values are stored in the correct locations of the unoptimized codes stack frame.
- Execution of the function's unoptimized code begins at exactly the same point that the deoptimization occurred.

An important thing to understand is that only functions which are provided stable input types will be optimized.

4.10 Port to ARM/Neon

We have ported these SIMD operations in Dart to the Neon instruction set provided by many ARM implementations. In most cases the mapping from SSE instructions to Neon instructions is straightforward. In the case of the shuffle operation, the Neon instruction set lacks a fully general single instruction. In this, and a limited number of additional cases, we take advantage of the overlap of the 128-bit "Q" registers with the 64-bit "D" and 32-bit "F" registers, and implement shuffles, etc., by simply manipulating the "D" and "F" registers that underly the "Q" registers. Presently, these sequences are generated naively, and we are unaware of the performance cost, though we assume it is small based on the benchmark results in Section 5. We leave as future work finding minimal Neon sequences to implement the more general instructions provided by SSE.

4.11 Implementation for JavaScript and V8

The SIMD programming model for Dart is used for JavaScript as well. The 128-bit wide value types are introduced, but as there are no class and operator overloading language features in JavaScript, the syntax of the SIMD API is different than Dart's. We introduced a SIMD global module with operations grouped by type. The following example demonstrates the syntactic differences. Figure 11 shows the translation of our compute function into JavaScript. The V8 implementation is conceptually similar to the implementation in the Dart VM.

- We added the 128-bit wide value constructor and SIMD API into full-codegen which generates un-optimized code and optimized them in the Crankshaft which generates optimized code.
- We allocated the 128-bit value in a heap object (with a header to indicate the type) and garbage collect it when it is boxed; when the value is un-boxed, we allocate it into a hardware 128-bit register (XMM register in the Intel IA32 and X64 architectures).
- We inlined all the SIMD operations, inlining is the key technique for the performance acceleration.

 Like the Dart VM, when transitioning from optimized to unoptimized code (due to a deoptimization event) the unboxed values are boxed and pointers to the boxed values are placed in the unoptimized codes stack frame.

Despite the many similarities, there are some important differences in the V8 implementation:

- The unoptimized code does not collect type information for Float32x4, Int32x4, and Float32x4 instances. Instead upon entry to a SIMD.type.op function the types of the parameters are verified to match the expected type. If they do not an exception is thrown.
- Because JavaScript is more dynamic than Dart and allows for object fields and functions to be modified at runtime, for example, the SIMD.float32x4.add method could have been overridden by the program. More checks are required to ensure that these operations have not been replaced with user written code. When this occurs inlining cannot be performed and performance suffers.

5. Benchmarks

In this section we will present benchmark results for four different benchmarks. Full source code of these benchmarks is available from a GitHub repository¹.

- Average Averaging many floating point numbers.
- Mandelbrot Generating a Mandelbrot [1] visualization.
- MatrixMultiply 4x4 matrix multiplication.
- **VectorTransform** 3D vertex transformation used for 3D rendering.

We ran these benchmarks on the Dart VM, V8, and IonMonkey using Dart and JavaScript implementations as appropriate. We used an Ubuntu 13.04 64-bit Linux system with an Intel CPU (Intel(R) Xeon(R) CPU E5-2690 @ 2.90GHz). We also ran the benchmarks on the Dart VM running on a Nexus 7, ARM Android device. Since ports to ARM/Neon are not yet complete for V8 and IonMonkey we did not run the JavaScript implementations on the Nexus 7.

We ran each benchmark repeatedly until at least 2 seconds had elapsed, then divided by the number of iterations in this time to arrive at the time taken for a single iteration. We report absolute times in microseconds for both the scalar and SIMD versions of the benchmarks, as well as the SIMD speedup calculated as the scalar time divided by the SIMD time.

5.1 Discussion

The results of our benchmarks are shown in Tables 1 and 2. Table 1 shows results on our Intel machine for Dart, V8, and IonMonkey. Table 2 shows results on a Nexus 7 device for Dart. The benchmark data show significant speedups across a variety of algorithms, implementations and across the two platforms when we use SIMD operations. Further, our JavaScript and Dart benchmark kernels and timing harness are as similar as possible, so it is possible not only to compare scalar and SIMD implementations running on the same VM, but also to compare results across the three VMs.

Thus, some of the results require some additional explanation. The theoretical performance gain from SIMD should only be 4x, however a number of our benchmarks show larger gains. It is important to note that in the case of Dart and JavaScript that the scalar code performs double precision arithmetic, while the SIMD code performs single precision arithmetic. The data in these scalar

5

¹ ECMAScript SIMD Polyfill

Benchmark	Scalar	SIMD	Speedup	
	Time(us)	Time(us)		
Dart				
Average	381	36	10.5x	
Mandelbrot	330714	128750	2.6x	
MatrixMultiply	68	17	4.0x	
VectorTransform	25	5	5.0x	
V8				
Average	208	35	5.9x	
Mandelbrot	393167	109158	3.6x	
MatrixMultiply	74	20	3.7x	
VectorTransform	30	6	5.0x	
IonMonkey				
Average	116	21	5.5x	
Mandelbrot	346333	152357	2.3x	
MatrixMultiply	97	19	5.1x	
VectorTransform	33	8	4.1x	

Table 1. Benchmark results for Dart, V8, and IonMonkey on our x64 Linux machine.

Benchmark	Scalar	SIMD	Speedup
	Time(us)	Time(us)	
Average	1832	180	10.1x
Mandelbrot	1806000	892333	2.0x
MatrixMultiply	630	224	2.8x
VectorTransform	173	67	2.6x

Table 2. Benchmark results for Dart on our ARM Android device.

benchmarks is loaded from an array holding single precision floating point values. Thus, the scalar code must convert from single to double precision before performing the calculation, while the SIMD code requires no conversion, implying some saved time for the SIMD codes.

As for the Mandelbrot benchmark, Dart and IonMonkey achieved only speedups of 2.6x and 2.3x respectively, while V8 achieved a speedup of 3.6x. The reason for the discrepancy is that the Dart VM has not fully implemented the necessary inlining optimizations for the Int32x4 type which is used in the Mandelbrot benchmark.

6. Related Work

6.1 C SSE Intrinsics

C/C++ compilers offer SIMD intrinsic functions (xmmintrin.h and emmintrin.h). At compile time these function calls are replaced with a single instruction. Conceptually, the SIMD programming model for Dart and JavaScript is similar but neither Dart nor JavaScript has static type information available at compile time and instead, must rely on run-time type collection (or enforcement) before the compiler can emit the SSE instructions.

6.2 SIMD in C#

The Mono C# compiler provided an API for SIMD [3] programming. This API is considered experimental and directly mimics the SSE instruction set without any concern for portability across different SIMD instruction sets. The SIMD programming model presented in this paper was designed to run across SSE and Neon instruction sets and has been implemented for both.

6.3 Auto-Vectorization

Mozilla has experimented [6] with an auto vectorization pass in their JavaScript compiler. The focus of this work was on a gaussian blur algorithm written in JavaScript. Speed gains of approximately 20% were achieved. This work was never merged and appears abandoned.

7. Conclusions and Future Work

In this paper we have presented a high level programming model that offers direct control of SIMD co-processors to web programs in both Dart and JavaScript. We have shown how both Dart and JavaScript VMs can avoid memory allocation and the resulting garbage collector (GC) pressure by avoiding instance creation with inlining and unboxed values. We have discussed the implementations in both the Dart VM and V8. Finally, we have presented benchmarks demonstrating the real world performance gains that this programming model provides. Future work includes:

- Support for wider (256-bit and 512-bit) SIMD register widths (AVX and AVX-512) and the natural data types they offer, for example, Float32x8 and Float32x16. This includes generating correct code for wider register widths on CPUs that only support 128-bit wide registers.
- Support for pixel processing by developing a portable abstraction around instructions that are algorithm specific operating on 16 individual bytes. Including support for saturating arithmetic operations.
- Support operations which do not have CPU instructions available, for example, Int32x4 division.
- Supporting for passing and returning unboxed values directly, avoiding the overhead of boxing values on method invocation and return.
- Support types that have few SIMD instructions, for example, Int16x8. Speed ups may be seen on these types because efficient native code can that does N scalar operations can be emitted directly.

References

- Benoit Mandelbrot, December 2013. http://en.wikipedia.org/ wiki/Benoit Mandelbrot.
- [2] Emscripten, January 2014. http://en.wikipedia.org/wiki/ Emscripten.
- [3] Mono Documentation: Mono.Simd Namespace, January 2014. http://docs.go-mono.com/?link=N%3aMono.Simd.
- [4] Urs Hölzle and David Ungar. Reconciling responsiveness with performance in pure object-oriented languages. ACM Trans. Program. Lang. Syst., 18(4):355–400, July 1996.
- [5] Xavier Leroy. Unboxed objects and polymorphic typing. In Proceedings of the 19th ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages, POPL '92, pages 177–188, New York, NY, USA, 1992. ACM.
- [6] Nicolas B. Pierron. IonMonkey: Use SIMD to optimize gaussian blur, January 2014. https://bugzilla.mozilla.org/show_bug.cgi? id=832718.

6 2014/1/10