

# The effect of social roles on group behaviour

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**Abstract:** In a recent series of papers, we proposed a mathematical model for the dynamics of a group of interacting pedestrians. The model is based on a non-Newtonian potential, that accounts for the need of pedestrians to keep both their interacting partner and their walking goal in their vision field, and to keep a comfortable distance between them. These two behaviours account respectively for the angular and radial part of the potential from which the force providing the pedestrian acceleration is derived. The angular term is asymmetric, i.e. does not follow the third law of dynamics, with observable effects of group formation and velocity. We first assumed the group to move in a scarcely dense environment, whose effect could be modelled through a “white noise thermic bath”, and successfully compared the predictions of the model with observations of real world pedestrian behaviour. We then studied, both from an empirical and a theoretical standpoint, the effect of crowd density on group dynamics. We verified that the average effect of crowd density may be modelled by adding a harmonic term to the group potential. The model predictions, which include “phase transitions” in the group configuration (e.g. in 3 people groups transition from a “V” formation to a “Λ” one, and eventually to pedestrians walking in a line), are again confirmed, at least in the observed density range, by a comparison with real world data. Until now we had averaged all pedestrian data collected in a given environmental setting (i.e. in corridors of similar width and at similar crowd densities) without differentiating on group composition and social roles. In this work, we present preliminary results on these features, namely we study how the group configuration and velocity is affected by inter-pedestrian relation (family, couples, colleagues, friends), purpose (work, leisure) and gender. We also show results related to the effect of asymmetric interactions, that confirm further the non-Newtonian nature of gaze-based angular interaction in our model.

**Keywords:** Group behaviour, social interaction, experimental data, mathematical modelling

## 1 Introduction

Urban crowds are characterised by the presence of a large number of social groups. The ratio between individual pedestrians and pedestrians moving in groups may change considerably between different environments and at different times of the day [1,2,3], but it is in general never negligible, with groups representing up to 85% of the walking population [4,5]. Despite this empirical evidence about the importance of groups, the standard approach in microscopic (agent-based) pedestrian modelling is to assume that the crowd is composed of individuals, moving without any preferential ties to other pedestrians. Such an approach is, at least, a strong simplification as the description of a system of complex molecules as a monoatomic gas and, although justified in the infancy of the field, it should be now replaced by more realistic models taking in account group and in general

social interactions.

Indeed, in recent years, a few studies concerning empirical observations and mathematical modelling of the groups’ characteristic configuration and velocity [1, 4,5,6,7,8,9,10,11] have been introduced. In a recent series of papers [1,2,12], we focused on the development of a mathematical model to describe group interaction. The model is based on few and intuitive ideas about social interaction in pedestrian groups, and its predictions are in agreement with the observed natural behaviour of pedestrians. It may also describe how group behaviour is modified by crowd density, just by adding a harmonic term to the low density potential.

In this work, after reviewing our model, we present some new empirical findings regarding how group dynamics is affected by group composition (purpose, inter-group relations, gender) and by asymmetric interactions, and discuss these findings under the light of our mathematical framework.

## 2 Potential for group interaction

### 2.1 Mathematical formulation

Following [1], we assume that 2 pedestrians, identified as  $i$  and  $j$ , are socially interacting while walking towards a common goal, identified by a unit vector  $\hat{g}$ .

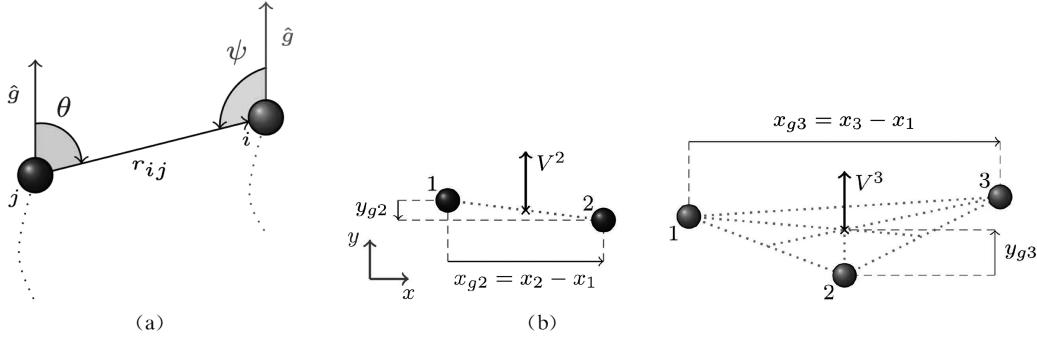


Fig. 1 (a)  $r$  and  $\theta$  give the position of pedestrian  $i$  with respect to  $j$ .  $|\theta|$  is the angle that  $j$ 's gaze has to span between the goal direction  $\hat{g}$  and  $i$ , while the corresponding angle for  $i$  is given by  $|\psi|$ . (b) Definition of the 2 and 3 people group observables.

so that  $|\psi|$  is the magnitude of the angle that  $i$ 's gaze has to span between the goal and the interaction partner, while  $|\theta|$  is the corresponding angle for  $j$ . Our model is based on the assumption that pedestrians want to look towards their goal for safe walking, but for social interaction they want both to have their partner in their vision field [13], and to be visible to their partner, so that their gazes may meet [14]. When pedestrians are in a relative position that does not allow for an optimal interaction, they feel a *discomfort*. We model this discomfort and assume that it plays the same role that potential energy plays in physics, namely the pedestrian's acceleration is determined by the negative gradient of the potential, so that the pedestrians move towards the *discomfort minimum*. The discomfort should grow with the angles  $|\theta|$  and  $|\psi|$ , and we may assume, out of simplicity, the law to be quadratic

$$\Theta^\eta(\theta) = (1 + \eta)\theta^2 + (1 - \eta)\psi^2, \quad -1 \leq \eta \leq 1. \quad (2)$$

The discomfort potential should have also a radial component, assuming a minimum at the distance  $r_0$  at which social interaction is maximally comfortable [15]. A simple choice is to have this potential to diverge for  $r \rightarrow 0$  to avoid physical overlapping, and to grow linearly for  $r \rightarrow \infty$ , so that the interaction force converges to a constant value for large distances. A simple choice<sup>1</sup> is

$$R(r) = \frac{r}{r_0} + \frac{r_0}{r}. \quad (3)$$

<sup>1</sup>Describing well pedestrian behaviour close to the potential minimum, but failing far from the minima, due probably also to the fact that far away pedestrians stop interacting.

Their relative position,  $\mathbf{r} \equiv \mathbf{r}_{ij} \equiv \mathbf{r}_i - \mathbf{r}_j$ , may be written in polar coordinates as  $(r, \theta)$ , where  $-\pi < \theta \leq \pi$  is the angle between  $\mathbf{r}_{ij}$  and  $\hat{g}$  (see Fig. 1). We also define the angle  $\psi$

$$\psi \equiv \begin{cases} \theta - \pi & \text{if } \theta > 0, \\ \theta + \pi & \text{if } \theta \leq 0, \end{cases} \quad (1)$$

We assume the total potential to be the sum of the angular and radial term<sup>2</sup>

$$U_{ij}^\eta(r, \theta) = C_r R(r) + C_\theta \Theta^\eta(\theta). \quad (4)$$

The acceleration of pedestrian  $i$  results to be

$$\dot{\mathbf{v}}_i = \mathbf{F}_{ij} = -\nabla_i U_{ij}^\eta(\mathbf{r}_i - \mathbf{r}_j). \quad (5)$$

If we choose a Cartesian system with  $y$  axis aligned to the goal direction  $\hat{g}$  we have

$$\begin{aligned} F_x^\eta &= \frac{C_r}{r_0} \left( \frac{r_0^2}{r^2} - 1 \right) \sin \theta - \frac{4}{r} C_\theta (\theta - \theta_{\text{sgn}(\theta)}) \cos \theta, \\ F_y^\eta &= \frac{C_r}{r_0} \left( \frac{r_0^2}{r^2} - 1 \right) \cos \theta + \frac{4}{r} C_\theta (\theta - \theta_{\text{sgn}(\theta)}) \sin \theta, \end{aligned} \quad (6)$$

where  $\theta_\pm$  are the angles at which the angular potential attains a minimum,

$$\theta_\pm = \pm (1 - \eta) \frac{\pi}{2}. \quad (7)$$

This system has some properties that make its dynamics very different from the one of a classical Newtonian  $n$  body system. Indeed,  $U_{ij}^\eta(\mathbf{r}_i - \mathbf{r}_j)$  is not the potential of the  $(i, j)$  system, but only of the pedestrian  $i$ . For  $\eta \neq 0$  we have

$$U^\eta(-\mathbf{r}) \neq U^\eta(\mathbf{r}) \Rightarrow \mathbf{F}_{ij} \neq -\mathbf{F}_{ji} \quad (8)$$

in contradiction with Newton's third law and conservation of momentum, as may be expected for an interaction based on gaze [16]. It is possible to show that the centre of mass of the  $(i, j)$  system<sup>3</sup> is accelerated by purely internal forces, with

$$\dot{V}_x^\eta = -\eta \frac{2\pi}{r} C_\theta \cos \theta, \quad \dot{V}_y^\eta = \eta \frac{2\pi}{r} C_\theta \sin \theta. \quad (9)$$

<sup>2</sup>So that the statistical distributions of  $r$  and  $\theta$  will be independent, as the velocity and position in a classical statistical gas.

<sup>3</sup>Here we assume  $0 < \theta \leq \pi$  to be the angle giving the position of the pedestrian on the right.

On the other end, the relative dynamics is given by a Newtonian potential

$$\dot{\mathbf{v}} \equiv \ddot{\mathbf{r}}_i - \ddot{\mathbf{r}}_j = -2 \nabla U^0(\mathbf{r}). \quad (10)$$

We expect this model to describe correctly pedestrian behaviour close to potential minima. In a wide, low density environment pedestrians should be close to these minima, and we may model the interaction with the environment using white noise  $\Xi$  with standard deviation  $\sigma$ . Using the Social Force Model framework [17], we assume pedestrians to be dragged towards the goal with acceleration<sup>1</sup>

$$\mathbf{F}_i^g = \kappa(\mathbf{v}_p - \mathbf{v}_i), \quad \mathbf{v}_p = v^{(1)}\hat{\mathbf{g}}. \quad (11)$$

As a result the dynamics of the centre of mass for a 2 people group is, ignoring stochastic terms,

$$\dot{\mathbf{V}} = \kappa(\mathbf{v}_p - \mathbf{V}) + \dot{\mathbf{V}}^\eta, \quad (12)$$

while the relative dynamics is given by the stochastic equation

$$\dot{\mathbf{v}} = -\kappa\mathbf{v} - 2 \nabla U^0(\mathbf{r}) + \Xi. \quad (13)$$

The probability distribution function for the relative distance between pedestrians in a group of 2 is given by the Boltzmann distribution

$$\rho(\mathbf{r}) \propto \exp(-\beta U^0(\mathbf{r})). \quad (14)$$

## 2.2 Consequences of the model

In the model above we assumed the interaction between the two pedestrians to be determined by potentials with the same functional form, a point that we will better study in this work. Under this assumption, the equilibrium configuration is necessarily an abreast one, as determined by eq. (10), in which  $\eta$  does not appear. The effect of the non-Newtonian interaction is anyway observable, since the two pedestrians are not in their most comfortable configuration and their velocity is slowed down (assuming  $\eta < 0$ , as found by comparison to the data) by the *load of interaction*

$$\Delta v^{(2)} \equiv v^{(2)} - v^{(1)} = \eta C_\theta \frac{2\pi}{r\kappa} \equiv \frac{\Delta a^{(2)}}{\kappa}, \quad (15)$$

$v^{(2)}$  being the velocity of a group of two interacting pedestrians.

In [1] we assumed the potential to act only between first neighbours. Assuming this to be true, if 3 pedestrians were walking in an abreast formation, the central one would be slowed down by a factor  $2\Delta a^{(2)}$ , compared to the factor  $\Delta a^{(2)}$  of the pedestrians on the wings. As a result, the pedestrians walk in a “V” formation (the central one being on the rear), with velocity

$$\Delta v^{(3)} \equiv v^{(3)} - v^{(1)} \approx \frac{4}{3} \eta C_\theta \frac{2\pi}{r\kappa} = \frac{4}{3} \Delta v^{(2)}. \quad (16)$$

<sup>1</sup>We use the value  $\kappa = 1.52 \text{ s}^{-1}$  from [18].  $v^{(1)}$  is the preferred velocity of pedestrians when walking alone.

## 2.3 Calibration and validation

We compared these predictions with the behaviour of actual pedestrians, tracked using 2D laser range sensors [19] in a pedestrian facility in Osaka, and whose group relations were identified by two human coders. The environment did fit well to our hypotheses by being relatively large (a corridor of  $\approx 6\text{-}7$  meters width) and at low density, ( $\approx 0.03 \text{ ped/m}^2$ ). The model agreed in a qualitative and quantitative way with observations, both regarding the group structure and the group velocity. In particular, given the individual pedestrian velocity  $v^{(1)} = 1.336 \pm 0.002 \text{ m/s}$ , and the two people group velocity  $v^{(2)} = 1.159 \pm 0.006 \text{ m/s}$ , the model predicts  $v^{(3)} = 1.098 \text{ m/s}$ , in agreement with the observed value  $v^{(3)} = 1.110 \pm 0.016$ . Fig. 2 shows, in logarithmic scale, a comparison between the empirical and modelled probability distribution functions for 2 pedestrian groups (left), and 3 pedestrian groups (right).

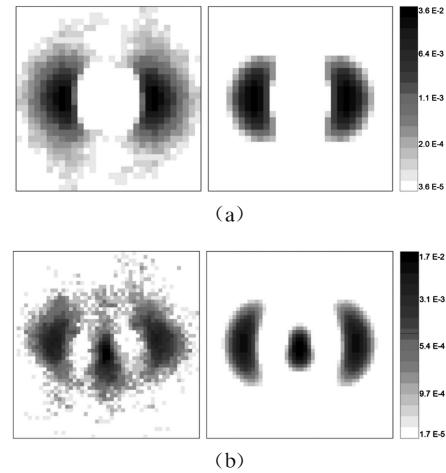


Fig. 2 (a) comparison, in logarithmic scale, between the empirical (left) and modelled (right) probability distribution function for the position of pedestrians in a 2 people group (positions are given in the centre of mass frame, the goal is given by the y axis). (b) comparison, in logarithmic scale, between the empirical (left) and modelled (right) probability distribution function for the position of pedestrians in a 3 people group (same referential frame as (a)).

## 2.4 New evidence for non-Newtonian gazing interaction

If the slower velocity of groups is due to the  $\eta$  term in the potential, in cases in which only a pedestrian is looking at the other, we should see an asymmetric situation, with the gazing pedestrian walking on the rear. We asked coders to analyse cases in which only one of the pedestrians was watching the other, and our preliminary analysis confirms the prediction (Fig. 3).

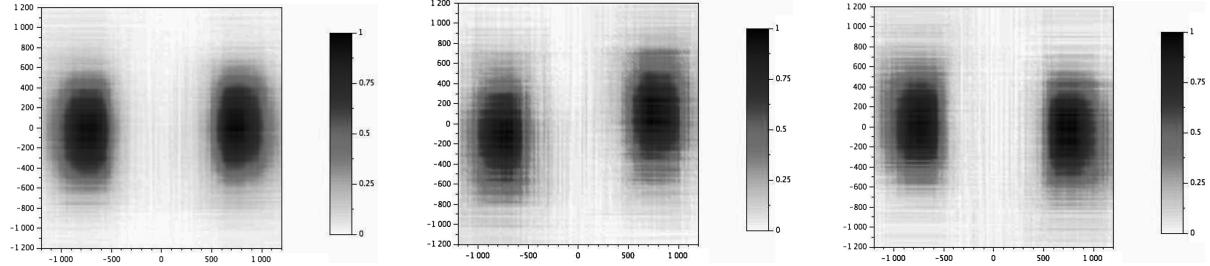


Fig. 3 Comparison between the empirical probability distribution functions for the position in a 2 people group for pedestrians that are: gazing at each other (left); only the pedestrian on the left gazes at the one on the right (centre); only the pedestrian on the right gazes at the one on the left (right).

### 3 The effect of density

In [2] we presented a large amount of data regarding the change in group shape and velocity with crowd density, and in [12] we proposed a mathematical model that may reproduce and explain this behaviour.

#### 3.1 Definition of observables

To analyse how group behaviour changes with density we studied, along with the group velocities  $v^{(2)}$  and  $v^{(3)}$ , the group extension along and orthogonal to the direction of motion.

We first define, for a group of  $n_g$  pedestrians, the position relative to the group centre

$$\mathbf{r}_i \equiv \mathbf{x}_i - \mathbf{X}, \quad \mathbf{X} \equiv \frac{\sum_{i=1}^{n_g} \mathbf{x}_i}{n_g}. \quad (17)$$

We assume that the goal of the group is identified by the group velocity

$$\hat{\mathbf{g}} = \frac{\mathbf{V}}{V}, \quad \mathbf{V} \equiv \frac{\sum_{i=1}^{n_g} \mathbf{v}_i}{n_g} \quad V = |\mathbf{V}| \quad (18)$$

and compute for each pedestrian the clockwise angle  $\theta_i$  between  $\hat{\mathbf{g}}$  and  $\mathbf{r}_i$ . Finally, we define the projections of each  $\mathbf{r}_i$  along the goal and orthogonal to it

$$y_i \equiv r_i \cos \theta_i, \quad x_i \equiv r_i \sin \theta_i. \quad (19)$$

Pedestrians are then re-numbered such as

$$x_1 \leqslant x_2 \leqslant \dots \leqslant x_{n_g} \quad (20)$$

The observables are those features that we verified to change with density in [2], namely, along with the group velocity  $V = v^{(2)}, v^{(3)}$ , the 2 and 3 people abreast extension, and the 2 and 3 people extension in the direction of motion (see also Fig. 1 (b))

$$\begin{aligned} x_{g2} &\equiv x_2 - x_1, & y_{g2} &\equiv y_2 - y_1, \\ x_{g3} &\equiv x_3 - x_1, & y_{g3} &\equiv (y_3 + y_1)/2 - y_2. \end{aligned} \quad (21)$$

#### 3.2 The model

We assumed that the effect of crowd density is a linear recall force with components

$$\begin{aligned} F_i^x &= -K^x(\rho) \frac{x_i}{r_0^2}, \\ F_i^y &= -K^y(\rho) \frac{y_i}{r_0^2}, \end{aligned} \quad (22)$$

$$K^{x,y}(\rho) \geqslant 0$$

or, equivalently, given by the potential

$$U_{\text{macro}}(r, \theta) \equiv \frac{1}{4} \left( K^x(\rho) \frac{r^2 \sin^2 \theta}{r_0^2} + K^y(\rho) \frac{r^2 \cos^2 \theta}{r_0^2} \right). \quad (23)$$

#### 3.3 Calibration and second order interaction

The data calibration and evaluation was based on the data set [20], obtained through an automatic tracking system [21] and analysed by a human coder to provide the ground truth for social interactions. The calibration has been performed by choosing the parameters that better reproduced the  $\rho$  dependence of  $v^{(2)}$  and  $x_{g2}$ , which resulted to be

$$\begin{aligned} K^y(\rho) &\approx 0, \\ K^x(\rho) &\approx \beta \rho, \\ \beta &= 2.7m^4 \text{ ped}^{-1} s^{-2}. \end{aligned} \quad (24)$$

Namely, the effect of crowd density may be modelled as a harmonic term only in the  $x$  direction.

We then compared the prediction of the model regarding the 3 people observables with the data. The agreement was very good concerning  $v^{(3)}$  and  $y_{g3}$ , but poor with respect to  $x_{g3}$ .

This poor reproduction of the 3 people group width was a problem that we had already identified in [1], and suggested that it may due to our choice of ignoring any interaction between second neighbours. We verified that by introducing a force between pedestrians on the wings

$$\mathbf{F}^{\text{second}} = \alpha \frac{C_r}{r_0} \left( \frac{r_0^2}{r^2} - 1 \right) \frac{\mathbf{r}}{r}, \quad (25)$$

where  $\mathbf{r}$  is the distance between pedestrians 1 and 3, and  $\alpha$  was numerically calibrated to  $\alpha = 0.558$ , the agreement between empirical data and model could be largely improved (Fig. 4).

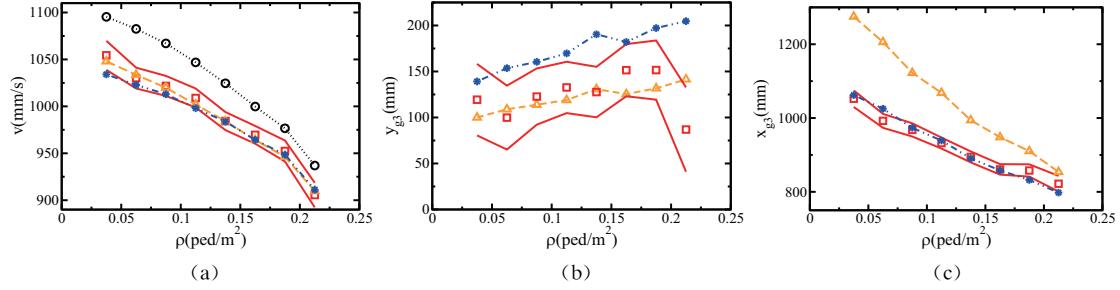


Fig. 4 (a)  $\rho$  dependence of  $v^{(3)}$  (red squares, confidence intervals in continuous line: empirical average; dashed orange and triangles: model prediction in absence of second order interactions; dashed-dotted blue and stars: model prediction using the second order interaction of eq. 25; dotted black and circles shows the empirical  $v^{(2)}(\rho)$  ). (b)  $\rho$  dependence of  $y_{g3}$  (red squares; empirical average; dashed orange and triangles: model prediction in absence of second order interactions; dashed-dotted blue and stars: model prediction using the second order interaction of eq. 25). (c)  $\rho$  dependence of  $x_{g3}$  (red squares: empirical average; dashed orange and triangles: model prediction in absence of second order interactions; dashed-dotted blue and stars: model prediction using the second order interaction of eq. 25).

### 3.4 Phase transitions at high densities

One of the interesting features of the model is its prediction of density dependent “phase transitions” in the group configuration. These phase transitions may be identified as the change (“symmetry breaking”) in the number of maxima assumed by the  $y_{g2}$  distribution (one when pedestrians walk abreast, two when the walk in a line) and by the  $y_{g3}$  distribution (one maximum when only the “V” configuration is present, two maxima when also the “ $\Lambda$ ” configuration is present, and three maxima when pedestrians walk in a line). The number of maxima predicted by the model is shown in Fig. 5. The V-  $\Lambda$  transition has been qualitatively observed in the data.

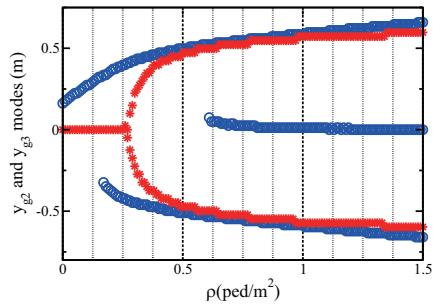


Fig. 5 Red stars: position of the  $y_{g2}$  distribution maxima as a function of  $\rho$ . Blue circles: position of the  $y_{g3}$  distribution maxima as a function of  $\rho$ .

## 4 The effect of group composition

### 4.1 Method

We asked 3 different “coders”, i. e. people not aware of the purpose of our study, to examine video-recordings corresponding to a few hours of our pedestrian group data sets, and to mark pedestrians in groups according to their apparent gender, age and purpose for

visiting the area (work or leisure). They were also asked to specify their apparent social relation, such as family members, couple<sup>1</sup>, friends and colleagues. All the coders were Japanese nationals, and, although their coding does not provide any objective knowledge regarding group composition, it should represent a reliable source of information, which may be complemented with the height of pedestrians, measured by our tracking system [21]. In this preliminary study we used only the observation of a single coder, an experienced non-technical member of our staff that already contributed to the group coding used in [1]. Furthermore, we used only information regarding the relation, purpose and gender composition<sup>2</sup> of two people groups. The comparison between the different coders, the analysis of larger groups, and of the effect of continuous variables such as height and age is left for an upcoming journal paper.

#### 4.1.1 Observables

We used as observables the group velocity  $V = v^{(2)}$  (eq. 18), the distance between pedestrians  $r$  and the abreast distance  $x = x_{g2}$  (eq. 21).

For each observable  $o$  we compute the average  $\mu_i$  for each group  $i$ , and then provide its average value as

$$\langle o \rangle \pm \epsilon, \quad \langle o \rangle = \frac{\sum_{i=1}^N \mu_i}{N}, \quad \epsilon = \frac{\sigma}{\sqrt{N}}, \quad \sigma = \sqrt{\sqrt{\frac{\sum_{i=1}^N \mu_i^2}{N}} - \langle o \rangle^2} \quad (26)$$

where  $N$  is the number of groups corresponding to each

<sup>1</sup>The Japanese word used, koibito, usually designs an unmarried, young couple.

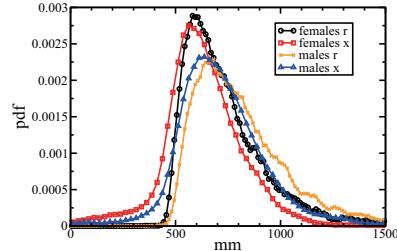
<sup>2</sup>We studied all female vs all males groups. Mixed groups behaviour is extremely different between, for example, couples and colleagues, and its analysis is left for future work.

category (females or males, etc.).

## 4.2 Results

### 4.2.1 The effect of gender

Table 1 compares the values of all observables between groups composed by two males and groups composed by two females, while Fig. 6 on the left shows the



probability distributions of the corresponding spatial variables.

**Table 1** Observable dependence on gender for 2 people groups.

	<i>N</i>	<i>V</i>	<i>r</i>	<i>x</i>
Females	114	$1065 \pm 22$ mm/s	$766 \pm 21$ mm	$631 \pm 10$ mm
Males	256	$1259 \pm 11$ mm/s	$836 \pm 12$ mm	$728 \pm 9$ mm

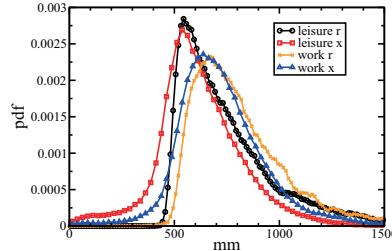


Fig. 6 Left: probability distribution function for the *r* and *x* variables in the all females and all males groups.

Right: Probability distribution function for the *r* and *x* variables in the groups whose purpose was leisure or work.

### 4.2.2 The effect of purpose

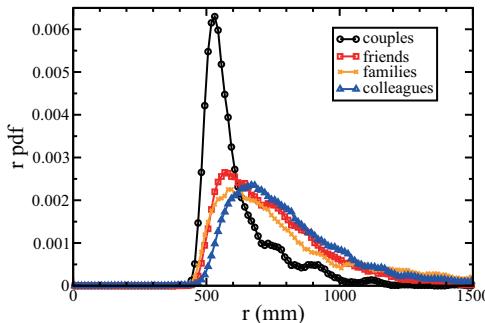
Table 2 compares the values of all observables between groups whose apparent purpose was leisure and groups whose apparent purpose was work, while Fig. 6 on the right shows the probability distributions of the corresponding spatial variables.

**Table 2** Observable dependence on purpose for 2 people groups.

	<i>N</i>	<i>V</i>	<i>r</i>	<i>x</i>
Leisure	276	$1071 \pm 13$ mm/s	$806 \pm 17$ mm	$624 \pm 9$ mm
Work	274	$1256 \pm 10$ mm/s	$845 \pm 13$ mm	$731 \pm 9$ mm

### 4.2.3 The effect of relation

Table 3 compares the values of all observables between groups whose apparent relation was: couples, friends, family or colleagues; while Fig. 7 shows the probability distributions of the corresponding spatial variables.



**Table 3** Observable dependence on relation for 2 people groups.

	<i>N</i>	<i>V</i>	<i>r</i>	<i>x</i>
Couples	48	$1068 \pm 29$ mm/s	$644 \pm 19$ mm	$597 \pm 19$ mm
Friends	112	$1069 \pm 22$ mm/s	$785 \pm 18$ mm	$654 \pm 15$ mm
Families	104	$1055 \pm 17$ mm/s	$898 \pm 35$ mm	$609 \pm 14$ mm
Colleagues	280	$1253 \pm 10$ mm/s	$842 \pm 13$ mm	$727 \pm 9$ mm

## 4.3 Discussion

We may see that gender has a significant influence on group velocity and pedestrian distances, with females walking slower and closer than males. A similar statement can be done for purpose, with workers walking significantly faster and at a larger distance than people visiting the area for leisure. It may be nevertheless noticed that while the difference in abreast distance *x* corresponds to a few confidence values  $\epsilon$ , such a difference is more reduced for the absolute distance *r*.

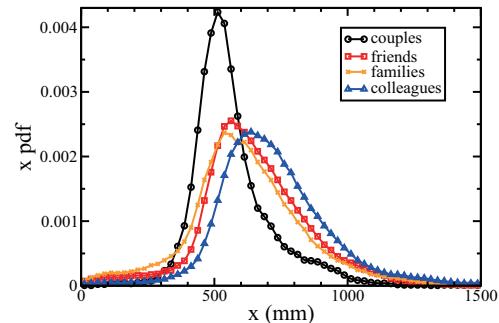


Fig. 7 Probability distribution function for the *r* (left) and *x* (right) variables in groups depending on their relation.

Regarding relation between pedestrians, we may see that couples, friends and family members walk at similar velocities, while colleagues walk much faster, suggesting that purpose affects velocity more than relation. Relation has, on the other end, a strong effect on distance. Couples walk very close and abreast (the  $x$  pdf assumes almost zero under 0.3 meters, suggesting that couples are almost always abreast), while friends walk at a larger distance but much closer than colleagues. Families have peak distributions similar to friends, but have also a strong tendency not to walk abreast, due probably to the erratic behaviour of children.

There is clearly a strong overlapping between, for example, the populations of colleagues, workers and males. In order to better understand the contribution of these factors, in our upcoming work we will further break up these categories (“leisure oriented males”, etc.).

## 5 Conclusion

In this paper we exposed our mathematical theory of pedestrian group behaviour, provided new evidence regarding the non-Newtonian nature of pedestrian interactions, and performed a preliminary analysis, based on empirical observations, on the effect of group composition on dynamics. We observed that females walk slower and closer than males, that workers walk faster, at large distance and more abreast than leisure oriented people, and that inter group relation has a strong effect on group structure, with couples walking very close and abreast, colleagues walking at a larger distance, and friends walking more abreast than family members.

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