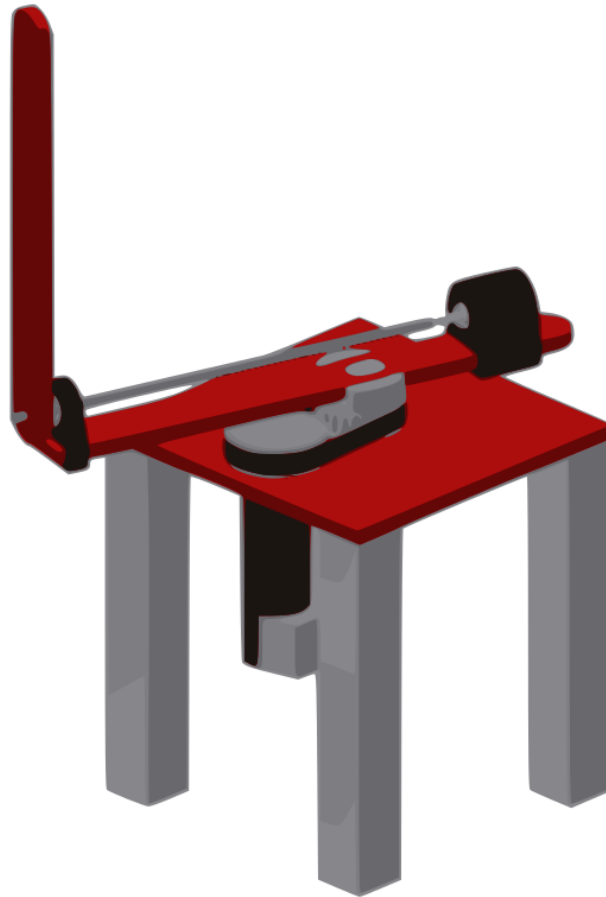


UNIVERSITY OF COLORADO AT BOULDER

MASTER'S PROJECT



Furuta Pendulum

ASEN 5115 :: Mechatronics

Authors:

Zachary VOGEL

Maurice WOODS



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Contents

1 Introduction

The inverted pendulum is the staple of any controls-based engineering curriculum; by displacing a cart from which a pendulum hangs, one can easily derive a controller that will swing-up and balance the pendulum in the upright position. Here, we've explored a modified system, where the linearly-displaced cart is replaced by a rotating armature, from which hangs our pendulum. We will construct a benchtop model and design a custom controller to balance the pendulum based on its specific inertial characteristics.

2 Model

To begin, our research referenced a paper by mechanical engineering students in an Advanced System Dynamics and Control course at MIT titled "Furuta Pendulum", written in Fall 2013. In the paper, students characterized a futura pendulum of their own design and design a controller based of the mechanics they derive for the system. Following the model and general concepts of that team we designed and built our own system. We chose not to write down the values the equations that fill in the state equations, the group from MIT used symbolic variables in Matlab to find the solution.

3 Hardware and System Identification

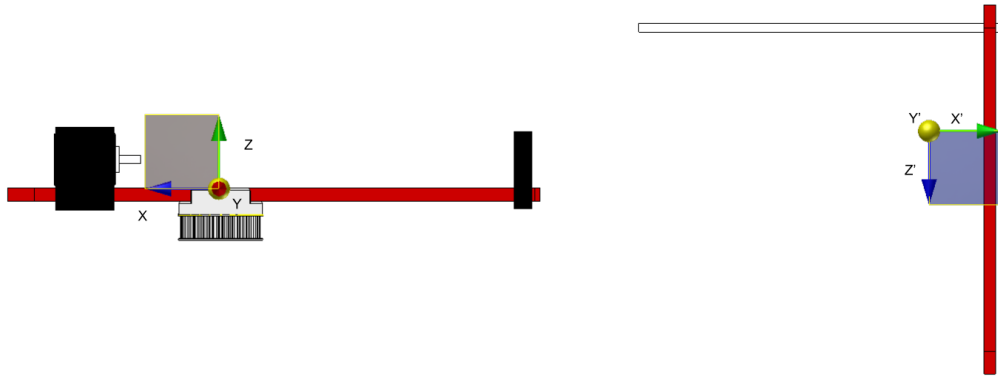
To begin, we were provided a collection of incomplete legacy hardware, used by a past team to construct a Furuta Pendulum. Ultimately, only the drive motor and the legs of the pendulum stand were reused as the remaining hardware was unusable. The revised pendulum eliminated the encoder cable by incorporating a slip ring, allowing the pendulum to spin without limit. Because the slip ring replaced the motor as the pendulum's pivot, the motor was displaced, requiring a timing belt/pulley assembly to transfer torque to the pendulum.

The pendulum's motion is controlled by a Teensy 3.2 microcontroller which senses the displacement of two rotary encoders (one that measures the rotation of the motor and one that measures the rotation of the pendulum rod), both quadrature. The Pittman brushed DC motor is controlled using a Pololu high power motor driver which is provided a PWM signal by the microcontroller. The motor is rated to 19V (however the motor controller is rated to 18V) and the remaining hardware is rated to 5V, so two power supplies are used to provide these two voltage levels to their respective components.

In order to accurately calculate the inertial parameters used to apply the controller to our specific pendulum, we used Autodesk Inventor CAD software to determine the center of mass and moment of inertia for each arm of the Furuta pendulum. In doing so, we found the following parameters:

$m_1 =$	0.107kg	$m_2 =$	0.077kg
$l_1 =$	0.15m	$l_2 =$	0.19m
$c_{x1} =$	0.0m	$c_{2x} =$	0.125m
$c_{y1} =$	0.0m	$c_{2y} =$	0.0m
$c_{z1} =$	0.0m	$c_{2z} =$	0.0544m
		$I_{2xx} =$	0.0003035 kg m ²
		$I_{2yy} =$	0.0005484 kg m ²
$I_{1zz} =$	0.0005622 kg m ²	$I_{2zz} =$	0.0002499 kg m ²
		$I_{2xz} =$	0.000146 kg m ²

Table 1: Parameters for our Furuta pendulum. The subscript ₁ refers to the drive arm (left figure below) and the subscript ₂ refers to the pendulum arm (right figure below). CoM distances are measured from the pivot point of the drive arm. Below, the coordinate frame and centers of mass are labeled.



To find the correct damping coefficient for the inverted pendulum rod, we needed to take data directly from the system. This was accomplished with some of the code in the Appendix. We utilized the prebuilt encoder library and the micro function call to find the rod position at a given time. Then we held the top rod still and gave it a tap. Print all that data nicely formatted over to Matlab, take the maximum and multiply by a few constants as seen in a section of the Matlab code, and you have the desired damping value.

Refer to the Bill of Materials, linked in the Appendix for more information on the parts used and pictures of the hardware.

4 Analysis and Simulation

Finally having identified all of our systems values, we needed to see what the response of our system looked like in simulation and design a controller or two from there. We took the state space equations directly from the "Furuta Pendulum" group at MIT[1]. Once calculated with our values and lack of

a current sensor the state space equations became:

$$\begin{bmatrix} \theta_1 \\ \theta_2 \\ \dot{\theta}_1 \\ \dot{\theta}_2 \\ i \end{bmatrix} = \dot{\mathbf{x}} = \begin{bmatrix} 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 16.69 & -1.079 & -0.01476 & 9.729 \\ 0 & 53.20 & -0.7660 & -0.07886 & 6.908 \\ 0 & 0 & -11.33 & 0 & -1860 \end{bmatrix} \begin{bmatrix} \theta_1 \\ \theta_2 \\ \dot{\theta}_1 \\ \dot{\theta}_2 \\ i \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 666.6 \end{bmatrix} \mathcal{V}$$

$$\begin{bmatrix} \theta_1 \\ \theta_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \end{bmatrix} \mathbf{x} + \begin{bmatrix} 0 \\ 0 \end{bmatrix} \mathcal{V}$$

Having recently been in Digital Control I, Zach, decided to design a fully digital controller. Thus I converted the system to discrete time with a sample rate that was 40 times the fastest pole frequency. That turned out to be $T = 0.003500\text{sec}$ at one point in the design process and we stuck with that for the rest of the project. With that decided the discrete time equations converted to modal form where:

$$\mathbf{x}(kT + T) = \mathbf{F}\mathbf{x}(kT) + \mathbf{G}u(kT) = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1.025 & 0 & 0 & 0 \\ 0 & 0 & 0.9742 & 0 & 0 \\ 0 & 0 & 0 & 0.99692 & 0 \\ 0 & 0 & 0 & 0 & 0.001489 \end{bmatrix} \mathbf{x}(kT) + \begin{bmatrix} 0.0429 \\ 0.03188 \\ -0.04185 \\ 0.005669 \\ 0.3581 \end{bmatrix} u(kT)$$

$$y(kT) = \begin{bmatrix} 0.25 & 0.00468 & 0.005635 & -0.1875 & 0.000002812 \\ 0 & 0.0167 & 0.01591 & 0.002542 & 0.000001997 \end{bmatrix} \mathbf{x}(kT) + \mathbf{0}u(kT)$$

As can be seen, the system has one marginally stable pole at 1 and one unstable pole at 1.025. Without any kind of feedback the step response of course just blow up. This can be seen in the root locus of the system as well. At this point we decided to move the poles arbitrarily to 0.99, 0.998, 0.95, 0.97, 0.0015 and the observer poles to -0.01, -0.05, 0.951, 0.97, 0.0. We ended up playing around with a bunch of values based on the Simulink results to no avail as regardless of if the simulation worked it still failed. Those are the values that gave the rest of the results in this section though.

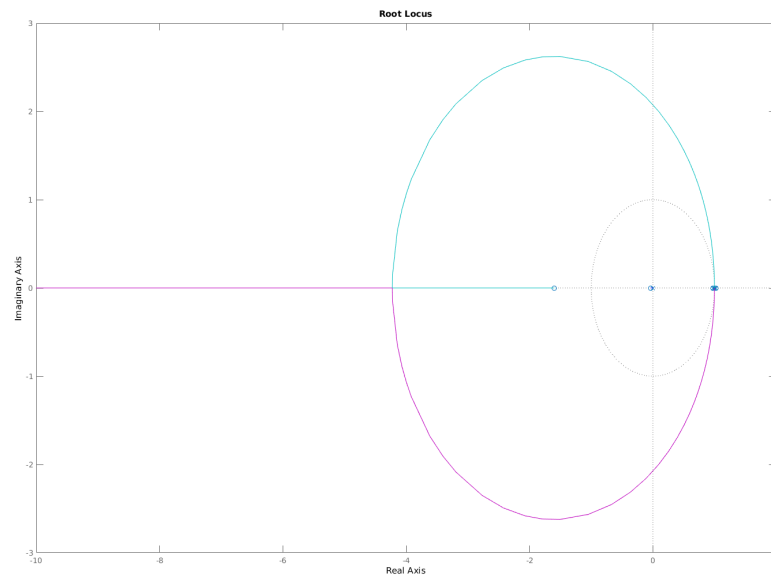


Figure 1: Root Locus of the System

With the values finally set, we implemented a Simulink model with the following diagram taken from Lucy Pao's Digital Control class. The diagram can be seen below. As well as all of the corresponding plots. The response is generally what we wanted. Unfortunately that didn't translate later. The feed in matrices were calculated based on the reference effecting the motor, then the rod would stabilize.

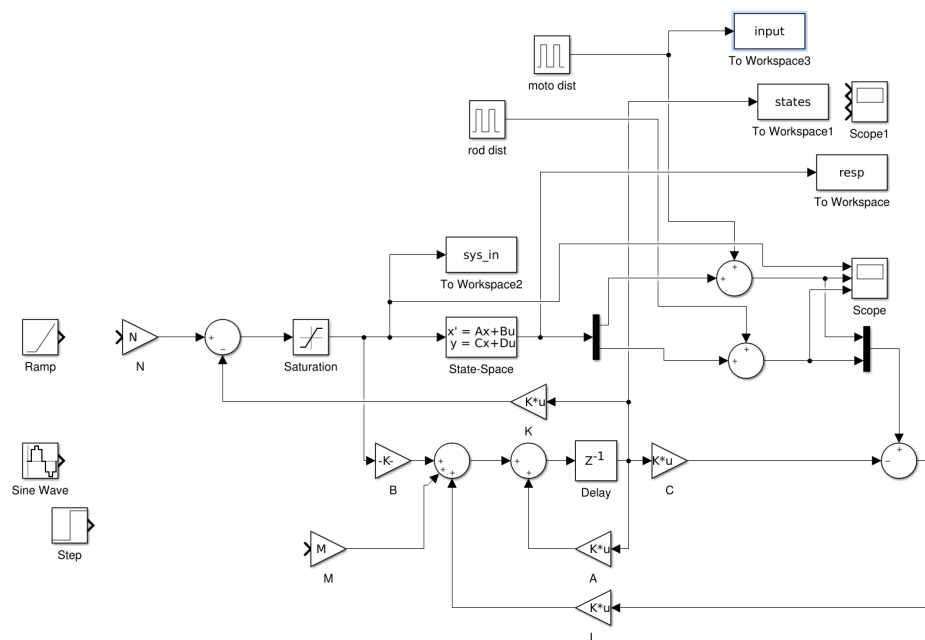


Figure 2: Since

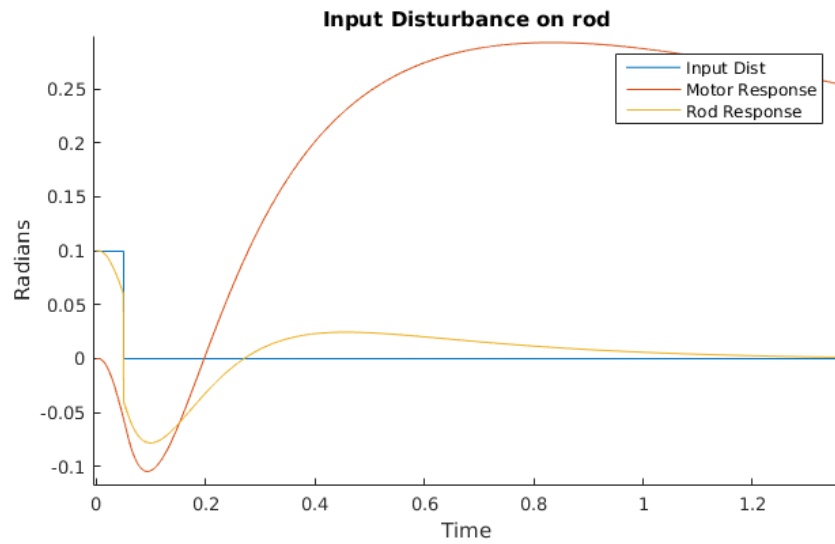


Figure 3: As you can see, a light tap on the rod provides a cool response in sim.

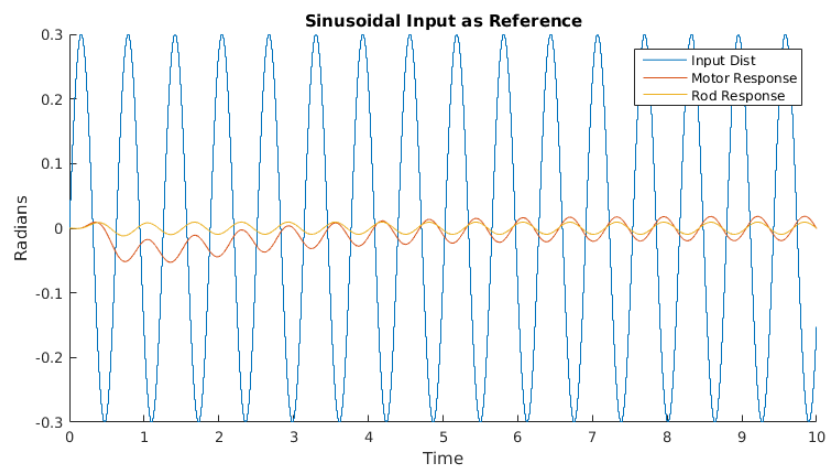


Figure 4: Theoretically should have been able to make a cool oscillatory motion too.

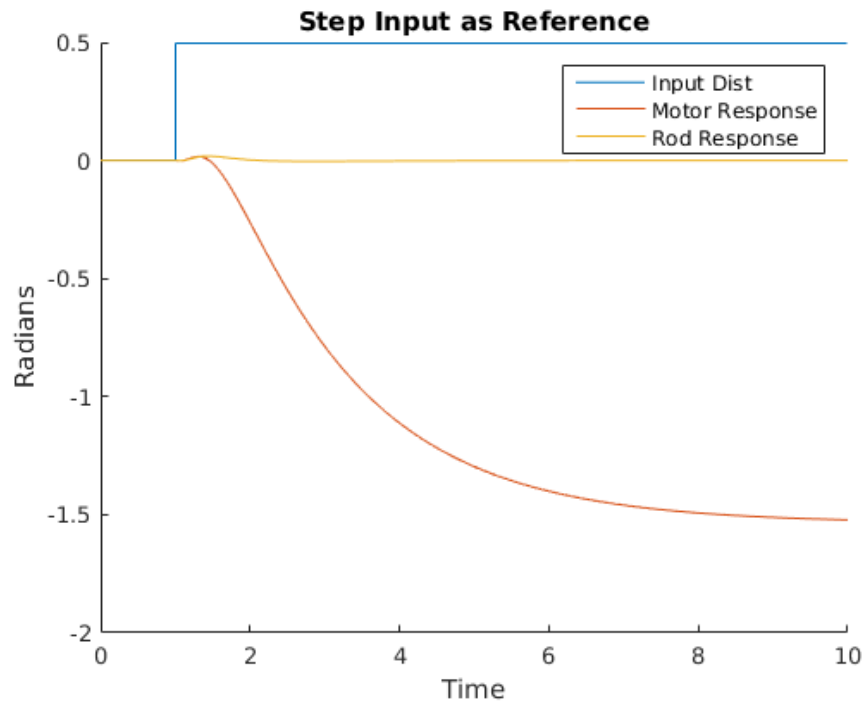


Figure 5: Here we see the step response, which also manages to keep balance.

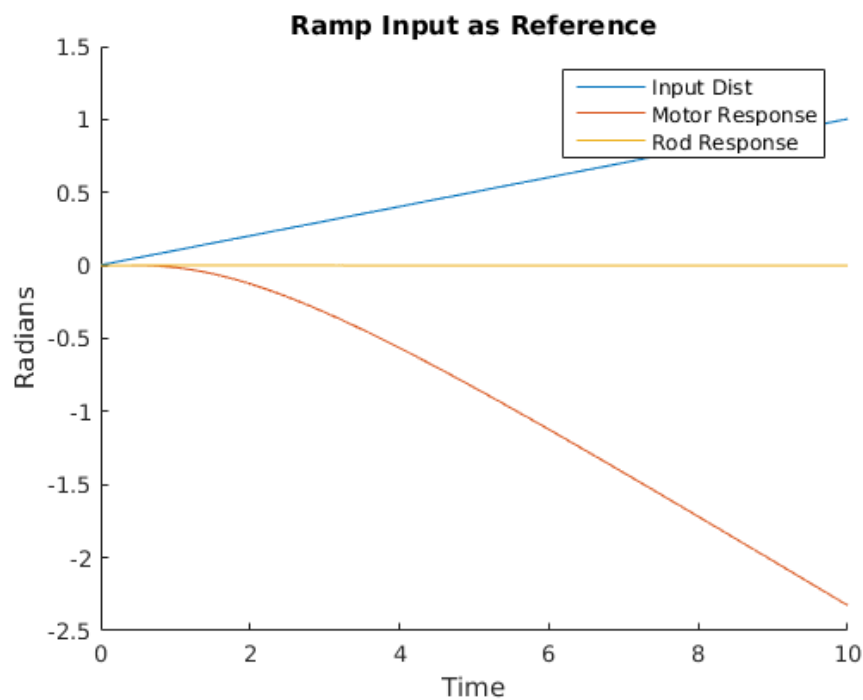


Figure 6: Finally the ramp input, which should keep it spinning slowly indefinitely.

Since the observer ended up not working, we designed a PID quickly using PID Tuner. The figure below shows its disturbance rejection. The values were $K=98.936$, $K_d=6.6904$, and $K_i=348.9383$. We just tuned this till it looked about right and those were the values we ended with. Certainly not a robust controller by any means.

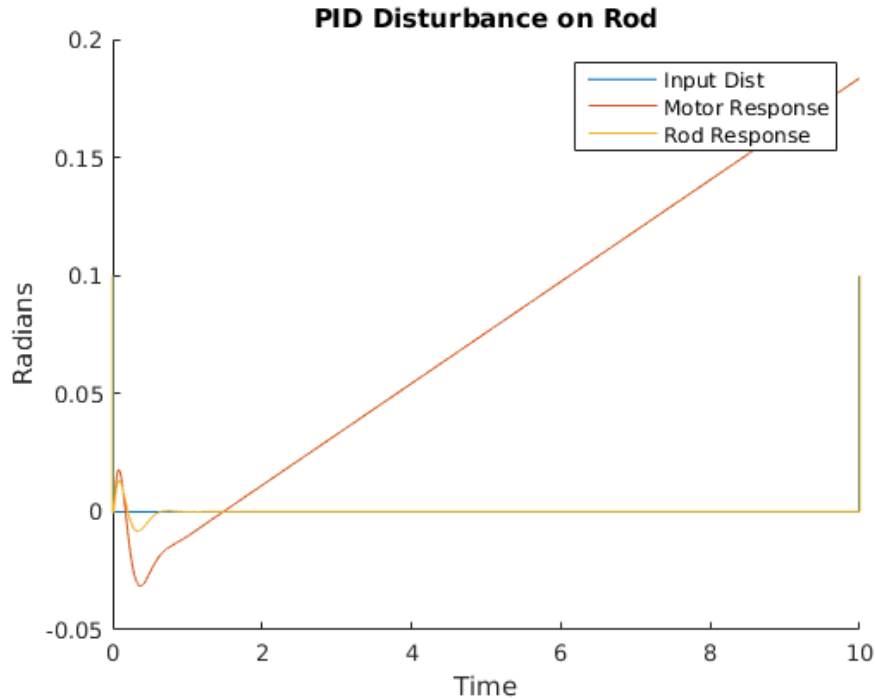


Figure 7: The observer model in Simulink

5 Implementation

The code mainly consists of two Real-Time Operating System Tasks. The first, which determines the two output states based on the encoder pulses and drives the motor. The second, which runs the controller that takes in the output states and outputs the encoder pulses. These are protected with binary Semaphores. The encoder pulses for both sets of encoders are kept track of by four interrupts implemented in the Teensy encoder library. Similarly, we use the timer library to implement an interrupt that tells us when to run our tasks. These tasks would be prevented from running by another set of binary semaphores, but that seemed to cause a hard fault on the microcontroller. This could be seen by the microcontroller moving to the Hard fault interrupt which is an infinite loop that blinks the LED.

The matrix math for the controller is done with two dimensional arrays and proper indexing. Most of the values are floats, but that is converted to an integer, so that it can be used with the PWM. The PWM pin that drives the motor has a 16 bit resolution up to 65535. Given our 18.1 volt motor that gives an easy conversion. The encoder outputs are similarly converted to radians using the ticks per cycle.

6 Results

We began testing with the state observer. This didn't work at all either due to the instability in the growth of the states due to improper matrix multiplication, or instability in the controller. We know this because the floating point numbers defining the states in the c code blew up to the maximum floating point value relatively quickly. Could also be the modeling of the system dynamics or the system identification, specifically the damping coefficient. Since this wasn't working and Zach didn't really know how to go about fixing the observer design, that is where it ended for now. The PID

controller kind of work and considering Zach implemented it Thursday morning it looked alright. This can be seen in the video that is inside the zip file with this report (link provided in the Appendix).

7 Final Thoughts and Further Work

While the centerpiece of this project is the controller, which is responsible for making the pendulum an interesting and eye-catching demonstration piece, the assembly has the added benefit of being built from materials that are readily available, relatively inexpensive, and easily modified, making it ideal for an small academic research project. With more financial resources, the model could be improved to incorporate more sensors for monitoring the motion of the pendulum and the effects of the motor while also considering nonlinear effects. We would also be able to construct a more stable platform from aluminum to minimize vibrations and disturbances, and implement a better controller like a linear quadratic regulator or Kalman filter. Throughout the project we have applied knowledge learned from other classes to a problem and although the controller didn't work properly we were able to garnet a lot of experience from implementing the various parts of this project.

8 References

- [1] Andrew Careaga Houck, Robert Kevin Katzschmann, Joao Luiz Almeida Souza Ramos. "Furuta Pendulum". Massachusetts Institute of Technology, Department of Mechanical Engineering, 2.151 Advanced System Dynamics & Control, 2013.

9 Appendix

9.1 Links and Files

Here we provide links to a video of the performance of the pendulum, as well as a repository of the CAD models used to design and assemble the mechanical model.

- [CAD Files](#)
- [Demonstration Video](#)

9.2 Matlab Code

```

1 %Zachary Vogel
2 %Real design of Control
3
4 %be clear that the first state is the motor angle
5 %second is the rod angle
6 %third and 4th are their derivatives
7 %fifth is motor current
8
9
10 %actual known values
11 g=9.8;%m/s^2 gravity
12 Rm=2.79;%ohms terminal resistance
13 kt=0.017;%Nm/A torque constant
14 Lm=.0015;%milli Henries, motor inductance
15 Jm=1.62*10^(-6);%kgm^2 motor inertia
16
17 %values from paper, need to find these before actual
    implementation
18
19 m1=0.107;%mass of first rod?
20 m2=0.077;%mass of second rod?
21 L1=0.125;%length from motor shaft to center of mass of motor rod+
    inverted pendulum rod
22 l1=0.0;%length from motor shaft to Center of mass of motor rod
23 L2=0.195;%length of inverted pendulum rod
24 l2=0.0544;%length from plane of motor rod to center of mass of
    motor rod+inverrted pendulum
25 %b1=6.0*10^(-4);%damping 1
26 b1=6.0*10^(-4)*pi;%viscous damping is 1.34*10^(-6)*pi
27 %b2=0.000109468513065094;%damping 2 from system id
28 b2=3.63316395*10^(-5);
29 %Inertia tensors are a 3 element vector of torques in 3 rotational
30 %directions equal to a 3X3 matrix of inertias times a 3 element
    vector of
31 %angular accelerations.

```

```

32
33 I1z=0.00056216; %Izz Inertia only one from
34 I2x=0.0003035; %other inertias , measured in CAD
35 I2y=0.0005484;
36 I2z=0.0002499;
37 I2xz=0.0001463;
38
39 den=( I2x*I1z-I2xz^2+I2x*I2z+I2x*L1^2*m2+I2x*l1^2*m1+I1z*l2^2*m2+
      I2z*l2^2*m2+2*I2xz*L1*l2*m2+l1^2*l2^2*m1*m2);
40
41 A11=0;
42 A12=-(g*l2*m2*( I2xz-L1*l2*m2))/den;
43 A13=-(b1*(m2*l2^2+I2x))/den;
44 A14=(b2*( I2xz-L1*l2*m2))/den;
45 A15=( kt*(m2*l2^2+I2x))/den;
46
47 A21=0;
48 A22=(g*l2*m2*(m2*L1^2+m1*l1^2+I1z*I2z))/den;
49 A23=(b1*( I2xz-L1*l2*m2))/den;
50 A24=-(b2*(m2*L1^2+m1*l1^2+I1z+I2z))/den;
51 A25=-(kt*( I2xz-L1*l2*m2))/den;
52
53 A31=0;
54 A32=0;
55 A33=-kt/Lm;
56 A34=0;
57 A35=-Rm/Lm;
58
59 B1=0;
60 B2=0;
61 B3=1/Lm;
62
63 A=[0 0 1 0 0;0 0 0 1 0;A11 A12 A13 A14 A15;A21 A22 A23 A24 A25;A31
      A32 A33 A34 A35];
64 B=[0;0;B1;B2;B3];
65 C=[1 0 0 0 0;0 1 0 0 0];
66 D=[0;0];
67
68 sys1=ss(A,B,C,D);
69 [Wn, zeta]=damp(sys1);
70 rank(obsv(A,C));
71 wn=min(Wn(Wn>0));
72 Ts=wn/(40*pi);
73 Ts=0.0035;
74 sys=c2d(sys1,Ts);
75 %pzmap(sys)
76 K=place(sys.a,sys.b,[0.99 0.998 0.95 0.97 0.0015])
77 L=place(sys.a',sys.c',[-0.01 -0.05 0.951 0.97 0.0])'

```

```

78
79 NMAT=[ sys . a-diag ([ 1 , 1 , 1 , 1 , 1 ]) , sys . b ; sys . c ( 1 , :) , [ 0 ] ;
80
81 NMAT=inv (NMAT) ;
82
83 r=NMAT* [ 0 ; 0 ; 0 ; 0 ; 0 ; 1 ] ;
84 N=r ( 6 ) +K*r ( 1 : 5 ) ;
85 M=sys . b*N ;
86
87
88 %observer poles
89 F2=sys . a-sys . b*K-L (: , 2 ) *sys . c ( 2 , :) ;
90 G2=L (: , 2 ) ;
91 H2=K ;
92 J2=0 ;
93 [ num1 , den1 ] = ss2tf ( F2 , G2 , H2 , J2 ) ;
94 [ num2 , den2 ] = tf2zp ( num1 , den1 ) ;
95
96
97 F1=sys . a-sys . b*K-L (: , 1 ) *sys . c ( 1 , :) ;
98 G1=L (: , 1 ) ;
99 H1=K ;
100 J1=0 ;
101 [ num3 , den3 ] = ss2tf ( F1 , G1 , H1 , J1 ) ;
102 [ num4 , den4 ] = tf2zp ( num3 , den3 ) ;
103
104 A1=A ;
105 B1=B ;
106 C1=[0 1 0 0 0] ;
107 %C1=C ;
108 %D1=D ;
109 D1=0 ;
110 sys4=ss ( A1 , B1 , C1 , D1 ) ;
111 sysd=c2d ( sys4 , Ts ) ;
112 sysm=canon ( sysd , 'modal' ) ;
113 sysc=canon ( sysd , 'companion' ) ;
114 K1=place ( sysc . a , sysc . b , [ 0 , 0.1 , 0.95 , 0.98 , 0.2 ] ) ;
115 L1=place ( sysc . a , sysc . c ' , [ 0 , 0.05 , 0.95 , 0.96 , 0.1 ] ) ' ;
116
117
118 PIDK=98.936 ;
119 PIDKD=6.6904 ;
120 PIDKI=348.9383 ;

```

9.3 MicroController Code

The code we used to identify the damping factor of the encoder based on the motor.

```

1 || #include <Encoder.h>
2 ||

```

```

3
4 Encoder knobLeft(5, 6);
5 Encoder knobRight(7, 8);
6
7
8 long a=0;
9
10 void setup() {
11     Serial.begin(9600);
12     Serial.println("TwoKnobs Encoder Test:");
13     a=micros();
14 }
15
16 long positionLeft = -999;
17 long positionRight = -999;
18
19
20 void loop() {
21     long newLeft, newRight;
22     newLeft = knobLeft.read();
23     newRight = knobRight.read();
24     if (newLeft != positionLeft || newRight != positionRight) {
25
26         //Serial.print("Left = ");
27         Serial.print(newLeft);
28         Serial.print(",");
29         Serial.print(micros()-a);
30         Serial.print(";");
31         Serial.println();
32
33         positionLeft = newLeft;
34         positionRight = newRight;
35
36     }
37
38     // if a character is sent from the serial monitor,
39     // reset both back to zero.
40     if (Serial.available()) {
41         Serial.read();
42         Serial.println("Reset both knobs to zero");
43         knobLeft.write(0);
44         knobRight.write(0);
45     }
46 }

```

The final code for the state observer with state feedback

```

1 #include <FreeRTOS_ARM.h>
2 #include <Encoder.h>
3
4 // #define ENCODER_USE_INTERRUPTS 1
5 // #define SUPDOG 1
6
7
8 #define MOTOPWM 9
9 #define MOTODIR 10
10 #define MOTOENCL 3
11 #define MOTOENCR 4
12 #define RODENCL 5

```

```

13 #define RODENCR 6
14
15 const float A[5][5]={1.0, 0.0, 0.0, 0.0, 0.0},
16                      {0.0, 1.025, 0.0, 0.0, 0.0},
17                      {0.0, 0.0, 0.9742, 0.0, 0.0},
18                      {0.0, 0.0, 0.0, 0.9969, 0.0},
19                      {0.0, 0.0, 0.0, 0.0, 0.001489}};
20 const float B[]={0.0429,
21                  0.03188,
22                  -0.04185,
23                  0.05669,
24                  0.3581};
25 const float C[2][5]={0.25,0.00468,0.005635,-0.1874,0.000002812},
26                      {0.0, 0.0167,0.01591,0.002542,0.000001997}};
27
28 const float L[5][2]={1.055597, -0.0018567},
29                      {-0.00818119, 1.08129},
30                      {12.875, -0.4049},
31                      {-2.08169, 9.38346},
32                      {-3.3927, -13.125}};
33
34 const float K[]={-1.389,105.456,-3.502506,15.021901,0.03726};
35
36
37 SemaphoreHandle_t sem1,sem2;
38 volatile int run1=0,run2=0;
39
40 //built in encoder interrupts
41 Encoder MotoEnc(MOTOENCL,MOTOENCR);
42 Encoder rodEnc(RODENCL,RODENCR);
43
44 //built in timer interrupt
45 IntervalTimer sampltimer;
46
47 //onl shared variables
48 volatile float ymeas[2]={0.0,0.0};
49 volatile int unew=0;
50
51
52 void TimeSemEnable(void)
53 {
54     //cause giving semaphores throws a fault
55     run1++;
56     run2++;
57 }
58
59
60
61 void Observer(void * params)
62 {
63     float x[]={0.0,0.0,0.0,0.0,0.0};
64     float xnew[5]={0.0,0.0,0.0,0.0,0.0};
65     float utemp=0.0;
66     int utempi=0;
67     float yest[2]={0.0,0.0};
68     float yerr[2]={0.0,0.0};
69     float temp[5];
70     int i;

```

```
71
72 #ifdef SUPDOG
73     int time1=0;
74     int maxtime=0;
75 #endif
76
77     //Serial.println("do I get here");
78     while(1)
79     {
80 #ifdef SUPDOG
81         time1=micros();
82 #endif
83         while(run2==0);
84
85         run2=0;
86
87
88
89         utemp=0;
90         yest[0]=0;
91         yest[1]=0;
92
93
94
95
96         //new state, output state
97         for(i=0;i<5;i++)
98         {
99             x[i]=xnew[i];
100             utemp+=K[i]*x[i];
101             yest[0]+=C[0][i]*x[i];
102             yest[1]+=C[1][i]*x[i];
103         }
104
105         /*Serial.print(yest[0]);
106         Serial.print(",");
107         Serial.println(yest[1]);*/
108
109         //mutex_lock
110         if(utemp>18)
111         {
112             utemp=18;
113         }
114         if(utemp < -18)
115         {
116             utemp=-18;
117         }
118         //Serial.println(utemp,8);
119         utempi=(int)(utemp*65535.0/18.0);
120 /*#ifdef PRINTING*/
121         Serial.print(x[0]);
122         Serial.print(",");
123         Serial.print(x[1]);
124         Serial.print(",");
125         Serial.print(x[2]);
126         Serial.print(",");
127         Serial.print(x[3]);
128         Serial.print(",");
```



```

129         Serial.println(x[4]);
130     /*#endif*/
131     if(utempi>65535)
132     {
133         utempi=65535;
134     }
135     if(utempi<-65535)
136     {
137         utempi=-65535;
138     }
139
140     xSemaphoreTake(sem1,0);
141     unew=utempi;
142     xSemaphoreGive(sem1);
143     //mutex unlock
144
145     //mutex_lock
146     xSemaphoreTake(sem2,0);
147     yerr[0]=ymeas[0]-yest[0];
148     yerr[1]=ymeas[1]-yest[1];
149     //mutex unlock
150     xSemaphoreGive(sem2);
151
152
153
154
155
156
157     for(i=0;i<5;i++)
158     {
159         temp[i]=utemp*B[i]+yerr[0]*L[i][0]+yerr[1]*L[i][1];
160
161     }
162     for(i=0;i<5;i++)
163     {
164         xnew[i]=temp[i]+x[0]*A[i][0]+x[1]*A[i][1]+x[2]*A[i][2]+x[3]*A
            [i][3]+x[4]*A[i][4];
165     }
166
167
168     /*#ifdef SUPDOG
169         time1=micros()-time1;
170         if(time1>maxtime)
171         {
172             maxtime=time1;
173             //Serial.print("Observer max time was");
174             //Serial.println(maxtime);
175         }
176     #endif*/
177
178
179     }
180     //Serial.print("max time after 100000 trialswas");
181     //Serial.print(maxtime);
182     //Serial.println(" in microseconds");
183     while(1);
184 }
185

```

```

186
187
188 void writer(void * params)
189 {
190
191     double ytemp[2]={0.0,0.0};
192     int utemp=0;
193
194 #ifdef SUPDOG
195     int time1=0;
196     int maxtime=0;
197 #endif
198
199
200
201
202     sampletimer.priority(200);
203     sampletimer.begin(TimeSemEnable,3500);
204     //sampletimer.end();
205     while(1)
206     {
207
208 #ifdef SUPDOG
209     time1=micros();
210 #endif
211
212     //mutex_lock
213     while(run1==0)
214     {
215         vTaskDelay(1);
216     }
217     run1=0;
218
219     ytemp[0]=0;
220     ytemp[1]=0;
221
222     ytemp[0]=(float)MotoEnc.read()*0.00349065850398868;
223     ytemp[1]=(float)rodEnc.read()*0.00785398163397448;
224     //Serial.println(ytemp[0]);
225     //Serial.println(ytemp[1]);
226     //mutex_lock
227     xSemaphoreTake(sem2,0);
228     ymeas[0]=ytemp[0];
229     ymeas[1]=ytemp[1];
230     xSemaphoreGive(sem2);
231     //mutex_unlock
232
233     if(ytemp[1]>0.34||ytemp[1]<-0.34)
234     {
235         analogWrite(MOTOPWM,0);
236     }
237     else{
238         xSemaphoreTake(sem1,0);
239         utemp=unew;
240         xSemaphoreGive(sem1);
241
242         if(utemp<0)
243         {

```

```
244         utemp=-utemp;
245         digitalWrite(MOTODIR,LOW);
246     }
247     else
248     {
249         digitalWrite(MOTODIR,HIGH);
250     }
251     analogWrite(MOTOPWM,utemp);
252     //Serial.println(utemp);
253 }
254 //mutex unlock
255
256
257
258
259 //xSemaphoreGive(run2);
260
261 #ifndef SUPDOG
262     time1=micros()-time1;
263     if(time1>maxtime)
264     {
265         maxtime=time1;
266         //Serial.print("writer max time was");
267         //Serial.println(maxtime);
268     }
269 #endif
270 //Serial.println(time1);
271
272
273
274 }
275 //Serial.print("max time after 100000 trialswas");
276 //Serial.print(oldtime);
277 //Serial.println(" in microseconds");
278 while(1);
279 }
280
281
282
283 void setup() {
284     analogWriteFrequency(MOTOPWM,732.4218);
285     analogWriteResolution(16);
286     portBASE_TYPE s;
287     pinMode(MOTODIR,OUTPUT);
288     MotoEnc.write(0);
289     rodEnc.write(0);
290     s = xTaskCreate(Observer, NULL, 200, NULL, 3, NULL);
291     s = xTaskCreate(writer, NULL, 200, NULL, 4, NULL);
292     sem1=xSemaphoreCreateMutex();
293     sem2=xSemaphoreCreateMutex();
294
295
296 //ifndef TESTING
297     Serial.begin(9600);
298 //endif
299 // start tasks
300 vTaskStartScheduler();
301 //Serial.println("Scheduler failed");
```

```
302     while(1);
303 }
304 //
305 // -----
306 // WARNING idle loop has a very small stack (configMINIMAL_STACK_SIZE)
307 // loop must never block
308 void loop() {
309     // not used
310 }
```

The PID controller code

```
1  const float PIDK=98.936;
2  const float PIDKD=6.6904;
3  const float PIDKI=348.9383;
4
5  const float DT=0.0035;
6
7  void PID(void * params)
8  {
9      float pre_yerr=0.0;
10     float integral=0.0;
11     float derivative=0.0;
12     float utemp=0.0;
13     int utempi=0.0;
14
15     float yerr=0.0;
16
17     int i;
18
19     #ifdef SUPDOG
20         int time1=0;
21         int maxtime=0;
22     #endif
23
24     //Serial.println("do I get here");
25     while(1)
26     {
27     #ifdef SUPDOG
28         time1=micros();
29     #endif
30         while(run2==0);
31
32         run2=0;
33
34
35
36         utemp=0;
37         //calculate input
38
39         if((yerr<0.01)|| (yerr>0.01))
40         {
41             integral=integral+yerr*DT;
42         }
43         derivative=(yerr-pre_yerr)/DT;
44
45         utemp=PIDK*yerr+PIDKI*integral+PIDKD*derivative;
46 }
```

```
47         utempi=(int)(utemp*65535.0/18);
48     /*#ifdef PRINTING*/
49
50 /*#endif*/
51     if(utempi>65535)
52     {
53         utempi=65535;
54     }
55     if(utempi<-65535)
56     {
57         utempi=-65535;
58     }
59
60     xSemaphoreTake(sem1,0);
61     unew=utempi;
62     xSemaphoreGive(sem1);
63     //mutex unlock
64
65     //mutex_lock
66     xSemaphoreTake(sem2,0);
67     yerr=y meas [1];
68     //mutex unlock
69     xSemaphoreGive(sem2);
70     yerr=-yerr;
71
72
73 }
74 //Serial.print("max time after 100000 trials was");
75 //Serial.print(maxtime);
76 //Serial.println(" in microseconds");
77 while(1);
78 }
```

9.4 Hardware

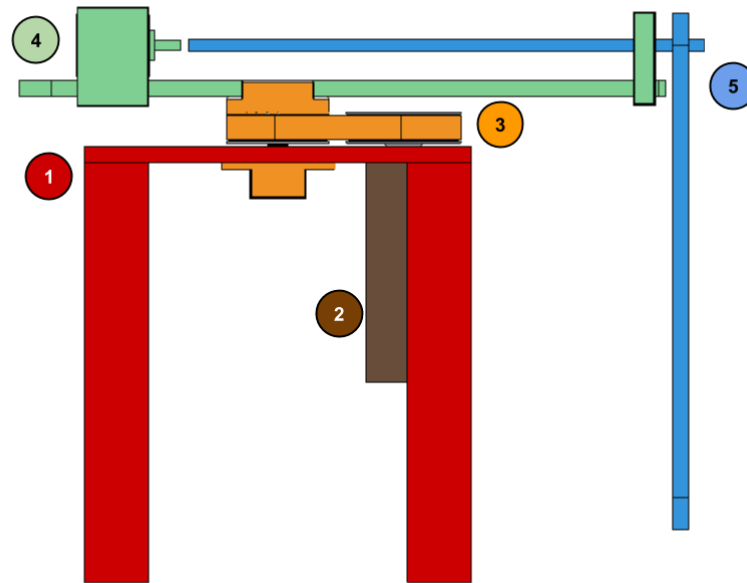


Figure 8: A labeled model of the Furuta pendulum 1) 6" tall base stand 2) Motor and encoder 3) Timing belt transmission and slip ring 4) Drive arm and encoder 5) Pendulum arm

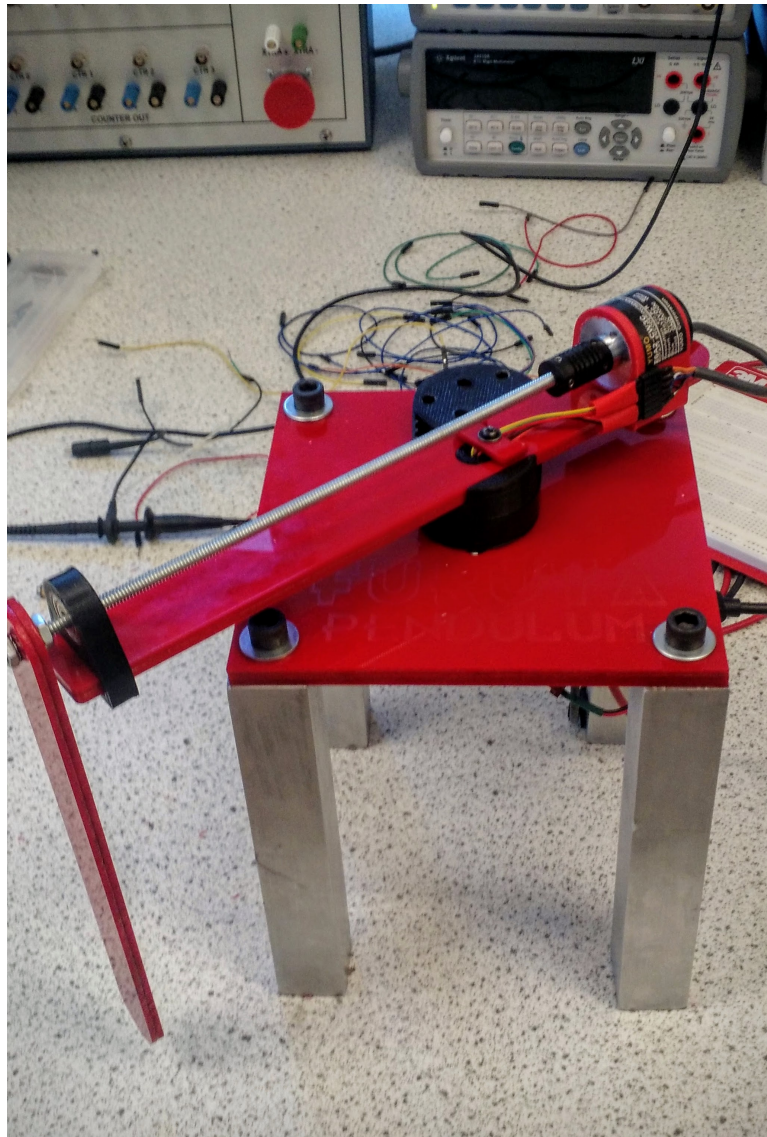


Figure 9: The fully assembled Furuta pendulum on the lab bench