homework 07

Name

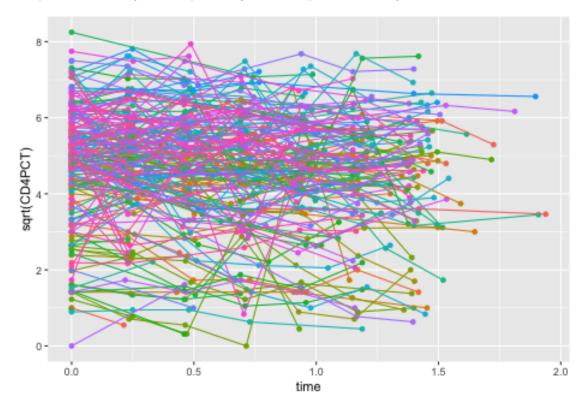
October 26, 2020

Data analysis

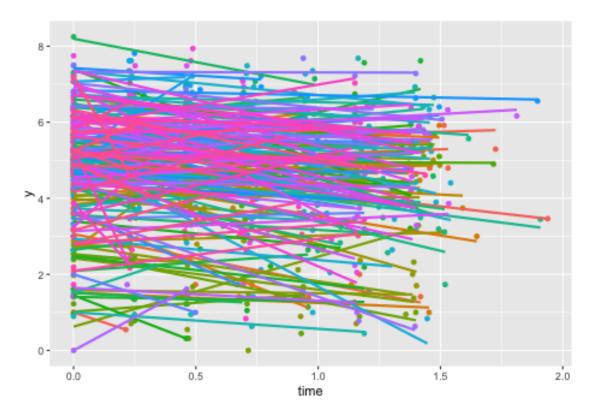
CD4 percentages for HIV infected kids

The folder cd4 has CD4 percentages for a set of young children with HIV who were measured several times over a period of two years. The dataset also includes the ages of the children at each measurement.

1. Graph the outcome (the CD4 percentage, on the square root scale) for each child as a function of time.



2. Each child's data has a time course that can be summarized by a linear fit. Estimate these lines and plot them for all the children.



3. Set up a model for the children's slopes and intercepts as a function of the treatment and age at baseline. Estimate this model using the two-step procedure–first estimate the intercept and slope separately for each child, then fit the between-child models using the point estimates from the first step.

```
##
## Call:
## lm(formula = intercept ~ treatment + age.baseline, data = coef)
##
## Residuals:
##
      Min
               1Q Median
                                3Q
  -3.9511 -0.6352 0.2292 0.9586 2.8988
##
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                5.18363
                           0.34684 14.945
                                             <2e-16 ***
## (Intercept)
## treatment
               -0.15222
                            0.20044
                                    -0.759
                                              0.449
                                    -0.757
                                              0.450
## age.baseline -0.03323
                            0.04390
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.408 on 195 degrees of freedom
## Multiple R-squared: 0.005778,
                                   Adjusted R-squared:
## F-statistic: 0.5666 on 2 and 195 DF, p-value: 0.5684
##
## Call:
## lm(formula = slop ~ treatment + age.baseline, data = coef)
##
## Residuals:
##
                     1Q
                                            3Q
         Min
                            Median
                                                     Max
```

```
## -1.072e-16 -7.310e-17 -6.430e-17 1.600e-18 7.734e-15
##
## Coefficients:
##
                 Estimate Std. Error
                                       t value Pr(>|t|)
## (Intercept) -4.014e-01 1.371e-16 -2.928e+15
                                                 <2e-16 ***
               -7.484e-17 7.922e-17 -9.450e-01
                                                  0.346
## treatment
## age.baseline 4.006e-18 1.735e-17 2.310e-01
                                                  0.818
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.566e-16 on 195 degrees of freedom
## Multiple R-squared: 0.4985, Adjusted R-squared: 0.4933
## F-statistic: 96.9 on 2 and 195 DF, p-value: < 2.2e-16
```

4. Write a model predicting CD4 percentage as a function of time with varying intercepts across children. Fit using lmer() and interpret the coefficient for time.

```
## lmer(formula = sqrt(CD4PCT) ~ (1 | newpid) + time, data = hiv.data)
               coef.est coef.se
## (Intercept) 4.81
                         0.10
## time
               -0.39
                         0.06
##
## Error terms:
  Groups
                         Std.Dev.
             Name
##
   newpid
             (Intercept) 1.40
                         0.76
## Residual
## number of obs: 978, groups: newpid, 226
## AIC = 2852.6, DIC = 2831.1
## deviance = 2837.9
```

The average model for all children (complete pooling) is written as:

```
y = 4.81 - 0.39 * time
```

With 1% increase in time, the square root scale of CD4 percentage will decrease by 0.39%

5. Extend the model in (4) to include child-level predictors (that is, group-level predictors) for treatment and age at baseline. Fit using lmer() and interpret the coefficients on time, treatment, and age at baseline.

```
## lmer(formula = sqrt(CD4PCT) ~ (1 | newpid) + time + treatment +
##
       age.baseline, data = hiv.data)
##
                coef.est coef.se
                 4.76
                          0.33
## (Intercept)
## time
                -0.38
                           0.06
## treatment
                 0.29
                          0.19
## age.baseline -0.12
                           0.04
##
## Error terms:
                         Std.Dev.
  Groups
             Name
             (Intercept) 1.37
  newpid
## Residual
                         0.76
## number of obs: 978, groups: newpid, 226
## AIC = 2852.5, DIC = 2815
## deviance = 2827.8
```

The average model for all children (complete pooling) is written as:

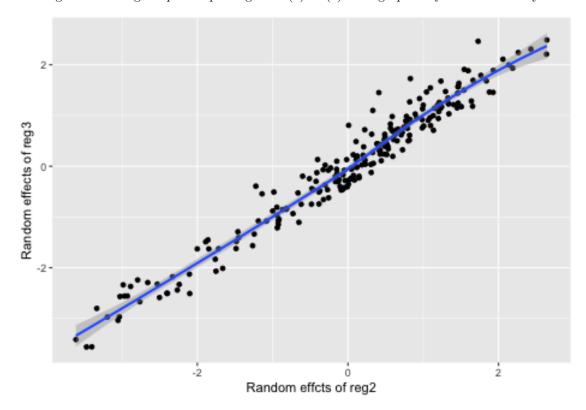
y = 4.76 - 0.38 * time + 0.29 * treatment - 0.12 * age.baseline

With 1% increase in time, the square root scale of CD4 percentage will decrease by 0.38%.

With 1 increase in treatment, the square root scale of CD4 percentage will increase by 0.29

With 1% increase in age.baseline, the square root scale of CD4 percentage will decrease by 0.12%

6. Investigate the change in partial pooling from (4) to (5) both graphically and numerically.



7. Use the model fit from (5) to generate simulation of predicted CD4 percentages for each child in the dataset at a hypothetical next time point.

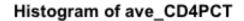
newpid	time	treatment	age.baseline	CD4PCT
1	2.2383333	1	3.9100000	13.738322
2	0.5133333	2	3.5650000	1.379835
3	2.0250000	1	6.1241667	26.048514
4	1.4883333	1	2.3025000	25.016452
5	0.3000000	1	0.6541667	16.965292
6	1.8308333	2	2.9183333	21.614623

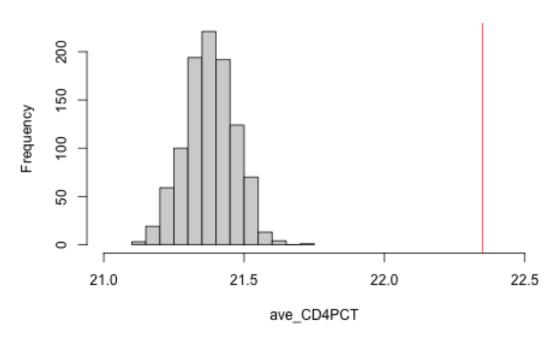
8. Use the same model fit to generate simulations of CD4 percentages at each of the time periods for a new child who was 4 years old at baseline.

treatment	time	age.baseline	CD4PCT
1	0.0	4	21.02477
1	0.1	4	20.67577
1	0.2	4	20.32969
1	0.3	4	19.98654

treatment	$_{ m time}$	age.baseline	CD4PCT
1	0.4	4	19.64630
1	0.5	4	19.30898
1	0.6	4	18.97459
1	0.7	4	18.64311
1	0.8	4	18.31456
1	0.9	4	17.98893
1	1.0	4	17.66622
1	1.1	4	17.34643
1	1.2	4	17.02956
1	1.3	4	16.71561
1	1.4	4	16.40458
1	1.5	4	16.09648
1	1.6	4	15.79129
1	1.7	4	15.48902
1	1.8	4	15.18968
1	1.9	4	14.89326
1	2.0	4	14.59975

9. Posterior predictive checking: continuing the previous exercise, use the fitted model from (5) to simulate a new dataset of CD4 percentages (with the same sample size and ages of the original dataset) for the final time point of the study, and record the average CD4 percentage in this sample. Repeat this process 1000 times and compare the simulated distribution to the observed CD4 percentage at the final time point for the actual data.





10. Extend the model to allow for varying slopes for the time predictor.

```
## lmer(formula = y ~ time + (1 + time | newpid), data = hiv.data)
## coef.est coef.se
```

```
## (Intercept) 4.80
                         0.10
                         0.07
## time
               -0.37
##
## Error terms:
##
    Groups
             Name
                         Std.Dev. Corr
##
    newpid
             (Intercept) 1.39
##
             time
                         0.59
                                   -0.10
##
   Residual
                         0.71
## ---
## number of obs: 978, groups: newpid, 226
## AIC = 2826.6, DIC = 2801.9
## deviance = 2808.2
 11. Next fit a model that does not allow for varying slopes but does allow for different coefficients for each
    time point (rather than fitting the linear trend).
model_5<-lmer(y ~ factor(time) + treatment + (1 | newpid),data = hiv.data)</pre>
summary(model_5)
## Linear mixed model fit by REML ['lmerMod']
## Formula: y ~ factor(time) + treatment + (1 | newpid)
      Data: hiv.data
##
##
## REML criterion at convergence: 1961.6
##
## Scaled residuals:
##
       Min
                1Q Median
                                 3Q
                                        Max
## -3.9255 -0.2478 0.0000 0.2602 4.1822
## Random effects:
##
    Groups
             Name
                         Variance Std.Dev.
   newpid
             (Intercept) 1.9986
                                   1.4137
  Residual
                         0.4989
                                   0.7063
## Number of obs: 978, groups: newpid, 226
##
## Fixed effects:
##
                                   Estimate Std. Error t value
## (Intercept)
                                   4.273150
                                              0.312067
                                                        13.693
## factor(time)0.205
                                  -1.235220
                                              0.670461
                                                        -1.842
## factor(time)0.20999999999999
                                  0.167573
                                              0.893167
                                                          0.188
## factor(time)0.2133333333333 0.186290
                                              0.948122
                                                          0.196
## factor(time)0.2133333333333 -1.249615
                                              0.948178
                                                         -1.318
## factor(time)0.2158333333333 1.501041
                                              0.900111
                                                          1.668
## factor(time)0.2158333333333 -0.245124
                                              0.876868
                                                        -0.280
## factor(time)0.216666666666667 -0.326427
                                                         -0.405
                                              0.806301
## factor(time)0.21916666666667 -0.461159
                                              0.856403
                                                        -0.538
## factor(time)0.22166666666667 0.220172
                                              0.948122
                                                         0.232
## factor(time)0.22416666666667 -1.452466
                                              0.847615
                                                        -1.714
## factor(time)0.22666666666667
                                              0.587678
                                                         2.436
                                   1.431352
## factor(time)0.2274999999999 -1.567907
                                                        -1.758
                                              0.891732
## factor(time)0.2275
                                  -0.009054
                                              0.464445
                                                        -0.019
## factor(time)0.229999999999 -0.389868
                                              0.590732
                                                        -0.660
## factor(time)0.23
                                  -0.129092
                                              0.133216
                                                        -0.969
```

0.453511

0.842739

-1.185

0.068

-0.537319

factor(time)0.2325

factor(time)0.2333333333333 0.057588

```
## factor(time)0.23500000000001 -1.935615
                                           0.802280
                                                    -2.413
                                                     0.117
## factor(time)0.2358333333333333
                                0.034807
                                           0.296540
## factor(time)0.235833333333334
                                0.167028
                                           0.621746
                                                     0.269
## factor(time)0.2375
                                1.772950
                                          0.948122
                                                     1.870
## factor(time)0.2383333333333 -0.236035
                                           0.490675
                                                    -0.481
## factor(time)0.238333333333333
                                0.835864
                                           0.820515
                                                     1.019
## factor(time)0.24083333333333 -0.198843
                                           0.787583
                                                    -0.252
## factor(time)0.240833333333333
                                0.332389
                                           0.594511
                                                     0.559
## factor(time)0.2433333333333 -0.495876
                                           0.893214
                                                    -0.555
## factor(time)0.24416666666667
                                0.069593
                                           0.480605
                                                     0.145
## factor(time)0.2458333333333333
                                0.104952
                                           0.434505
                                                     0.242
## factor(time)0.24583333333333 -0.243282
                                           0.607262
                                                    -0.401
  0.670798
                                                    -0.394
## factor(time)0.24666666666667
                                0.370885
                                           0.858195
                                                     0.432
## factor(time)0.24916666666666
                                0.169771
                                          0.387125
                                                     0.439
## factor(time)0.249166666666667 -0.331923
                                           0.200435
                                                    -1.656
## factor(time)0.25166666666667
                                0.252969
                                           0.431768
                                                     0.586
## factor(time)0.2516666666668
                                           0.806826
                                                     0.365
                                0.294871
## factor(time)0.25416666666667 -0.597056
                                                    -0.707
                                           0.844021
## factor(time)0.25666666666667
                                0.299664
                                           0.651407
                                                     0.460
## factor(time)0.25749999999999
                                0.068429
                                           0.846792
                                                     0.081
## factor(time)0.2575
                                0.462339
                                          0.633484
                                                     0.730
## factor(time)0.2625
                               -0.054029
                                           0.846219
                                                    -0.064
## factor(time)0.265
                               -0.182887
                                           0.848763
                                                    -0.215
## factor(time)0.26583333333333 -0.345180
                                           0.841961
                                                    -0.410
## factor(time)0.26833333333333 -0.407728
                                           0.596062
                                                    -0.684
## factor(time)0.2683333333333334
                                0.040952
                                           0.497565
                                                     0.082
  factor(time)0.2875
                                0.478992
                                           0.527637
                                                     0.908
## factor(time)0.2933333333333 -0.327323
                                           0.948178
                                                    -0.345
## factor(time)0.30416666666667
                                0.251505
                                          0.894059
                                                     0.281
0.948178
                                                    -0.294
## factor(time)0.30666666666667
                                0.460600
                                           0.833782
                                                     0.552
## factor(time)0.32583333333334 -0.129321
                                          0.895751
                                                    -0.144
## factor(time)0.32833333333333 -0.917440
                                          0.948178
                                                    -0.968
## factor(time)0.33166666666667
                                                     0.079
                                0.074614
                                           0.948122
## factor(time)0.3583333333333 0.665458
                                           0.865263
                                                     0.769
## factor(time)0.36416666666667 -0.049550
                                           0.610120
                                                    -0.081
-0.276
                                           0.948122
## factor(time) 0.429166666666667 -0.411948
                                          0.900111
                                                    -0.458
## factor(time)0.4383333333333 -0.880173
                                           0.900004
                                                    -0.978
## factor(time)0.4408333333333 -0.096418
                                           0.775791
                                                    -0.124
## factor(time)0.4433333333333333
                               0.120968
                                          0.851279
                                                     0.142
## factor(time)0.44916666666667 -0.106290
                                          0.795773
                                                    -0.134
  factor(time)0.45416666666666
                               0.295639
                                          0.900111
                                                     0.328
## factor(time)0.455
                               -1.457467
                                           0.891732
                                                    -1.634
0.948122
                                                     0.281
## factor(time) 0.4575
                               -0.169796
                                           0.492694
                                                    -0.345
## factor(time)0.45916666666667
                                0.233933
                                           0.621871
                                                     0.376
0.251679
                                           0.572366
                                                     0.440
## factor(time)0.46
                               -0.266614
                                           0.172311
                                                    -1.547
## factor(time)0.4600000000000 -0.230663
                                                    -0.674
                                           0.342320
## factor(time)0.46249999999999 -1.004826
                                           0.591558
                                                    -1.699
## factor(time) 0.4625
                                0.429701
                                          0.413612
                                                     1.039
## factor(time)0.46333333333333 -0.708283
                                           0.814059 -0.870
```

```
## factor(time)0.465
                                -0.844262
                                           0.491471
                                                    -1.718
## factor(time)0.46583333333333 0.332495
                                           0.588491
                                                      0.565
                                                    -0.726
## factor(time)0.46583333333333 -0.603658
                                           0.831474
                                                     2.458
## factor(time) 0.4675
                                2.330785
                                           0.948122
## factor(time)0.468333333333 -0.778996
                                           0.856403
                                                    -0.910
## factor(time)0.4708333333333 -0.328961
                                           0.466210
                                                    -0.706
## factor(time)0.47083333333333 -0.480714
                                           0.609998
                                                    -0.788
## factor(time)0.4733333333333 -0.173185
                                           0.622871
                                                     -0.278
## factor(time)0.4733333333333333
                                0.470338
                                           0.794898
                                                      0.592
0.823731
                                                    -0.800
## factor(time)0.47416666666667 -0.864499
                                           0.806903
                                                    -1.071
## factor(time)0.4758333333333 -0.442349
                                           0.806516
                                                     -0.548
  factor(time)0.47583333333333 -1.379260
                                           0.587510
                                                    -2.348
## factor(time)0.47666666666667
                               0.622695
                                           0.406318
                                                     1.533
0.582033
                                                     -0.373
## factor(time)0.479166666666667 -0.016261
                                           0.253065
                                                     -0.064
## factor(time)0.48166666666666
                                0.142042
                                           0.588947
                                                      0.241
## factor(time)0.48166666666667
                                           0.428995
                                                      0.550
                                0.235913
## factor(time)0.48416666666667 -2.706088
                                           0.808605
                                                     -3.347
## factor(time)0.485
                                0.892373
                                           0.624525
                                                      1.429
## factor(time)0.4874999999999 -0.174287
                                           0.773839
                                                     -0.225
## factor(time) 0.4875
                                1.795269
                                           0.824280
                                                      2.178
## factor(time)0.48750000000001
                                           0.806826
                                                     2.171
                                1.751384
0.083884
                                           0.858195
                                                      0.098
## factor(time)0.495
                               -0.114439
                                           0.600507
                                                    -0.191
## factor(time)0.49583333333333 -0.071798
                                           0.900170
                                                    -0.080
## factor(time)0.4983333333333 -0.777435
                                                     -1.779
                                           0.436966
  factor(time)0.49833333333333 -0.381371
                                           0.425277
                                                     -0.897
## factor(time)0.5008333333333 -0.246927
                                           0.796321
                                                    -0.310
## factor(time)0.5008333333333333
                               0.116819
                                           0.816822
                                                      0.143
## factor(time)0.50166666666667 -1.147262
                                           0.617146
                                                    -1.859
  factor(time)0.5033333333333333
                                0.608316
                                           0.841961
                                                      0.722
## factor(time)0.50416666666666
                               0.229750
                                           0.519787
                                                      0.442
## factor(time)0.50583333333333 -1.555569
                                           0.822002
                                                    -1.892
## factor(time)0.51166666666667 -1.138914
                                           0.877639
                                                     -1.298
## factor(time)0.5141666666666 0.119408
                                           0.626184
                                                     0.191
## factor(time)0.515
                                0.189303
                                           0.948122
                                                      0.200
## factor(time)0.5175
                                           0.422854
                                                    -1.188
                               -0.502450
## factor(time)0.51750000000001 -1.022268
                                           0.832721
                                                     -1.228
## factor(time)0.5333333333333 -0.310532
                                           0.646166
                                                    -0.481
## factor(time)0.53333333333333 -1.092253
                                           0.869642
                                                    -1.256
## factor(time)0.53416666666667
                               0.146220
                                           0.628151
                                                     0.233
## factor(time)0.53666666666667 -0.408976
                                           0.513599
                                                    -0.796
## factor(time)0.5558333333333 -0.167965
                                           0.948178
                                                    -0.177
## factor(time)0.55833333333333333
                               1.762287
                                           0.948122
                                                     1.859
## factor(time)0.56416666666667 -0.971363
                                           0.904185
                                                     -1.074
## factor(time)0.575
                               -0.225507
                                           0.640809
                                                     -0.352
## factor(time)0.5825
                                0.667176
                                           0.948122
                                                      0.704
## factor(time)0.59416666666667 -0.401448
                                           0.895832
                                                    -0.448
## factor(time)0.6108333333333 -1.130547
                                           0.948178
                                                     -1.192
## factor(time)0.6375
                                           0.899971
                                                     2.014
                                1.812946
## factor(time)0.64833333333333 -2.086157
                                           0.891522
                                                    -2.340
0.894769
                                                    -1.249
## factor(time)0.67
                               -0.384380
                                           0.853863 -0.450
```

```
## factor(time)0.67083333333333 -0.982520
                                         0.493669
                                                  -1.990
## factor(time)0.6733333333333333
                               0.078450
                                         0.948122
                                                    0.083
## factor(time)0.67583333333333 -0.123402
                                         0.670719
                                                   -0.184
## factor(time)0.68416666666667
                               0.499723
                                         0.897286
                                                    0.557
## factor(time)0.685
                               0.588783
                                         0.841181
                                                    0.700
## factor(time)0.6875
                              -1.545170
                                         0.611818
                                                   -2.526
0.893167
                                                   -0.145
## factor(time)0.68916666666667
                               0.142586
                                         0.810354
                                                    0.176
## factor(time)0.69
                              -0.161315
                                         0.166577
                                                   -0.968
## factor(time)0.6925
                               0.561116
                                         0.560131
                                                    1.002
## factor(time)0.69250000000001
                               0.896022
                                         0.840110
                                                    1.067
## factor(time)0.69333333333334 -0.461159
                                         0.856403
                                                   -0.538
  factor(time)0.695
                               0.372792
                                         0.876868
                                                   0.425
                                                   -0.354
## factor(time)0.69583333333333 -0.304166
                                         0.859387
## factor(time)0.69583333333333 -1.673665
                                         0.835014
                                                   -2.004
## factor(time)0.695833333333333
                               0.809040
                                         0.597089
                                                    1.355
  factor(time)0.698333333333333
                               0.070361
                                                    0.084
                                         0.839637
## factor(time)0.6983333333333 -0.630620
                                                   -1.067
                                         0.590823
## factor(time)0.700833333333333
                               1.589406
                                                   3.255
                                         0.488246
## factor(time)0.7033333333333 -0.901457
                                         0.578693
                                                   -1.558
## factor(time)0.7033333333333 -1.083736
                                         0.820515
                                                   -1.321
## factor(time)0.704166666666667 -4.823671
                                         0.806903
                                                   -5.978
## factor(time)0.7058333333333 -0.457542
                                         0.495704
                                                   -0.923
## factor(time)0.70666666666667
                               2.374372
                                         0.800608
                                                    2.966
0.799532
                                                   -0.161
## factor(time)0.70916666666667
                               0.258942
                                         0.278697
                                                    0.929
## factor(time)0.71166666666666
                              0.123918
                                         0.843290
                                                   0.147
                                                   -0.552
  factor(time)0.71166666666667 -0.451241
                                         0.818063
  factor(time)0.71166666666666 -0.884471
                                         0.570842
                                                   -1.549
## factor(time)0.71416666666667 -1.425496
                                         0.578886
                                                   -2.462
## factor(time)0.7149999999999 -0.705677
                                         0.796511
                                                   -0.886
  factor(time)0.71500000000001 -0.639719
                                         0.862059
                                                   -0.742
## factor(time)0.7175
                              -1.003521
                                         0.808605
                                                   -1.241
## factor(time)0.72
                              -4.300981
                                         0.782976
                                                   -5.493
## factor(time)0.725
                              -0.607833
                                         0.602155
                                                   -1.009
## factor(time)0.725833333333333
                              0.329598
                                         0.846792
                                                   0.389
## factor(time)0.7258333333333333
                               0.725080
                                         0.832456
                                                    0.871
## factor(time)0.725833333333333
                                                    0.375
                               0.355986
                                         0.948122
## factor(time)0.7283333333333 -0.269459
                                         0.291383
                                                   -0.925
## factor(time)0.7308333333333333
                               0.062819
                                         0.507333
                                                    0.124
## factor(time)0.7333333333333 -0.750935
                                         0.846292
                                                   -0.887
0.815466
                                                   -3.515
0.948178
                                                   -1.338
  0.015552
                                         0.851279
                                                   0.018
## factor(time)0.73666666666667
                               1.515534
                                         0.845977
                                                    1.791
## factor(time)0.7425
                              -0.524947
                                         0.948178
                                                   -0.554
## factor(time)0.74416666666667
                               0.169516
                                         0.575827
                                                    0.294
## factor(time)0.745
                              -0.403251
                                         0.826247
                                                   -0.488
## factor(time)0.7475
                              -0.328621
                                         0.367218
                                                   -0.895
## factor(time)0.75250000000001 -1.636682
                                         0.841961
                                                   -1.944
## factor(time)0.7583333333333333
                               0.316056
                                         0.865263
                                                   0.365
0.813016
                                                   -0.787
## factor(time)0.7633333333333 -0.038079
                                                   -0.044
                                         0.869642
0.900170 -0.055
```

```
## factor(time)0.76583333333333 -1.253662
                                          0.877639
                                                    -1.428
## factor(time)0.76666666666667 -0.387873
                                                    -0.989
                                           0.392260
                                                    -2.074
## factor(time)0.775
                               -1.693469
                                           0.816660
                                                     0.646
## factor(time)0.78
                                1.024583
                                           1.586614
0.996067
                                          0.894059
                                                     1.114
## factor(time)0.785
                               -0.193405
                                          0.832268
                                                    -0.232
## factor(time)0.78833333333333 -0.714924
                                           0.948122
                                                    -0.754
## factor(time)0.79416666666667 -0.704648
                                           0.822852
                                                    -0.856
## factor(time)0.8025
                               -0.574098
                                          0.822399
                                                    -0.698
## factor(time)0.805
                               -1.473256
                                           0.832721
                                                    -1.769
## factor(time)0.80500000000000 0.090842
                                           0.792566
                                                     0.115
## factor(time)0.80750000000001 -0.523588
                                           0.904185
                                                    -0.579
  factor(time)0.82416666666667
                               0.137776
                                           0.640972
                                                     0.215
## factor(time)0.8625
                               -0.455841
                                           0.612682
                                                    -0.744
## factor(time)0.8675
                                0.571095
                                           0.899971
                                                     0.635
## factor(time)0.8783333333333 -0.206629
                                           0.891522
                                                    -0.232
## factor(time)0.8958333333333 -0.729675
                                                    -0.818
                                          0.891732
## factor(time)0.9008333333333 -0.412331
                                           0.853883
                                                    -0.483
## factor(time)0.900833333333333
                               0.274063
                                           0.586660
                                                     0.467
## factor(time)0.9033333333333 -1.055211
                                           0.768614
                                                    -1.373
## factor(time)0.903333333333333
                                2.278205
                                          0.948122
                                                     2.403
## factor(time)0.9058333333333333
                                1.288250
                                          0.900111
                                                     1.431
## factor(time)0.9083333333333 -0.411948
                                           0.900111
                                                    -0.458
## factor(time)0.90916666666667 -0.302822
                                           0.814059
                                                    -0.372
                                                    -0.325
## factor(time)0.91166666666667 -0.257515
                                           0.792129
## factor(time)0.9175
                               -0.514800
                                           0.841181
                                                    -0.612
## factor(time)0.919166666666667 0.042230
                                           0.478726
                                                     0.088
  factor(time)0.9199999999999 -0.847018
                                                    -1.069
                                           0.792385
## factor(time)0.92
                               -0.984342
                                           0.284896
                                                    -3.455
## factor(time)0.9200000000001 -0.927801
                                                    -1.652
                                           0.561724
## factor(time)0.9225
                               -0.515963
                                           0.590331
                                                    -0.874
  factor(time)0.92583333333333 -1.743925
                                           0.592472
                                                    -2.943
## factor(time)0.925833333333334
                                0.331361
                                           0.840110
                                                     0.394
                                0.027749
## factor(time)0.9283333333333333
                                          0.790415
                                                     0.035
## factor(time)0.92833333333334 -0.933976
                                           0.831474
                                                    -1.123
## factor(time)0.9308333333333 -0.700332
                                           0.559738
                                                    -1.251
## factor(time)0.93083333333333 -1.987878
                                           0.812976
                                                    -2.445
## factor(time)0.93333333333333
                                0.434292
                                           0.828705
                                                     0.524
0.008022
                                           0.590293
                                                     0.014
## factor(time)0.93416666666664 -0.801587
                                           0.839637
                                                    -0.955
## factor(time)0.93416666666667 -1.088679
                                           0.806903
                                                    -1.349
## factor(time)0.9358333333333 -0.506940
                                                    -0.854
                                           0.593352
## factor(time)0.93583333333333 -0.694866
                                           0.847615
                                                    -0.820
  factor(time)0.93666666666667
                                0.142828
                                           0.788935
                                                     0.181
## factor(time)0.9383333333333333
                                0.021226
                                           0.806588
                                                     0.026
0.335472
                                                    -0.502
  factor(time)0.93916666666667
                                0.060105
                                           0.332742
                                                     0.181
0.410911
                                                    -0.713
0.818063
                                                    -0.586
## factor(time)0.94416666666667
                                0.147901
                                           0.876868
                                                     0.169
## factor(time)0.9475
                                0.654097
                                           0.587478
                                                     1.113
## factor(time)0.95250000000001 -0.430246
                                           0.794898
                                                    -0.541
## factor(time)0.955
                                1.583590
                                           0.843290
                                                     1.878
## factor(time)0.95500000000001 -0.409689
                                           0.816822 -0.502
```

```
## factor(time)0.95583333333333 -1.091349
                                             0.851279
                                                      -1.282
                                  0.369367
## factor(time)0.9575
                                            0.792207
                                                        0.466
## factor(time)0.9583333333333333
                                 0.107922
                                             0.363268
                                                        0.297
## factor(time)0.9583333333333 -0.140528
                                             0.462228
                                                       -0.304
## factor(time)0.9608333333333 -1.521609
                                             0.825267
                                                       -1.844
0.846792
                                                       -0.042
## factor(time)0.96416666666667
                                 0.500484
                                             0.832456
                                                        0.601
## factor(time)0.9658333333333333
                                 0.015552
                                             0.851279
                                                        0.018
  factor(time)0.976666666666667 -0.483905
                                             0.844021
                                                       -0.573
## factor(time)0.9774999999999 -3.280808
                                             0.815466
                                                      -4.023
## factor(time)0.9775
                                 -0.371726
                                             0.363176
                                                      -1.024
## factor(time)0.97750000000001
                                 0.559254
                                             0.862059
                                                       0.649
  factor(time)0.9824999999999999999 -0.287737
                                             0.824630
                                                      -0.349
## factor(time)0.9825
                                 -0.097572
                                             0.846292
                                                       -0.115
## factor(time)0.9833333333333 -0.059553
                                             0.881073
                                                       -0.068
## factor(time)0.9858333333333 -0.454586
                                             0.948178
                                                       -0.479
  -0.934
                                             0.570752
## factor(time)0.996666666666667 -0.938093
                                                       -2.226
                                             0.421411
## factor(time)0.99916666666667 -0.995369
                                             0.783710
                                                      -1.270
## factor(time)1
                                 -0.949910
                                            0.842739
                                                      -1.127
## factor(time)1.0016666666667
                                 -0.345180
                                             0.841961
                                                      -0.410
## factor(time)1.0025
                                 -1.289563
                                             0.845977
                                                       -1.524
## factor(time)1.01083333333333
                                            0.813016
                                                      -0.453
                                 -0.368065
## factor(time)1.0158333333333333
                                  0.161039
                                             0.900170
                                                        0.179
## factor(time)1.02083333333333
                                 -1.324099
                                             0.855522
                                                      -1.548
## factor(time)1.0325
                                  0.728730
                                            0.894059
                                                       0.815
## factor(time)1.035
                                 -0.678692
                                             0.441936
                                                      -1.536
                                                      -1.510
  factor(time)1.048333333333333
                                 -1.325592
                                             0.877639
## factor(time)1.05333333333333
                                 -0.095291
                                             0.832268
                                                      -0.114
## factor(time)1.0541666666667
                                 -0.467276
                                                      -0.790
                                             0.591133
## factor(time)1.075833333333333
                                 -1.024455
                                             0.850062
                                                       -1.205
  factor(time)1.0866666666667
                                  0.266708
                                             1.586614
                                                        0.168
## factor(time)1.09
                                 -1.573205
                                             0.948178
                                                      -1.659
## factor(time)1.0925
                                 -0.300134
                                             0.633673
                                                       -0.474
## factor(time)1.11416666666667
                                  0.066164
                                             0.857342
                                                       0.077
## factor(time)1.13083333333333
                                  0.363543
                                             0.853883
                                                       0.426
## factor(time)1.13583333333333
                                 -2.772075
                                            0.948122
                                                       -2.924
## factor(time)1.1391666666667
                                  0.121262
                                             0.788935
                                                        0.154
## factor(time)1.14166666666667
                                 -0.480091
                                             0.578228
                                                       -0.830
## factor(time)1.145
                                 -0.427556
                                             0.891732
                                                      -0.479
## factor(time)1.1475
                                 -1.371209
                                             0.841181
                                                      -1.630
## factor(time)1.14916666666667
                                                      -1.162
                                 -0.669992
                                             0.576679
                                                      -1.802
## factor(time)1.15
                                 -0.411921
                                             0.228615
## factor(time)1.1525
                                                      -1.794
                                 -0.988881
                                             0.551104
## factor(time)1.15583333333333
                                 -1.176169
                                             0.491431
                                                      -2.393
## factor(time)1.1575
                                 -0.048408
                                             0.562024
                                                       -0.086
                                                      -2.730
## factor(time)1.15833333333333
                                 -1.626371
                                            0.595810
## factor(time)1.160833333333333
                                 -1.044164
                                             0.410850
                                                      -2.541
0.853615
                                             0.596947
                                                        1.430
## factor(time)1.1641666666667
                                  0.335970
                                             0.839637
                                                       0.400
## factor(time)1.16583333333333
                                                      -1.870
                                 -1.561071
                                             0.834968
## factor(time)1.168333333333333
                                 -0.327805
                                            0.806588
                                                      -0.406
## factor(time)1.1691666666667
                                 -0.465419
                                             0.336780
                                                      -1.382
## factor(time)1.17166666666667
                                 -1.376135
                                             0.576640
                                                      -2.386
```

```
## factor(time)1.1766666666667
                                               0.847615
                                  -1.269441
                                                         -1.498
## factor(time)1.1775
                                              0.806516
                                                         -0.102
                                  -0.082289
## factor(time)1.18
                                  -0.468358
                                               0.799532
                                                         -0.586
## factor(time)1.18833333333333
                                  -0.099785
                                              0.221174
                                                         -0.451
## factor(time)1.1966666666667
                                   0.314537
                                               0.631627
                                                          0.498
## factor(time)1.20166666666667
                                   0.092099
                                              0.480176
                                                          0.192
## factor(time)1.2041666666667
                                  -0.579355
                                               0.595696
                                                         -0.973
## factor(time)1.2066666666667
                                   0.281658
                                              0.792207
                                                          0.356
## factor(time)1.2075
                                  -1.104851
                                               0.479003
                                                         -2.307
## factor(time)1.2125
                                   0.087831
                                               0.846292
                                                          0.104
## factor(time)1.2241666666667
                                  -0.330725
                                               0.862059
                                                         -0.384
## factor(time)1.22583333333333
                                   0.033760
                                               0.865183
                                                          0.039
                                   0.038629
## factor(time)1.2266666666667
                                                          0.065
                                               0.596772
                                  -0.105761
## factor(time)1.22916666666667
                                               0.591487
                                                         -0.179
## factor(time)1.2316666666667
                                  -1.398918
                                               0.806301
                                                         -1.735
## factor(time)1.2325
                                  -0.109906
                                               0.800608
                                                         -0.137
## factor(time)1.24583333333333
                                                         -1.088
                                  -0.641479
                                               0.589733
## factor(time)1.24833333333333
                                  -1.644380
                                               0.845977
                                                         -1.944
## factor(time)1.265
                                                         -0.473
                                  -0.224398
                                               0.474713
## factor(time)1.2675
                                  -0.216097
                                               0.842739
                                                         -0.256
## factor(time)1.2841666666667
                                  -1.895928
                                               0.900170
                                                         -2.106
## factor(time)1.3025
                                  -0.729231
                                               0.877639
                                                         -0.831
## factor(time)1.30333333333333
                                  -0.316140
                                               0.573767
                                                         -0.551
## factor(time)1.3116666666667
                                  -1.985489
                                               0.816660
                                                         -2.431
## factor(time)1.3416666666667
                                  -1.104945
                                               0.788935
                                                         -1.401
## factor(time)1.35
                                  -0.387462
                                               0.894769
                                                         -0.433
## factor(time)1.35833333333333
                                                         -2.006
                                  -1.687437
                                               0.841181
## factor(time)1.36
                                  -0.129600
                                               0.893167
                                                         -0.145
## factor(time)1.36083333333333
                                  -0.023905
                                               0.895751
                                                         -0.027
## factor(time)1.36583333333333
                                  -0.745221
                                                         -0.941
                                              0.792129
## factor(time)1.37166666666667
                                  -0.337294
                                               0.569126
                                                         -0.593
## factor(time)1.37416666666667
                                  -0.597457
                                              0.792385
                                                         -0.754
## factor(time)1.375
                                  -0.810512
                                               0.793534
                                                         -1.021
                                              0.766511
## factor(time)1.3766666666667
                                  -3.034697
                                                         -3.959
## factor(time)1.37916666666667
                                   0.054603
                                               0.782780
                                                          0.070
## factor(time)1.38
                                  -0.552245
                                               0.355582
                                                         -1.553
## factor(time)1.3825
                                  -1.535259
                                               0.553663
                                                         -2.773
## factor(time)1.3858333333333
                                                         -1.319
                                  -0.784283
                                               0.594616
## factor(time)1.38583333333334
                                   0.171597
                                              0.831474
                                                          0.206
## factor(time)1.3875
                                               0.790924
                                   0.152660
                                                          0.193
## factor(time)1.38833333333333
                                  -1.484169
                                               0.802263
                                                         -1.850
                                                         -0.984
## factor(time)1.390833333333333
                                  -0.564722
                                               0.574092
## factor(time)1.395833333333333
                                  -0.575124
                                               0.599835
                                                         -0.959
## factor(time)1.39666666666667
                                   0.294433
                                               0.769814
                                                          0.382
## factor(time)1.39833333333333
                                  -0.270299
                                               0.831378
                                                         -0.325
## factor(time)1.39916666666667
                                  -0.296376
                                               0.372938
                                                         -0.795
                                  -2.160278
## factor(time)1.4016666666667
                                              0.605387
                                                         -3.568
## factor(time)1.41
                                  -1.276899
                                              0.554898
                                                         -2.301
## factor(time)1.4125
                                  -0.652333
                                               0.847615
                                                         -0.770
## factor(time)1.415
                                  -0.178479
                                               0.577104
                                                         -0.309
## factor(time)1.41833333333333
                                  -0.134236
                                                         -0.293
                                               0.458217
## factor(time)1.42083333333333
                                  -0.714924
                                               0.948122
                                                         -0.754
## factor(time)1.42416666666667
                                   0.403196
                                              0.789039
                                                          0.511
## factor(time)1.42583333333333
                                  -0.125484
                                               0.816822 -0.154
```

```
## factor(time)1.42916666666667
                                  0.677918
                                             0.879411
                                                        0.771
## factor(time)1.4316666666667
                                 -0.125232
                                             0.584933
                                                      -0.214
                                  0.426945
## factor(time)1.43666666666667
                                             0.810861
                                                        0.527
## factor(time)1.4375
                                 -0.849338
                                             0.789631
                                                       -1.076
## factor(time)1.44583333333333
                                 -3.444148
                                             0.815466
                                                       -4.224
-0.826162
                                             0.900111
                                                       -0.918
## factor(time)1.4541666666667
                                 -0.463561
                                             0.862059
                                                       -0.538
## factor(time)1.45583333333333
                                 -0.579365
                                             0.792207
                                                       -0.731
## factor(time)1.4566666666667
                                 -0.186155
                                             0.411889
                                                       -0.452
## factor(time)1.4625
                                  0.328763
                                             0.800608
                                                        0.411
## factor(time)1.47
                                  0.200931
                                             0.585263
                                                        0.343
## factor(time)1.4725
                                  0.147681
                                             0.824630
                                                        0.179
## factor(time)1.475
                                  0.258339
                                             0.846292
                                                        0.305
                                                       -1.790
## factor(time)1.4816666666667
                                 -1.513951
                                             0.845977
## factor(time)1.4925
                                 -2.564073
                                             0.806301
                                                       -3.180
## factor(time)1.495
                                  0.173118
                                             0.484732
                                                        0.357
## factor(time)1.4975
                                  0.416845
                                             0.631627
                                                        0.660
## factor(time)1.50583333333333
                                 -0.751251
                                             0.900170
                                                       -0.835
## factor(time)1.51416666666667
                                  0.262359
                                             0.792566
                                                        0.331
## factor(time)1.5166666666667
                                 -1.897447
                                             0.842739
                                                       -2.252
## factor(time)1.51916666666667
                                 -2.732923
                                             0.900170
                                                       -3.036
## factor(time)1.53
                                  0.484814
                                             0.848763
                                                        0.571
## factor(time)1.53083333333333
                                  0.047336
                                             0.894059
                                                        0.053
0.246767
                                             0.817981
                                                        0.302
## factor(time)1.5416666666667
                                 -1.030583
                                             0.816660
                                                      -1.262
## factor(time)1.5908333333333
                                 -1.117941
                                             0.894769
                                                       -1.249
## factor(time)1.615
                                 -0.691941
                                                       -0.831
                                             0.832268
                                 -1.555450
                                                       -1.827
## factor(time)1.64833333333333
                                             0.851279
## factor(time)1.7166666666667
                                 -0.002842
                                             0.847568
                                                       -0.003
## factor(time)1.725
                                 -0.362218
                                             0.792566
                                                       -0.457
## factor(time)1.8116666666667
                                  0.324673
                                             0.848763
                                                        0.383
## factor(time)1.8966666666667
                                 -0.346110
                                             0.831378
                                                       -0.416
## factor(time)1.90833333333333
                                 -0.638850
                                             0.865263
                                                       -0.738
                                 -0.856373
## factor(time)1.93833333333333
                                                       -0.903
                                             0.948122
## treatment
                                  0.359121
                                             0.200190
                                                        1.794
##
## Correlation matrix not shown by default, as p = 377 > 12.
## Use print(x, correlation=TRUE)
##
       vcov(x)
                     if you need it
```

12. Compare the results of these models both numerically and graphically.

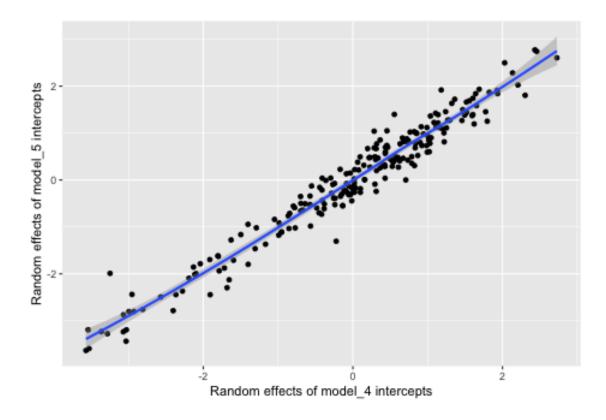


Figure skate in the 1932 Winter Olympics

The folder olympics has seven judges' ratings of seven figure skaters (on two criteria: "technical merit" and "artistic impression") from the 1932 Winter Olympics. Take a look at http://www.stat.columbia.edu/~gelma n/arm/examples/olympics/olympics1932.txt

- 1. Construct a $7 \times 7 \times 2$ array of the data (ordered by skater, judge, and judging criterion).
- 2. Reformulate the data as a 98×4 array (similar to the top table in Figure 11.7), where the first two columns are the technical merit and artistic impression scores, the third column is a skater ID, and the fourth column is a judge ID.
- 3. Add another column to this matrix representing an indicator variable that equals 1 if the skater and judge are from the same country, or 0 otherwise.
- 4. Write the notation for a non-nested multilevel model (varying across skaters and judges) for the technical merit ratings and fit using lmer().
- 5. Fit the model in (4) using the artistic impression ratings.
- 6. Display your results for both outcomes graphically.
- 7. (optional) Use posterior predictive checks to investigate model fit in (4) and (5).

Different ways to write the model:

Using any data that are appropriate for a multilevel model, write the model in the five ways discussed in Section 12.5 of Gelman and Hill.

Models for adjusting individual ratings:

A committee of 10 persons is evaluating 100 job applications. Each person on the committee reads 30 applications (structured so that each application is read by three people) and gives each a numerical rating between 1 and 10.

- 1. It would be natural to rate the applications based on their combined scores; however, there is a worry that different raters use different standards, and we would like to correct for this. Set up a model for the ratings (with parameters for the applicants and the raters).
- 2. It is possible that some persons on the committee show more variation than others in their ratings. Expand your model to allow for this.

Multilevel logistic regression

The folder speed.dating contains data from an experiment on a few hundred students that randomly assigned each participant to 10 short dates with participants of the opposite sex (Fisman et al., 2006). For each date, each person recorded several subjective numerical ratings of the other person (attractiveness, compatibility, and some other characteristics) and also wrote down whether he or she would like to meet the other person again. Label $y_{ij} = 1$ if person i is interested in seeing person j again 0 otherwise. And r_{ij1}, \ldots, r_{ij6} as person i's numerical ratings of person j on the dimensions of attractiveness, compatibility, and so forth. Please look at http://www.stat.columbia.edu/~gelman/arm/examples/speed.dating/Speed%20Dating%20Data%20Key.doc for details.

1. Fit a classical logistic regression predicting $Pr(y_{ij} = 1)$ given person i's 6 ratings of person j. Discuss the importance of attractiveness, compatibility, and so forth in this predictive model.

```
##
## Call:
  glm(formula = match ~ attr_o + sinc_o + intel_o + fun_o + amb_o +
       shar_o, family = binomial, data = dating)
##
##
##
  Deviance Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                            Max
                     -0.4420
##
  -1.5300
           -0.6362
                              -0.2381
                                         3.1808
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -5.62091
                           0.21859 -25.714 < 2e-16 ***
## attr_o
                0.22047
                           0.02388
                                     9.233
                                            < 2e-16 ***
## sinc_o
               -0.01996
                           0.03067
                                     -0.651
                                              0.5152
## intel_o
                0.07176
                           0.03716
                                     1.931
                                              0.0535
                           0.02922
                                     8.665
## fun_o
                0.25315
                                            < 2e-16 ***
## amb_o
               -0.12099
                           0.02838
                                     -4.264 2.01e-05 ***
                                     9.608 < 2e-16 ***
                0.21225
                           0.02209
## shar_o
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 6466.6 on 7030 degrees of freedom
## Residual deviance: 5611.0 on 7024 degrees of freedom
     (1347 observations deleted due to missingness)
##
## AIC: 5625
##
## Number of Fisher Scoring iterations: 5
```

2. Expand this model to allow varying intercepts for the persons making the evaluation; that is, some people are more likely than others to want to meet someone again. Discuss the fitted model.

```
## Generalized linear mixed model fit by maximum likelihood (Laplace
     Approximation) [glmerMod]
   Family: binomial (logit)
##
## Formula: match ~ gender + attr o + sinc o + intel o + fun o + amb o +
##
      shar o + (1 | iid)
##
      Data: dating
##
##
        AIC
                BIC
                      logLik deviance df.resid
     5543.3
             5605.0 -2762.6
                               5525.3
##
                                          7022
##
## Scaled residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -1.7416 -0.4458 -0.2883 -0.1459 10.3426
##
## Random effects:
   Groups Name
                      Variance Std.Dev.
           (Intercept) 0.4268
                               0.6533
## iid
## Number of obs: 7031, groups: iid, 551
##
## Fixed effects:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -6.02083
                          0.24369 -24.707 < 2e-16 ***
## gender
               0.15329
                          0.09314
                                    1.646
                                           0.0998 .
               0.23540
## attr_o
                          0.02648
                                    8.888 < 2e-16 ***
## sinc_o
               -0.01372
                          0.03261
                                   -0.421
                                            0.6739
                                    1.770
## intel_o
               0.07019
                          0.03967
                                            0.0768 .
               0.26270
                          0.03140
                                    8.366 < 2e-16 ***
## fun o
              -0.13138
                          0.03025
                                   -4.343 1.4e-05 ***
## amb_o
## shar_o
               0.22389
                          0.02325
                                    9.629 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##
           (Intr) gender attr_o sinc_o intel_ fun_o amb_o
## gender -0.192
## attr_o -0.264 0.109
## sinc_o -0.163 0.048 -0.120
## intel o -0.298 -0.055 -0.040 -0.466
          ## fun o
## amb o
           -0.038 -0.092 -0.061 -0.015 -0.372 -0.187
## shar_o -0.056 0.010 -0.099 -0.053 -0.003 -0.265 -0.201
## optimizer (Nelder_Mead) convergence code: 0 (OK)
## Model failed to converge with max|grad| = 0.0385024 (tol = 0.002, component 1)
  3. Expand further to allow varying intercepts for the persons being rated. Discuss the fitted model.
## Generalized linear mixed model fit by maximum likelihood (Laplace
     Approximation) [glmerMod]
##
  Family: binomial (logit)
## Formula: match ~ gender + attr_o + sinc_o + intel_o + fun_o + amb_o +
       shar_o + (1 | iid) + (1 | pid)
##
##
      Data: dating
```

```
##
##
        ATC
                 BIC
                       logLik deviance df.resid
##
     5257.8
              5326.4
                     -2618.9
                                5237.8
##
## Scaled residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
   -3.6948 -0.3825 -0.2195 -0.0921
##
## Random effects:
##
   Groups Name
                       Variance Std.Dev.
           (Intercept) 0.6041
                                0.7773
           (Intercept) 1.2468
                                1.1166
## Number of obs: 7031, groups: iid, 551; pid, 537
##
## Fixed effects:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -8.25536
                           0.38243 -21.587
                                           < 2e-16 ***
## gender
                0.17144
                           0.14935
                                     1.148
                                           0.25100
## attr_o
                0.33694
                           0.03280
                                    10.272
                                           < 2e-16 ***
## sinc o
                0.02002
                           0.03896
                                     0.514
                                            0.60740
## intel_o
                0.10517
                           0.04741
                                     2.218 0.02655 *
                0.30042
                           0.03636
                                     8.263
                                            < 2e-16 ***
## fun o
                                    -2.585 0.00973 **
## amb_o
               -0.09309
                           0.03601
                0.26005
                           0.02844
## shar o
                                     9.144 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##
           (Intr) gender attr_o sinc_o intel_ fun_o amb_o
## gender -0.195
## attr_o
          -0.337
                  0.093
## sinc_o -0.220 0.036 -0.064
## intel_o -0.301 -0.045 -0.025 -0.438
## fun_o
           -0.154 0.009 -0.215 -0.123 -0.099
## amb o
           -0.125 -0.071 -0.051 0.011 -0.334 -0.168
## shar_o -0.100 0.004 -0.075 -0.059 -0.021 -0.237 -0.159
## optimizer (Nelder Mead) convergence code: 0 (OK)
## Model failed to converge with max|grad| = 0.676557 (tol = 0.002, component 1)
```

- 4. You will now fit some models that allow the coefficients for attractiveness, compatibility, and the other attributes to vary by person. Fit a no-pooling model: for each person i, fit a logistic regression to the data y_{ij} for the 10 persons j whom he or she rated, using as predictors the 6 ratings r_{ij1}, \ldots, r_{ij6} . (Hint: with 10 data points and 6 predictors, this model is difficult to fit. You will need to simplify it in some way to get reasonable fits.)
- 5. Fit a multilevel model, allowing the intercept and the coefficients for the 6 ratings to vary by the rater i.

```
## Generalized linear mixed model fit by maximum likelihood (Laplace
## Approximation) [glmerMod]
## Family: binomial ( logit )
## Formula: match ~ gender + attr_o + sinc_o + intel_o + fun_o + amb_o +
## shar_o + (1 + attr_o + sinc_o + intel_o + fun_o + amb_o +
## shar_o | iid) + (1 | pid)
## Data: as.data.frame(dating)
##
```

```
##
                BIC
                      logLik deviance df.resid
       AIC
##
    5295.7
             5549.4 -2610.8
                               5221.7
                                          6994
##
## Scaled residuals:
##
               1Q Median
                               3Q
  -2.7326 -0.3691 -0.2139 -0.0896
                                  7.6375
##
## Random effects:
##
   Groups Name
                      Variance Std.Dev. Corr
##
   iid
           (Intercept) 0.613176 0.78306
##
          attr_o
                      0.025847 0.16077
                                         0.93
##
          sinc_o
                      0.019073 0.13811
                                        -0.13 -0.09
##
          intel_o
                      0.012170 0.11032 -0.59 -0.81 0.22
          fun_o
                      0.042213 0.20546 -0.58 -0.46 -0.54 -0.09
##
##
                      0.009754 0.09876
                                        0.45 0.34 -0.16 0.15 -0.64
          amb_o
##
          shar_o
                      0.018171 0.13480 -0.60 -0.31 0.19 -0.19 0.56 -0.61
           (Intercept) 1.330615 1.15352
##
   pid
## Number of obs: 7031, groups: iid, 551; pid, 537
##
## Fixed effects:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -8.425861
                          0.423136 -19.913 < 2e-16 ***
                                     0.925
                                             0.3551
## gender
               0.141989
                          0.153545
                                     9.078
                                            < 2e-16 ***
## attr o
               0.326907
                          0.036010
## sinc o
               0.003774
                          0.045587
                                     0.083
                                             0.9340
## intel o
               0.127322
                          0.052451
                                     2.427
                                             0.0152 *
## fun_o
               0.325926
                          0.044059
                                     7.397 1.39e-13 ***
              -0.101773
                                    -2.544
## amb_o
                          0.039999
                                             0.0109 *
## shar_o
               0.267084
                          0.033219
                                    8.040 8.98e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
           (Intr) gender attr_o sinc_o intel_ fun_o amb_o
## gender
          -0.185
## attr_o -0.247 0.064
## sinc o -0.215 0.036 -0.052
## intel_o -0.308 -0.040 -0.034 -0.438
## fun o
          -0.071 -0.056 -0.092 0.002 -0.278 -0.218
## amb_o
## shar o -0.136 0.007 -0.080 -0.094 -0.033 -0.098 -0.204
## optimizer (Nelder_Mead) convergence code: 4 (failure to converge in 10000 evaluations)
## unable to evaluate scaled gradient
## Model failed to converge: degenerate Hessian with 3 negative eigenvalues
## failure to converge in 10000 evaluations
```

6. Compare the inferences from the multilevel model in (5) to the no-pooling model in (4) and the complete-pooling model from part (1) of the previous exercise.