

Index sets

$$\begin{aligned} CONSUMERS &= \{1, 2, 3\} \\ COUNTRIES &= \{AUT, DEU, SVN\} \\ SECTORS &= \{A, B, C\} \end{aligned}$$

1 CONSUMER $i \in COUNTRIES$ $h \in CONSUMERS$

1.1 Optimisation problem

$$\max_{(D^{(i,s,h)})_{s \in SECTORS}} U^{(i,h)} = \left(\sum_{s \in SECTORS} \alpha^{(i,s,h)} D^{(i,s,h)\omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} \quad (1.1)$$

s.t. :

$$INC^{(i,h)} + \Pi^{(i,h)} = \sum_{s \in SECTORS} p^{(i,s)} D^{(i,s,h)} \left(\lambda^{\text{CONSUMER}^1(i,h)} \right) \quad (1.2)$$

1.2 Identities

$$INC^{(i,h)} = L^{(i,h)} + p^k K^{(i,h)} \quad (1.3)$$

$$K^{(i,h)} = k s^{\text{data}(i,h)} \quad (1.4)$$

$$L^{(i,h)} = l s^{\text{data}(i,h)} \quad (1.5)$$

1.3 First order conditions

$$s \in SECTORS: \quad \lambda^{\text{CONSUMER}^1(i,h)} p^{(i,s)} + \alpha^{(i,s,h)} D^{(i,s,h)^{-1+\omega}(-1+\omega)} \left(\sum_{s \in SECTORS} \alpha^{(i,s,h)} D^{(i,s,h)\omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad \left(D^{(i,s,h)} \right) \quad (1.6)$$

2 FIRM $i \in COUNTRIES$ $s \in SECTORS$

2.1 Optimisation problem

$$\max_{Y^{\langle i,s \rangle}, K^{\langle i,s \rangle}, L^{\langle i,s \rangle}, (X^{\langle i, \mathfrak{s}l, s \rangle})_{\mathfrak{s}l \in SECTORS}} \pi^{\langle i,s \rangle} = -L^{\langle i,s \rangle} - p^k K^{\langle i,s \rangle} + p^{\langle i,s \rangle} Y^{\langle i,s \rangle} - \sum_{\mathfrak{s}l \in SECTORS} p^{\langle i, \mathfrak{s}l \rangle} X^{\langle i, \mathfrak{s}l, s \rangle} \quad (2.1)$$

s.t. :

$$Y^{\langle i,s \rangle} = \gamma^{\langle i,s \rangle} K^{\langle i,s \rangle} \eta^{k^{\langle i,s \rangle}} L^{\langle i,s \rangle} \eta^{l^{\langle i,s \rangle}} \left(\sum_{\mathfrak{s}l \in SECTORS} \beta^{x^{\langle i, \mathfrak{s}l, s \rangle}} X^{\langle i, \mathfrak{s}l, s \rangle} \rho^{\langle i \rangle} \right)^{\eta^{x^{\langle i,s \rangle}} \rho^{\langle i \rangle} - 1} \left(\lambda^{\text{FIRM}^1 \langle i,s \rangle} \right) \quad (2.2)$$

2.2 First order conditions

$$-\lambda^{\text{FIRM}^1 \langle i,s \rangle} + p^{\langle i,s \rangle} = 0 \quad \left(Y^{\langle i,s \rangle} \right) \quad (2.3)$$

$$-p^k + \eta^{k^{\langle i,s \rangle}} \gamma^{\langle i,s \rangle} \lambda^{\text{FIRM}^1 \langle i,s \rangle} K^{\langle i,s \rangle - 1 + \eta^{k^{\langle i,s \rangle}}} L^{\langle i,s \rangle} \eta^{l^{\langle i,s \rangle}} \left(\sum_{\mathfrak{s}l \in SECTORS} \beta^{x^{\langle i, \mathfrak{s}l, s \rangle}} X^{\langle i, \mathfrak{s}l, s \rangle} \rho^{\langle i \rangle} \right)^{\eta^{x^{\langle i,s \rangle}} \rho^{\langle i \rangle} - 1} = 0 \quad \left(K^{\langle i,s \rangle} \right) \quad (2.4)$$

$$-1 + \eta^{l^{\langle i,s \rangle}} \gamma^{\langle i,s \rangle} \lambda^{\text{FIRM}^1 \langle i,s \rangle} K^{\langle i,s \rangle} \eta^{k^{\langle i,s \rangle}} L^{\langle i,s \rangle - 1 + \eta^{l^{\langle i,s \rangle}}} \left(\sum_{\mathfrak{s}l \in SECTORS} \beta^{x^{\langle i, \mathfrak{s}l, s \rangle}} X^{\langle i, \mathfrak{s}l, s \rangle} \rho^{\langle i \rangle} \right)^{\eta^{x^{\langle i,s \rangle}} \rho^{\langle i \rangle} - 1} = 0 \quad \left(L^{\langle i,s \rangle} \right) \quad (2.5)$$

$$\mathfrak{s}l \in SECTORS: \quad -p^{\langle i, \mathfrak{s}l \rangle} + \beta^{x^{\langle i, \mathfrak{s}l, s \rangle}} \eta^{x^{\langle i,s \rangle}} \gamma^{\langle i,s \rangle} \lambda^{\text{FIRM}^1 \langle i,s \rangle} K^{\langle i,s \rangle} \eta^{k^{\langle i,s \rangle}} L^{\langle i,s \rangle} \eta^{l^{\langle i,s \rangle}} X^{\langle i, \mathfrak{s}l, s \rangle - 1 + \rho^{\langle i \rangle}} \left(\sum_{\mathfrak{s}l \in SECTORS} \beta^{x^{\langle i, \mathfrak{s}l, s \rangle}} X^{\langle i, \mathfrak{s}l, s \rangle} \rho^{\langle i \rangle} \right)^{-1 + \eta^{x^{\langle i,s \rangle}} \rho^{\langle i \rangle} - 1} = 0 \quad \left(X^{\langle i, \mathfrak{s}l, s \rangle} \right) \quad (2.6)$$

2.3 First order conditions after reduction

$$-p^k + \eta^{k^{\langle i,s \rangle}} \gamma^{\langle i,s \rangle} p^{\langle i,s \rangle} K^{\langle i,s \rangle - 1 + \eta^{k^{\langle i,s \rangle}}} L^{\langle i,s \rangle} \eta^{l^{\langle i,s \rangle}} \left(\sum_{\mathfrak{s}l \in SECTORS} \beta^{x^{\langle i, \mathfrak{s}l, s \rangle}} X^{\langle i, \mathfrak{s}l, s \rangle} \rho^{\langle i \rangle} \right)^{\eta^{x^{\langle i,s \rangle}} \rho^{\langle i \rangle} - 1} = 0 \quad \left(K^{\langle i,s \rangle} \right) \quad (2.7)$$

$$-1 + \eta^{l^{\langle i,s \rangle}} \gamma^{\langle i,s \rangle} p^{\langle i,s \rangle} K^{\langle i,s \rangle} \eta^{k^{\langle i,s \rangle}} L^{\langle i,s \rangle - 1 + \eta^{l^{\langle i,s \rangle}}} \left(\sum_{\mathfrak{s}l \in SECTORS} \beta^{x^{\langle i, \mathfrak{s}l, s \rangle}} X^{\langle i, \mathfrak{s}l, s \rangle} \rho^{\langle i \rangle} \right)^{\eta^{x^{\langle i,s \rangle}} \rho^{\langle i \rangle} - 1} = 0 \quad \left(L^{\langle i,s \rangle} \right) \quad (2.8)$$

$$s_i \in SECTORS: \quad -p^{\langle i, s_i \rangle} + \beta^x \langle i, s_i, s \rangle \eta^{x \langle i, s \rangle} \gamma^{\langle i, s \rangle} p^{\langle i, s \rangle} K^{\langle i, s \rangle} \eta^{k \langle i, s \rangle} L^{\langle i, s \rangle} \eta^{l \langle i, s \rangle} X^{\langle i, s_i, s \rangle - 1 + \rho^{\langle i \rangle}} \left(\sum_{s \in SECTORS} \beta^x \langle i, s_i, s \rangle X^{\langle i, s_i, s \rangle} \rho^{\langle i \rangle} \right)^{-1 + \eta^{x \langle i, s \rangle} \rho^{\langle i \rangle} - 1} = 0 \quad \left(\left(X^{\langle i, s_i, s \rangle} \right)_{s_i \in SECTORS} \right) \quad (2.9)$$

3 EQUILIBRIUM

3.1 Identities

$$i \in COUNTRIES: \quad \sum_{h \in CONSUMERS} K^{\langle i, h \rangle} = \sum_{s \in SECTORS} K^{\langle i, s \rangle} \quad (3.1)$$

$$s \in SECTORS: \quad p^{\langle AUT, s \rangle} = 1 \quad (3.2)$$

$$i \in COUNTRIES \setminus \{AUT\}: \quad s \in SECTORS \setminus \{A\}: \quad p^{\langle i, s \rangle} = 1 \quad (3.3)$$

$$i \in COUNTRIES: \quad h \in CONSUMERS: \quad \Pi^{\langle i, h \rangle} = \pi^{h \langle i, h \rangle} \left(\sum_{s \in SECTORS} \pi^{\langle i, s \rangle} \right) \quad (3.4)$$

4 Equilibrium relationships (before expansion and reduction)

$$i \in COUNTRIES \setminus \{AUT\}: \quad s \in SECTORS \setminus \{A\}: \quad 1 - p^{\langle i, s \rangle} = 0 \quad (4.1)$$

$$i \in COUNTRIES: \quad - \sum_{h \in CONSUMERS} K^{\langle i, h \rangle} + \sum_{s \in SECTORS} K^{\langle i, s \rangle} = 0 \quad (4.2)$$

$$i \in COUNTRIES: \quad h \in CONSUMERS: \quad ks^{\text{data} \langle i, h \rangle} - K^{\langle i, h \rangle} = 0 \quad (4.3)$$

$$i \in COUNTRIES: \quad h \in CONSUMERS: \quad ls^{\text{data} \langle i, h \rangle} - L^{\langle i, h \rangle} = 0 \quad (4.4)$$

$$i \in COUNTRIES: \quad h \in CONSUMERS: \quad - \Pi^{\langle i, h \rangle} + \pi^{h \langle i, h \rangle} \left(\sum_{s \in SECTORS} \pi^{\langle i, s \rangle} \right) = 0 \quad (4.5)$$

$$i \in COUNTRIES: \quad h \in CONSUMERS: \quad U^{\langle i, h \rangle} - \left(\sum_{s \in SECTORS} \alpha^{\langle i, s, h \rangle} D^{\langle i, s, h \rangle} \omega^{-1(-1+\omega)} \right)^{\omega(-1+\omega)-1} = 0 \quad (4.6)$$

$$i \in COUNTRIES: \quad h \in CONSUMERS: \quad -INC^{\langle i,h \rangle} + L^{\langle i,h \rangle} + p^k K^{\langle i,h \rangle} = 0 \quad (4.7)$$

$$i \in COUNTRIES: \quad h \in CONSUMERS: \quad -INC^{\langle i,h \rangle} - \Pi^{\langle i,h \rangle} + \sum_{s \in SECTORS} p^{\langle i,s \rangle} D^{\langle i,s,h \rangle} = 0 \quad (4.8)$$

$$i \in COUNTRIES: \quad h \in CONSUMERS: \quad s \in SECTORS: \quad \lambda^{\text{CONSUMER}^1 \langle i,h \rangle} p^{\langle i,s \rangle + \alpha \langle i,s,h \rangle} D^{\langle i,s,h \rangle - 1 + \omega^{-1}(-1+\omega)} \left(\sum_{s \in SECTORS} \alpha^{\langle i,s,h \rangle} D^{\langle i,s,h \rangle \omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad (4.9)$$

$$i \in COUNTRIES: \quad s \in SECTORS: \quad -1 + \eta^{1 \langle i,s \rangle} \gamma^{\langle i,s \rangle} p^{\langle i,s \rangle} K^{\langle i,s \rangle} \eta^{k \langle i,s \rangle} L^{\langle i,s \rangle - 1 + \eta^{1 \langle i,s \rangle}} \left(\sum_{\mathfrak{s} \in SECTORS} \beta^{\mathbf{x} \langle i,\mathfrak{s},s \rangle} X^{\langle i,\mathfrak{s},s \rangle \rho^{\langle i \rangle}} \right)^{\eta^{\mathbf{x} \langle i,s \rangle} \rho^{\langle i \rangle - 1}} = 0 \quad (4.10)$$

$$i \in COUNTRIES: \quad s \in SECTORS: \quad -p^k + \eta^{k \langle i,s \rangle} \gamma^{\langle i,s \rangle} p^{\langle i,s \rangle} K^{\langle i,s \rangle - 1 + \eta^{k \langle i,s \rangle}} L^{\langle i,s \rangle} \eta^{1 \langle i,s \rangle} \left(\sum_{\mathfrak{s} \in SECTORS} \beta^{\mathbf{x} \langle i,\mathfrak{s},s \rangle} X^{\langle i,\mathfrak{s},s \rangle \rho^{\langle i \rangle}} \right)^{\eta^{\mathbf{x} \langle i,s \rangle} \rho^{\langle i \rangle - 1}} = 0 \quad (4.11)$$

$$i \in COUNTRIES: \quad s \in SECTORS: \quad -Y^{\langle i,s \rangle} + \gamma^{\langle i,s \rangle} K^{\langle i,s \rangle} \eta^{k \langle i,s \rangle} L^{\langle i,s \rangle} \eta^{1 \langle i,s \rangle} \left(\sum_{\mathfrak{s} \in SECTORS} \beta^{\mathbf{x} \langle i,\mathfrak{s},s \rangle} X^{\langle i,\mathfrak{s},s \rangle \rho^{\langle i \rangle}} \right)^{\eta^{\mathbf{x} \langle i,s \rangle} \rho^{\langle i \rangle - 1}} = 0 \quad (4.12)$$

$$i \in COUNTRIES: \quad s \in SECTORS: \quad \pi^{\langle i,s \rangle} + L^{\langle i,s \rangle} + p^k K^{\langle i,s \rangle} - p^{\langle i,s \rangle} Y^{\langle i,s \rangle} + \sum_{\mathfrak{s} \in SECTORS} p^{\langle i,\mathfrak{s} \rangle} X^{\langle i,\mathfrak{s},s \rangle} = 0 \quad (4.13)$$

$$i \in COUNTRIES: \quad s \in SECTORS: \quad \mathfrak{s} \in SECTORS: \quad -p^{\langle i,\mathfrak{s} \rangle} + \beta^{\mathbf{x} \langle i,\mathfrak{s},s \rangle} \eta^{\mathbf{x} \langle i,s \rangle} \gamma^{\langle i,s \rangle} p^{\langle i,s \rangle} K^{\langle i,s \rangle} \eta^{k \langle i,s \rangle} L^{\langle i,s \rangle} \eta^{1 \langle i,s \rangle} X^{\langle i,\mathfrak{s},s \rangle - 1 + \rho^{\langle i \rangle}} \left(\sum_{\mathfrak{s} \in SECTORS} \beta^{\mathbf{x} \langle i,\mathfrak{s},s \rangle} X^{\langle i,\mathfrak{s},s \rangle \rho^{\langle i \rangle}} \right)^{-1 + \eta^{\mathbf{x} \langle i,s \rangle} \rho^{\langle i \rangle - 1}} = 0 \quad (4.14)$$

$$s \in SECTORS: \quad 1 - p^{\langle \text{AUT},s \rangle} = 0 \quad (4.15)$$

5 Equilibrium relationships (after expansion and reduction)

$$-1 + \eta^{1 \langle \text{AUT},A \rangle} \gamma^{\langle \text{AUT},A \rangle} p^{\langle \text{AUT},A \rangle} K^{\langle \text{AUT},A \rangle} \eta^{k \langle \text{AUT},A \rangle} L^{\langle \text{AUT},A \rangle - 1 + \eta^{1 \langle \text{AUT},A \rangle}} \left(\beta^{\mathbf{x} \langle \text{AUT},A,A \rangle} X^{\langle \text{AUT},A,A \rangle \rho^{\langle \text{AUT} \rangle}} + \beta^{\mathbf{x} \langle \text{AUT},B,A \rangle} X^{\langle \text{AUT},B,A \rangle \rho^{\langle \text{AUT} \rangle}} + \beta^{\mathbf{x} \langle \text{AUT},C,A \rangle} X^{\langle \text{AUT},C,A \rangle \rho^{\langle \text{AUT} \rangle}} \right)^{\eta^{\mathbf{x} \langle \text{AUT},A \rangle} \rho^{\langle \text{AUT} \rangle - 1}} = 0 \quad (5.1)$$

$$1 - p^{\langle \text{AUT}, \text{A} \rangle} = 0 \quad (5.10)$$

$$1 - p^{\langle \text{AUT}, \text{B} \rangle} = 0 \quad (5.11)$$

$$1 - p^{\langle \text{AUT}, \text{C} \rangle} = 0 \quad (5.12)$$

$$1 - p^{\langle \text{DEU}, \text{B} \rangle} = 0 \quad (5.13)$$

$$1 - p^{\langle \text{DEU}, \text{C} \rangle} = 0 \quad (5.14)$$

$$1 - p^{\langle \text{SVN}, \text{B} \rangle} = 0 \quad (5.15)$$

$$1 - p^{\langle \text{SVN}, \text{C} \rangle} = 0 \quad (5.16)$$

$$k_{\text{S}}^{\text{data} \langle \text{AUT}, 1 \rangle} - K^{\langle \text{AUT}, 1 \rangle} = 0 \quad (5.17)$$

$$k_{\text{S}}^{\text{data} \langle \text{AUT}, 2 \rangle} - K^{\langle \text{AUT}, 2 \rangle} = 0 \quad (5.18)$$

$$k_{\text{S}}^{\text{data} \langle \text{AUT}, 3 \rangle} - K^{\langle \text{AUT}, 3 \rangle} = 0 \quad (5.19)$$

$$k_{\text{S}}^{\text{data} \langle \text{DEU}, 1 \rangle} - K^{\langle \text{DEU}, 1 \rangle} = 0 \quad (5.20)$$

$$k_{\text{S}}^{\text{data} \langle \text{DEU}, 2 \rangle} - K^{\langle \text{DEU}, 2 \rangle} = 0 \quad (5.21)$$

$$k_{\text{S}}^{\text{data} \langle \text{DEU}, 3 \rangle} - K^{\langle \text{DEU}, 3 \rangle} = 0 \quad (5.22)$$

$$k_{\text{S}}^{\text{data} \langle \text{SVN}, 1 \rangle} - K^{\langle \text{SVN}, 1 \rangle} = 0 \quad (5.23)$$

$$k_{\text{S}}^{\text{data} \langle \text{SVN}, 2 \rangle} - K^{\langle \text{SVN}, 2 \rangle} = 0 \quad (5.24)$$

$$k_{\text{S}}^{\text{data} \langle \text{SVN}, 3 \rangle} - K^{\langle \text{SVN}, 3 \rangle} = 0 \quad (5.25)$$

$$l_s^{\text{data}\langle\text{AUT},1\rangle} - L^{\langle\text{AUT},1\rangle} = 0 \quad (5.26)$$

$$l_s^{\text{data}\langle\text{AUT},2\rangle} - L^{\langle\text{AUT},2\rangle} = 0 \quad (5.27)$$

$$l_s^{\text{data}\langle\text{AUT},3\rangle} - L^{\langle\text{AUT},3\rangle} = 0 \quad (5.28)$$

$$l_s^{\text{data}\langle\text{DEU},1\rangle} - L^{\langle\text{DEU},1\rangle} = 0 \quad (5.29)$$

$$l_s^{\text{data}\langle\text{DEU},2\rangle} - L^{\langle\text{DEU},2\rangle} = 0 \quad (5.30)$$

$$l_s^{\text{data}\langle\text{DEU},3\rangle} - L^{\langle\text{DEU},3\rangle} = 0 \quad (5.31)$$

$$l_s^{\text{data}\langle\text{SVN},1\rangle} - L^{\langle\text{SVN},1\rangle} = 0 \quad (5.32)$$

$$l_s^{\text{data}\langle\text{SVN},2\rangle} - L^{\langle\text{SVN},2\rangle} = 0 \quad (5.33)$$

$$l_s^{\text{data}\langle\text{SVN},3\rangle} - L^{\langle\text{SVN},3\rangle} = 0 \quad (5.34)$$

$$-p^k + \eta^{k\langle\text{AUT},\text{A}\rangle} \gamma^{\langle\text{AUT},\text{A}\rangle} p^{\langle\text{AUT},\text{A}\rangle} K^{\langle\text{AUT},\text{A}\rangle - 1 + \eta^{k\langle\text{AUT},\text{A}\rangle}} L^{\langle\text{AUT},\text{A}\rangle} \eta^{1\langle\text{AUT},\text{A}\rangle} \left(\beta^{\text{x}\langle\text{AUT},\text{A},\text{A}\rangle} X^{\langle\text{AUT},\text{A},\text{A}\rangle \rho^{\langle\text{AUT}\rangle}} + \beta^{\text{x}\langle\text{AUT},\text{B},\text{A}\rangle} X^{\langle\text{AUT},\text{B},\text{A}\rangle \rho^{\langle\text{AUT}\rangle}} + \beta^{\text{x}\langle\text{AUT},\text{C},\text{A}\rangle} X^{\langle\text{AUT},\text{C},\text{A}\rangle \rho^{\langle\text{AUT}\rangle}} \right)^{\eta^{\text{x}\langle\text{AUT},\text{A}\rangle} \rho^{\langle\text{AUT}\rangle}} \quad (5.35)$$

$$-p^k + \eta^{k\langle\text{AUT},\text{B}\rangle} \gamma^{\langle\text{AUT},\text{B}\rangle} p^{\langle\text{AUT},\text{B}\rangle} K^{\langle\text{AUT},\text{B}\rangle - 1 + \eta^{k\langle\text{AUT},\text{B}\rangle}} L^{\langle\text{AUT},\text{B}\rangle} \eta^{1\langle\text{AUT},\text{B}\rangle} \left(\beta^{\text{x}\langle\text{AUT},\text{A},\text{B}\rangle} X^{\langle\text{AUT},\text{A},\text{B}\rangle \rho^{\langle\text{AUT}\rangle}} + \beta^{\text{x}\langle\text{AUT},\text{B},\text{B}\rangle} X^{\langle\text{AUT},\text{B},\text{B}\rangle \rho^{\langle\text{AUT}\rangle}} + \beta^{\text{x}\langle\text{AUT},\text{C},\text{B}\rangle} X^{\langle\text{AUT},\text{C},\text{B}\rangle \rho^{\langle\text{AUT}\rangle}} \right)^{\eta^{\text{x}\langle\text{AUT},\text{B}\rangle} \rho^{\langle\text{AUT}\rangle}} \quad (5.36)$$

$$-p^k + \eta^{k\langle\text{AUT},\text{C}\rangle} \gamma^{\langle\text{AUT},\text{C}\rangle} p^{\langle\text{AUT},\text{C}\rangle} K^{\langle\text{AUT},\text{C}\rangle - 1 + \eta^{k\langle\text{AUT},\text{C}\rangle}} L^{\langle\text{AUT},\text{C}\rangle} \eta^{1\langle\text{AUT},\text{C}\rangle} \left(\beta^{\text{x}\langle\text{AUT},\text{A},\text{C}\rangle} X^{\langle\text{AUT},\text{A},\text{C}\rangle \rho^{\langle\text{AUT}\rangle}} + \beta^{\text{x}\langle\text{AUT},\text{B},\text{C}\rangle} X^{\langle\text{AUT},\text{B},\text{C}\rangle \rho^{\langle\text{AUT}\rangle}} + \beta^{\text{x}\langle\text{AUT},\text{C},\text{C}\rangle} X^{\langle\text{AUT},\text{C},\text{C}\rangle \rho^{\langle\text{AUT}\rangle}} \right)^{\eta^{\text{x}\langle\text{AUT},\text{C}\rangle} \rho^{\langle\text{AUT}\rangle}} \quad (5.37)$$

$$-p^{\langle \text{SVN}, C \rangle} + \beta^{\text{x} \langle \text{SVN}, C, C \rangle} \eta^{\text{x} \langle \text{SVN}, C \rangle} \gamma^{\langle \text{SVN}, C \rangle} p^{\langle \text{SVN}, C \rangle} K^{\langle \text{SVN}, C \rangle} \eta^{k^{\langle \text{SVN}, C \rangle}} L^{\langle \text{SVN}, C \rangle} \eta^{1^{\langle \text{SVN}, C \rangle}} X^{\langle \text{SVN}, C, C \rangle - 1 + \rho^{\langle \text{SVN} \rangle}} \left(\beta^{\text{x} \langle \text{SVN}, A, C \rangle} X^{\langle \text{SVN}, A, C \rangle} \rho^{\langle \text{SVN} \rangle} + \beta^{\text{x} \langle \text{SVN}, B, C \rangle} X^{\langle \text{SVN}, B, C \rangle} \rho^{\langle \text{SVN} \rangle} + \beta^{\text{x} \langle \text{SVN}, C, C \rangle} X^{\langle \text{SVN}, C, C \rangle} \rho^{\langle \text{SVN} \rangle} \right) \quad (5.70)$$

$$-\Pi^{\langle \text{AUT}, 1 \rangle} + \pi^{\text{h}\langle \text{AUT}, 1 \rangle} \left(\pi^{\langle \text{AUT}, \text{A} \rangle} + \pi^{\langle \text{AUT}, \text{B} \rangle} + \pi^{\langle \text{AUT}, \text{C} \rangle} \right) = 0 \quad (5.71)$$

$$-\Pi^{\langle \text{AUT}, 2 \rangle} + \pi^{\text{h}\langle \text{AUT}, 2 \rangle} \left(\pi^{\langle \text{AUT}, \text{A} \rangle} + \pi^{\langle \text{AUT}, \text{B} \rangle} + \pi^{\langle \text{AUT}, \text{C} \rangle} \right) = 0 \quad (5.72)$$

$$-\Pi^{\langle \text{AUT}, 3 \rangle} + \pi^{\text{h}\langle \text{AUT}, 3 \rangle} \left(\pi^{\langle \text{AUT}, \text{A} \rangle} + \pi^{\langle \text{AUT}, \text{B} \rangle} + \pi^{\langle \text{AUT}, \text{C} \rangle} \right) = 0 \quad (5.73)$$

$$-\Pi^{\langle \text{DEU}, 1 \rangle} + \pi^{\text{h} \langle \text{DEU}, 1 \rangle} \left(\pi^{\langle \text{DEU}, \text{A} \rangle} + \pi^{\langle \text{DEU}, \text{B} \rangle} + \pi^{\langle \text{DEU}, \text{C} \rangle} \right) = 0 \quad (5.74)$$

$$-\Pi^{\langle \text{DEU}, 2 \rangle} + \pi^{\text{h} \langle \text{DEU}, 2 \rangle} \left(\pi^{\langle \text{DEU}, \text{A} \rangle} + \pi^{\langle \text{DEU}, \text{B} \rangle} + \pi^{\langle \text{DEU}, \text{C} \rangle} \right) = 0 \quad (5.75)$$

$$-\Pi^{\langle \text{DEU}, 3 \rangle} + \pi^{\text{h} \langle \text{DEU}, 3 \rangle} \left(\pi^{\langle \text{DEU}, \text{A} \rangle} + \pi^{\langle \text{DEU}, \text{B} \rangle} + \pi^{\langle \text{DEU}, \text{C} \rangle} \right) = 0 \quad (5.76)$$

$$-\Pi^{\langle \text{SVN}, 1 \rangle} + \pi^{\text{h} \langle \text{SVN}, 1 \rangle} \left(\pi^{\langle \text{SVN}, \text{A} \rangle} + \pi^{\langle \text{SVN}, \text{B} \rangle} + \pi^{\langle \text{SVN}, \text{C} \rangle} \right) = 0 \quad (5.77)$$

$$-\Pi^{\langle \text{SVN}, 2 \rangle} + \pi^{\text{h} \langle \text{SVN}, 2 \rangle} \left(\pi^{\langle \text{SVN}, \text{A} \rangle} + \pi^{\langle \text{SVN}, \text{B} \rangle} + \pi^{\langle \text{SVN}, \text{C} \rangle} \right) = 0 \quad (5.78)$$

$$-\Pi^{\langle \text{SVN},3 \rangle} + \pi^{\text{h}\langle \text{SVN},3 \rangle} \left(\pi^{\langle \text{SVN},\text{A} \rangle} + \pi^{\langle \text{SVN},\text{B} \rangle} + \pi^{\langle \text{SVN},\text{C} \rangle} \right) = 0 \quad (5.79)$$

$$U^{\langle \text{AUT}, 1 \rangle} - \left(\alpha^{\langle \text{AUT}, \text{A}, 1 \rangle} D^{\langle \text{AUT}, \text{A}, 1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle \text{AUT}, \text{B}, 1 \rangle} D^{\langle \text{AUT}, \text{B}, 1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle \text{AUT}, \text{C}, 1 \rangle} D^{\langle \text{AUT}, \text{C}, 1 \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} = 0 \quad (5.80)$$

$$U^{\langle \text{AUT}, 2 \rangle} - \left(\alpha^{\langle \text{AUT}, \text{A}, 2 \rangle} D^{\langle \text{AUT}, \text{A}, 2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle \text{AUT}, \text{B}, 2 \rangle} D^{\langle \text{AUT}, \text{B}, 2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle \text{AUT}, \text{C}, 2 \rangle} D^{\langle \text{AUT}, \text{C}, 2 \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} = 0 \quad (5.81)$$

$$U^{\langle \text{AUT}, 3 \rangle} - \left(\alpha^{\langle \text{AUT}, \text{A}, 3 \rangle} D^{\langle \text{AUT}, \text{A}, 3 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle \text{AUT}, \text{B}, 3 \rangle} D^{\langle \text{AUT}, \text{B}, 3 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle \text{AUT}, \text{C}, 3 \rangle} D^{\langle \text{AUT}, \text{C}, 3 \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} = 0 \quad (5.82)$$

$$U^{\langle \text{DEU}, 1 \rangle} - \left(\alpha^{\langle \text{DEU}, \text{A}, 1 \rangle} D^{\langle \text{DEU}, \text{A}, 1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle \text{DEU}, \text{B}, 1 \rangle} D^{\langle \text{DEU}, \text{B}, 1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle \text{DEU}, \text{C}, 1 \rangle} D^{\langle \text{DEU}, \text{C}, 1 \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} = 0 \quad (5.83)$$

$$-INC^{\langle DEU,1 \rangle} + L^{\langle DEU,1 \rangle} + p^k K^{\langle DEU,1 \rangle} = 0 \quad (5.128)$$

$$-INC^{\langle DEU,2 \rangle} + L^{\langle DEU,2 \rangle} + p^k K^{\langle DEU,2 \rangle} = 0 \quad (5.129)$$

$$-INC^{\langle DEU,3 \rangle} + L^{\langle DEU,3 \rangle} + p^k K^{\langle DEU,3 \rangle} = 0 \quad (5.130)$$

$$-INC^{\langle SVN,1 \rangle} + L^{\langle SVN,1 \rangle} + p^k K^{\langle SVN,1 \rangle} = 0 \quad (5.131)$$

$$-INC^{\langle SVN,2 \rangle} + L^{\langle SVN,2 \rangle} + p^k K^{\langle SVN,2 \rangle} = 0 \quad (5.132)$$

$$-INC^{\langle SVN,3 \rangle} + L^{\langle SVN,3 \rangle} + p^k K^{\langle SVN,3 \rangle} = 0 \quad (5.133)$$

$$-INC^{\langle AUT,1 \rangle} - \Pi^{\langle AUT,1 \rangle} + p^{\langle AUT,A \rangle} D^{\langle AUT,A,1 \rangle} + p^{\langle AUT,B \rangle} D^{\langle AUT,B,1 \rangle} + p^{\langle AUT,C \rangle} D^{\langle AUT,C,1 \rangle} = 0 \quad (5.134)$$

$$-INC^{\langle AUT,2 \rangle} - \Pi^{\langle AUT,2 \rangle} + p^{\langle AUT,A \rangle} D^{\langle AUT,A,2 \rangle} + p^{\langle AUT,B \rangle} D^{\langle AUT,B,2 \rangle} + p^{\langle AUT,C \rangle} D^{\langle AUT,C,2 \rangle} = 0 \quad (5.135)$$

$$-INC^{\langle AUT,3 \rangle} - \Pi^{\langle AUT,3 \rangle} + p^{\langle AUT,A \rangle} D^{\langle AUT,A,3 \rangle} + p^{\langle AUT,B \rangle} D^{\langle AUT,B,3 \rangle} + p^{\langle AUT,C \rangle} D^{\langle AUT,C,3 \rangle} = 0 \quad (5.136)$$

$$-INC^{\langle DEU,1 \rangle} - \Pi^{\langle DEU,1 \rangle} + p^{\langle DEU,A \rangle} D^{\langle DEU,A,1 \rangle} + p^{\langle DEU,B \rangle} D^{\langle DEU,B,1 \rangle} + p^{\langle DEU,C \rangle} D^{\langle DEU,C,1 \rangle} = 0 \quad (5.137)$$

$$-INC^{\langle DEU,2 \rangle} - \Pi^{\langle DEU,2 \rangle} + p^{\langle DEU,A \rangle} D^{\langle DEU,A,2 \rangle} + p^{\langle DEU,B \rangle} D^{\langle DEU,B,2 \rangle} + p^{\langle DEU,C \rangle} D^{\langle DEU,C,2 \rangle} = 0 \quad (5.138)$$

$$-INC^{\langle DEU,3 \rangle} - \Pi^{\langle DEU,3 \rangle} + p^{\langle DEU,A \rangle} D^{\langle DEU,A,3 \rangle} + p^{\langle DEU,B \rangle} D^{\langle DEU,B,3 \rangle} + p^{\langle DEU,C \rangle} D^{\langle DEU,C,3 \rangle} = 0 \quad (5.139)$$

$$-INC^{\langle SVN,1 \rangle} - \Pi^{\langle SVN,1 \rangle} + p^{\langle SVN,A \rangle} D^{\langle SVN,A,1 \rangle} + p^{\langle SVN,B \rangle} D^{\langle SVN,B,1 \rangle} + p^{\langle SVN,C \rangle} D^{\langle SVN,C,1 \rangle} = 0 \quad (5.140)$$

$$-INC^{\langle SVN,2 \rangle} - \Pi^{\langle SVN,2 \rangle} + p^{\langle SVN,A \rangle} D^{\langle SVN,A,2 \rangle} + p^{\langle SVN,B \rangle} D^{\langle SVN,B,2 \rangle} + p^{\langle SVN,C \rangle} D^{\langle SVN,C,2 \rangle} = 0 \quad (5.141)$$

$$-INC^{\langle SVN,3 \rangle} - \Pi^{\langle SVN,3 \rangle} + p^{\langle SVN,A \rangle} D^{\langle SVN,A,3 \rangle} + p^{\langle SVN,B \rangle} D^{\langle SVN,B,3 \rangle} + p^{\langle SVN,C \rangle} D^{\langle SVN,C,3 \rangle} = 0 \quad (5.142)$$

$$-K^{\langle AUT,1 \rangle} - K^{\langle AUT,2 \rangle} - K^{\langle AUT,3 \rangle} + K^{\langle AUT,A \rangle} + K^{\langle AUT,B \rangle} + K^{\langle AUT,C \rangle} = 0 \quad (5.143)$$

$$-K^{\langle \text{DEU},1 \rangle} - K^{\langle \text{DEU},2 \rangle} - K^{\langle \text{DEU},3 \rangle} + K^{\langle \text{DEU},A \rangle} + K^{\langle \text{DEU},B \rangle} + K^{\langle \text{DEU},C \rangle} = 0 \quad (5.144)$$

$$-K^{\langle \text{SVN},1 \rangle} - K^{\langle \text{SVN},2 \rangle} - K^{\langle \text{SVN},3 \rangle} + K^{\langle \text{SVN},A \rangle} + K^{\langle \text{SVN},B \rangle} + K^{\langle \text{SVN},C \rangle} = 0 \quad (5.145)$$

$$\pi^{\langle \text{AUT},A \rangle} + L^{\langle \text{AUT},A \rangle} + p^k K^{\langle \text{AUT},A \rangle} + p^{\langle \text{AUT},A \rangle} X^{\langle \text{AUT},A,A \rangle} - p^{\langle \text{AUT},A \rangle} Y^{\langle \text{AUT},A \rangle} + p^{\langle \text{AUT},B \rangle} X^{\langle \text{AUT},B,A \rangle} + p^{\langle \text{AUT},C \rangle} X^{\langle \text{AUT},C,A \rangle} = 0 \quad (5.146)$$

$$\pi^{\langle \text{AUT},B \rangle} + L^{\langle \text{AUT},B \rangle} + p^k K^{\langle \text{AUT},B \rangle} + p^{\langle \text{AUT},A \rangle} X^{\langle \text{AUT},A,B \rangle} + p^{\langle \text{AUT},B \rangle} X^{\langle \text{AUT},B,B \rangle} - p^{\langle \text{AUT},B \rangle} Y^{\langle \text{AUT},B \rangle} + p^{\langle \text{AUT},C \rangle} X^{\langle \text{AUT},C,B \rangle} = 0 \quad (5.147)$$

$$\pi^{\langle \text{AUT},C \rangle} + L^{\langle \text{AUT},C \rangle} + p^k K^{\langle \text{AUT},C \rangle} + p^{\langle \text{AUT},A \rangle} X^{\langle \text{AUT},A,C \rangle} + p^{\langle \text{AUT},B \rangle} X^{\langle \text{AUT},B,C \rangle} + p^{\langle \text{AUT},C \rangle} X^{\langle \text{AUT},C,C \rangle} - p^{\langle \text{AUT},C \rangle} Y^{\langle \text{AUT},C \rangle} = 0 \quad (5.148)$$

$$\pi^{\langle \text{DEU},A \rangle} + L^{\langle \text{DEU},A \rangle} + p^k K^{\langle \text{DEU},A \rangle} + p^{\langle \text{DEU},A \rangle} X^{\langle \text{DEU},A,A \rangle} - p^{\langle \text{DEU},A \rangle} Y^{\langle \text{DEU},A \rangle} + p^{\langle \text{DEU},B \rangle} X^{\langle \text{DEU},B,A \rangle} + p^{\langle \text{DEU},C \rangle} X^{\langle \text{DEU},C,A \rangle} = 0 \quad (5.149)$$

$$\pi^{\langle \text{DEU},B \rangle} + L^{\langle \text{DEU},B \rangle} + p^k K^{\langle \text{DEU},B \rangle} + p^{\langle \text{DEU},A \rangle} X^{\langle \text{DEU},A,B \rangle} + p^{\langle \text{DEU},B \rangle} X^{\langle \text{DEU},B,B \rangle} - p^{\langle \text{DEU},B \rangle} Y^{\langle \text{DEU},B \rangle} + p^{\langle \text{DEU},C \rangle} X^{\langle \text{DEU},C,B \rangle} = 0 \quad (5.150)$$

$$\pi^{\langle \text{DEU},C \rangle} + L^{\langle \text{DEU},C \rangle} + p^k K^{\langle \text{DEU},C \rangle} + p^{\langle \text{DEU},A \rangle} X^{\langle \text{DEU},A,C \rangle} + p^{\langle \text{DEU},B \rangle} X^{\langle \text{DEU},B,C \rangle} + p^{\langle \text{DEU},C \rangle} X^{\langle \text{DEU},C,C \rangle} - p^{\langle \text{DEU},C \rangle} Y^{\langle \text{DEU},C \rangle} = 0 \quad (5.151)$$

$$\pi^{\langle \text{SVN},A \rangle} + L^{\langle \text{SVN},A \rangle} + p^k K^{\langle \text{SVN},A \rangle} + p^{\langle \text{SVN},A \rangle} X^{\langle \text{SVN},A,A \rangle} - p^{\langle \text{SVN},A \rangle} Y^{\langle \text{SVN},A \rangle} + p^{\langle \text{SVN},B \rangle} X^{\langle \text{SVN},B,A \rangle} + p^{\langle \text{SVN},C \rangle} X^{\langle \text{SVN},C,A \rangle} = 0 \quad (5.152)$$

$$\pi^{\langle \text{SVN},B \rangle} + L^{\langle \text{SVN},B \rangle} + p^k K^{\langle \text{SVN},B \rangle} + p^{\langle \text{SVN},A \rangle} X^{\langle \text{SVN},A,B \rangle} + p^{\langle \text{SVN},B \rangle} X^{\langle \text{SVN},B,B \rangle} - p^{\langle \text{SVN},B \rangle} Y^{\langle \text{SVN},B \rangle} + p^{\langle \text{SVN},C \rangle} X^{\langle \text{SVN},C,B \rangle} = 0 \quad (5.153)$$

$$\pi^{\langle \text{SVN},C \rangle} + L^{\langle \text{SVN},C \rangle} + p^k K^{\langle \text{SVN},C \rangle} + p^{\langle \text{SVN},A \rangle} X^{\langle \text{SVN},A,C \rangle} + p^{\langle \text{SVN},B \rangle} X^{\langle \text{SVN},B,C \rangle} + p^{\langle \text{SVN},C \rangle} X^{\langle \text{SVN},C,C \rangle} - p^{\langle \text{SVN},C \rangle} Y^{\langle \text{SVN},C \rangle} = 0 \quad (5.154)$$

6 Calibrating equations

$$-d^{\text{data}\langle \text{AUT},B,1 \rangle} + D^{\langle \text{AUT},B,1 \rangle} = 0 \quad (6.1)$$

$$-d^{\text{data}\langle \text{AUT},B,2 \rangle} + D^{\langle \text{AUT},B,2 \rangle} = 0 \quad (6.2)$$

$$-d^{\text{data}\langle \text{AUT},B,3 \rangle} + D^{\langle \text{AUT},B,3 \rangle} = 0 \quad (6.3)$$

$$-d^{\text{data}\langle \text{AUT},C,1 \rangle} + D^{\langle \text{AUT},C,1 \rangle} = 0 \quad (6.4)$$

$$-d^{\text{data}\langle\text{AUT},\text{C},2\rangle} + D^{\langle\text{AUT},\text{C},2\rangle} = 0 \quad (6.5)$$

$$-d^{\text{data}\langle\text{AUT},\text{C},3\rangle} + D^{\langle\text{AUT},\text{C},3\rangle} = 0 \quad (6.6)$$

$$-d^{\text{data}\langle\text{DEU},\text{B},1\rangle} + D^{\langle\text{DEU},\text{B},1\rangle} = 0 \quad (6.7)$$

$$-d^{\text{data}\langle\text{DEU},\text{B},2\rangle} + D^{\langle\text{DEU},\text{B},2\rangle} = 0 \quad (6.8)$$

$$-d^{\text{data}\langle\text{DEU},\text{B},3\rangle} + D^{\langle\text{DEU},\text{B},3\rangle} = 0 \quad (6.9)$$

$$-d^{\text{data}\langle\text{DEU},\text{C},1\rangle} + D^{\langle\text{DEU},\text{C},1\rangle} = 0 \quad (6.10)$$

$$-d^{\text{data}\langle\text{DEU},\text{C},2\rangle} + D^{\langle\text{DEU},\text{C},2\rangle} = 0 \quad (6.11)$$

$$-d^{\text{data}\langle\text{DEU},\text{C},3\rangle} + D^{\langle\text{DEU},\text{C},3\rangle} = 0 \quad (6.12)$$

$$-d^{\text{data}\langle\text{SVN},\text{B},1\rangle} + D^{\langle\text{SVN},\text{B},1\rangle} = 0 \quad (6.13)$$

$$-d^{\text{data}\langle\text{SVN},\text{B},2\rangle} + D^{\langle\text{SVN},\text{B},2\rangle} = 0 \quad (6.14)$$

$$-d^{\text{data}\langle\text{SVN},\text{B},3\rangle} + D^{\langle\text{SVN},\text{B},3\rangle} = 0 \quad (6.15)$$

$$-d^{\text{data}\langle\text{SVN},\text{C},1\rangle} + D^{\langle\text{SVN},\text{C},1\rangle} = 0 \quad (6.16)$$

$$-d^{\text{data}\langle\text{SVN},\text{C},2\rangle} + D^{\langle\text{SVN},\text{C},2\rangle} = 0 \quad (6.17)$$

$$-d^{\text{data}\langle\text{SVN},\text{C},3\rangle} + D^{\langle\text{SVN},\text{C},3\rangle} = 0 \quad (6.18)$$

$$-k^{\text{data}\langle\text{AUT},\text{A}\rangle} + K^{\langle\text{AUT},\text{A}\rangle} = 0 \quad (6.19)$$

$$-k^{\text{data}\langle\text{AUT},\text{B}\rangle} + K^{\langle\text{AUT},\text{B}\rangle} = 0 \quad (6.20)$$

$$-k^{\text{data}}_{\langle \text{AUT}, \text{C} \rangle} + K^{\langle \text{AUT}, \text{C} \rangle} = 0 \quad (6.21)$$

$$-k^{\text{data}}_{\langle \text{DEU}, \text{A} \rangle} + K^{\langle \text{DEU}, \text{A} \rangle} = 0 \quad (6.22)$$

$$-k^{\text{data}}_{\langle \text{DEU}, \text{B} \rangle} + K^{\langle \text{DEU}, \text{B} \rangle} = 0 \quad (6.23)$$

$$-k^{\text{data}}_{\langle \text{DEU}, \text{C} \rangle} + K^{\langle \text{DEU}, \text{C} \rangle} = 0 \quad (6.24)$$

$$-k^{\text{data}}_{\langle \text{SVN}, \text{A} \rangle} + K^{\langle \text{SVN}, \text{A} \rangle} = 0 \quad (6.25)$$

$$-k^{\text{data}}_{\langle \text{SVN}, \text{B} \rangle} + K^{\langle \text{SVN}, \text{B} \rangle} = 0 \quad (6.26)$$

$$-k^{\text{data}}_{\langle \text{SVN}, \text{C} \rangle} + K^{\langle \text{SVN}, \text{C} \rangle} = 0 \quad (6.27)$$

$$-l^{\text{data}}_{\langle \text{AUT}, \text{A} \rangle} + L^{\langle \text{AUT}, \text{A} \rangle} = 0 \quad (6.28)$$

$$-l^{\text{data}}_{\langle \text{AUT}, \text{B} \rangle} + L^{\langle \text{AUT}, \text{B} \rangle} = 0 \quad (6.29)$$

$$-l^{\text{data}}_{\langle \text{AUT}, \text{C} \rangle} + L^{\langle \text{AUT}, \text{C} \rangle} = 0 \quad (6.30)$$

$$-l^{\text{data}}_{\langle \text{DEU}, \text{A} \rangle} + L^{\langle \text{DEU}, \text{A} \rangle} = 0 \quad (6.31)$$

$$-l^{\text{data}}_{\langle \text{DEU}, \text{B} \rangle} + L^{\langle \text{DEU}, \text{B} \rangle} = 0 \quad (6.32)$$

$$-l^{\text{data}}_{\langle \text{DEU}, \text{C} \rangle} + L^{\langle \text{DEU}, \text{C} \rangle} = 0 \quad (6.33)$$

$$-l^{\text{data}}_{\langle \text{SVN}, \text{A} \rangle} + L^{\langle \text{SVN}, \text{A} \rangle} = 0 \quad (6.34)$$

$$-l^{\text{data}}_{\langle \text{SVN}, \text{B} \rangle} + L^{\langle \text{SVN}, \text{B} \rangle} = 0 \quad (6.35)$$

$$-l^{\text{data}}_{\langle \text{SVN}, \text{C} \rangle} + L^{\langle \text{SVN}, \text{C} \rangle} = 0 \quad (6.36)$$

$$-x^{\text{data}\langle\text{AUT,A,B}\rangle} + X^{\langle\text{AUT,A,B}\rangle} = 0 \quad (6.37)$$

$$-x^{\text{data}\langle\text{AUT,A,C}\rangle} + X^{\langle\text{AUT,A,C}\rangle} = 0 \quad (6.38)$$

$$-x^{\text{data}\langle\text{AUT,B,A}\rangle} + X^{\langle\text{AUT,B,A}\rangle} = 0 \quad (6.39)$$

$$-x^{\text{data}\langle\text{AUT,B,C}\rangle} + X^{\langle\text{AUT,B,C}\rangle} = 0 \quad (6.40)$$

$$-x^{\text{data}\langle\text{AUT,C,A}\rangle} + X^{\langle\text{AUT,C,A}\rangle} = 0 \quad (6.41)$$

$$-x^{\text{data}\langle\text{AUT,C,B}\rangle} + X^{\langle\text{AUT,C,B}\rangle} = 0 \quad (6.42)$$

$$-x^{\text{data}\langle\text{DEU,A,B}\rangle} + X^{\langle\text{DEU,A,B}\rangle} = 0 \quad (6.43)$$

$$-x^{\text{data}\langle\text{DEU,A,C}\rangle} + X^{\langle\text{DEU,A,C}\rangle} = 0 \quad (6.44)$$

$$-x^{\text{data}\langle\text{DEU,B,A}\rangle} + X^{\langle\text{DEU,B,A}\rangle} = 0 \quad (6.45)$$

$$-x^{\text{data}\langle\text{DEU,B,C}\rangle} + X^{\langle\text{DEU,B,C}\rangle} = 0 \quad (6.46)$$

$$-x^{\text{data}\langle\text{DEU,C,A}\rangle} + X^{\langle\text{DEU,C,A}\rangle} = 0 \quad (6.47)$$

$$-x^{\text{data}\langle\text{DEU,C,B}\rangle} + X^{\langle\text{DEU,C,B}\rangle} = 0 \quad (6.48)$$

$$-x^{\text{data}\langle\text{SVN,A,B}\rangle} + X^{\langle\text{SVN,A,B}\rangle} = 0 \quad (6.49)$$

$$-x^{\text{data}\langle\text{SVN,A,C}\rangle} + X^{\langle\text{SVN,A,C}\rangle} = 0 \quad (6.50)$$

$$-x^{\text{data}\langle\text{SVN,B,A}\rangle} + X^{\langle\text{SVN,B,A}\rangle} = 0 \quad (6.51)$$

$$-x^{\text{data}\langle\text{SVN,B,C}\rangle} + X^{\langle\text{SVN,B,C}\rangle} = 0 \quad (6.52)$$

$$-x^{\text{data}\langle\text{SVN,C,A}\rangle} + X^{\langle\text{SVN,C,A}\rangle} = 0 \quad (6.53)$$

$$-x^{\text{data}\langle\text{SVN,C,B}\rangle} + X^{\langle\text{SVN,C,B}\rangle} = 0 \quad (6.54)$$

$$-y^{\text{data}\langle\text{AUT,A}\rangle} + Y^{\langle\text{AUT,A}\rangle} = 0 \quad (6.55)$$

$$-y^{\text{data}\langle\text{AUT,B}\rangle} + Y^{\langle\text{AUT,B}\rangle} = 0 \quad (6.56)$$

$$-y^{\text{data}\langle\text{AUT,C}\rangle} + Y^{\langle\text{AUT,C}\rangle} = 0 \quad (6.57)$$

$$-y^{\text{data}\langle\text{DEU,A}\rangle} + Y^{\langle\text{DEU,A}\rangle} = 0 \quad (6.58)$$

$$-y^{\text{data}\langle\text{DEU,B}\rangle} + Y^{\langle\text{DEU,B}\rangle} = 0 \quad (6.59)$$

$$-y^{\text{data}\langle\text{DEU,C}\rangle} + Y^{\langle\text{DEU,C}\rangle} = 0 \quad (6.60)$$

$$-y^{\text{data}\langle\text{SVN,A}\rangle} + Y^{\langle\text{SVN,A}\rangle} = 0 \quad (6.61)$$

$$-y^{\text{data}\langle\text{SVN,B}\rangle} + Y^{\langle\text{SVN,B}\rangle} = 0 \quad (6.62)$$

$$-y^{\text{data}\langle\text{SVN,C}\rangle} + Y^{\langle\text{SVN,C}\rangle} = 0 \quad (6.63)$$

$$-1 + \beta^{\text{x}\langle\text{AUT,A,A}\rangle} + \beta^{\text{x}\langle\text{AUT,B,A}\rangle} + \beta^{\text{x}\langle\text{AUT,C,A}\rangle} = 0 \quad (6.64)$$

$$-1 + \beta^{\text{x}\langle\text{AUT,A,B}\rangle} + \beta^{\text{x}\langle\text{AUT,B,B}\rangle} + \beta^{\text{x}\langle\text{AUT,C,B}\rangle} = 0 \quad (6.65)$$

$$-1 + \beta^{\text{x}\langle\text{AUT,A,C}\rangle} + \beta^{\text{x}\langle\text{AUT,B,C}\rangle} + \beta^{\text{x}\langle\text{AUT,C,C}\rangle} = 0 \quad (6.66)$$

$$-1 + \beta^{\text{x}\langle\text{DEU,A,A}\rangle} + \beta^{\text{x}\langle\text{DEU,B,A}\rangle} + \beta^{\text{x}\langle\text{DEU,C,A}\rangle} = 0 \quad (6.67)$$

$$-1 + \beta^{\text{x}\langle\text{DEU,A,B}\rangle} + \beta^{\text{x}\langle\text{DEU,B,B}\rangle} + \beta^{\text{x}\langle\text{DEU,C,B}\rangle} = 0 \quad (6.68)$$

$$-1 + \beta^{\mathbf{x}\langle \text{DEU}, \text{A}, \text{C} \rangle} + \beta^{\mathbf{x}\langle \text{DEU}, \text{B}, \text{C} \rangle} + \beta^{\mathbf{x}\langle \text{DEU}, \text{C}, \text{C} \rangle} = 0 \quad (6.69)$$

$$-1 + \beta^{\mathbf{x}\langle \text{SVN}, \text{A}, \text{A} \rangle} + \beta^{\mathbf{x}\langle \text{SVN}, \text{B}, \text{A} \rangle} + \beta^{\mathbf{x}\langle \text{SVN}, \text{C}, \text{A} \rangle} = 0 \quad (6.70)$$

$$-1 + \beta^{\mathbf{x}\langle \text{SVN}, \text{A}, \text{B} \rangle} + \beta^{\mathbf{x}\langle \text{SVN}, \text{B}, \text{B} \rangle} + \beta^{\mathbf{x}\langle \text{SVN}, \text{C}, \text{B} \rangle} = 0 \quad (6.71)$$

$$-1 + \beta^{\mathbf{x}\langle \text{SVN}, \text{A}, \text{C} \rangle} + \beta^{\mathbf{x}\langle \text{SVN}, \text{B}, \text{C} \rangle} + \beta^{\mathbf{x}\langle \text{SVN}, \text{C}, \text{C} \rangle} = 0 \quad (6.72)$$

$$-1 + \eta^{\mathbf{k}\langle \text{AUT}, \text{A} \rangle} + \eta^{\mathbf{l}\langle \text{AUT}, \text{A} \rangle} + \eta^{\mathbf{x}\langle \text{AUT}, \text{A} \rangle} = 0 \quad (6.73)$$

$$-1 + \eta^{\mathbf{k}\langle \text{AUT}, \text{B} \rangle} + \eta^{\mathbf{l}\langle \text{AUT}, \text{B} \rangle} + \eta^{\mathbf{x}\langle \text{AUT}, \text{B} \rangle} = 0 \quad (6.74)$$

$$-1 + \eta^{\mathbf{k}\langle \text{AUT}, \text{C} \rangle} + \eta^{\mathbf{l}\langle \text{AUT}, \text{C} \rangle} + \eta^{\mathbf{x}\langle \text{AUT}, \text{C} \rangle} = 0 \quad (6.75)$$

$$-1 + \eta^{\mathbf{k}\langle \text{DEU}, \text{A} \rangle} + \eta^{\mathbf{l}\langle \text{DEU}, \text{A} \rangle} + \eta^{\mathbf{x}\langle \text{DEU}, \text{A} \rangle} = 0 \quad (6.76)$$

$$-1 + \eta^{\mathbf{k}\langle \text{DEU}, \text{B} \rangle} + \eta^{\mathbf{l}\langle \text{DEU}, \text{B} \rangle} + \eta^{\mathbf{x}\langle \text{DEU}, \text{B} \rangle} = 0 \quad (6.77)$$

$$-1 + \eta^{\mathbf{k}\langle \text{DEU}, \text{C} \rangle} + \eta^{\mathbf{l}\langle \text{DEU}, \text{C} \rangle} + \eta^{\mathbf{x}\langle \text{DEU}, \text{C} \rangle} = 0 \quad (6.78)$$

$$-1 + \eta^{\mathbf{k}\langle \text{SVN}, \text{A} \rangle} + \eta^{\mathbf{l}\langle \text{SVN}, \text{A} \rangle} + \eta^{\mathbf{x}\langle \text{SVN}, \text{A} \rangle} = 0 \quad (6.79)$$

$$-1 + \eta^{\mathbf{k}\langle \text{SVN}, \text{B} \rangle} + \eta^{\mathbf{l}\langle \text{SVN}, \text{B} \rangle} + \eta^{\mathbf{x}\langle \text{SVN}, \text{B} \rangle} = 0 \quad (6.80)$$

$$-1 + \eta^{\mathbf{k}\langle \text{SVN}, \text{C} \rangle} + \eta^{\mathbf{l}\langle \text{SVN}, \text{C} \rangle} + \eta^{\mathbf{x}\langle \text{SVN}, \text{C} \rangle} = 0 \quad (6.81)$$

$$-1 + \pi^{\mathbf{h}\langle \text{AUT}, 1 \rangle} + \pi^{\mathbf{h}\langle \text{AUT}, 2 \rangle} + \pi^{\mathbf{h}\langle \text{AUT}, 3 \rangle} = 0 \quad (6.82)$$

$$-1 + \pi^{\mathbf{h}\langle \text{DEU}, 1 \rangle} + \pi^{\mathbf{h}\langle \text{DEU}, 2 \rangle} + \pi^{\mathbf{h}\langle \text{DEU}, 3 \rangle} = 0 \quad (6.83)$$

$$-1 + \pi^{\mathbf{h}\langle \text{SVN}, 1 \rangle} + \pi^{\mathbf{h}\langle \text{SVN}, 2 \rangle} + \pi^{\mathbf{h}\langle \text{SVN}, 3 \rangle} = 0 \quad (6.84)$$

$$-1 + \alpha^{\langle \text{AUT}, \text{A}, 1 \rangle}{}^\omega + \alpha^{\langle \text{AUT}, \text{B}, 1 \rangle}{}^\omega + \alpha^{\langle \text{AUT}, \text{C}, 1 \rangle}{}^\omega = 0 \quad (6.85)$$

$$-1 + \alpha^{\langle \text{AUT}, \text{A}, 2 \rangle}{}^\omega + \alpha^{\langle \text{AUT}, \text{B}, 2 \rangle}{}^\omega + \alpha^{\langle \text{AUT}, \text{C}, 2 \rangle}{}^\omega = 0 \quad (6.86)$$

$$-1 + \alpha^{\langle \text{AUT}, \text{A}, 3 \rangle}{}^\omega + \alpha^{\langle \text{AUT}, \text{B}, 3 \rangle}{}^\omega + \alpha^{\langle \text{AUT}, \text{C}, 3 \rangle}{}^\omega = 0 \quad (6.87)$$

$$-1 + \alpha^{\langle \text{DEU}, \text{A}, 1 \rangle}{}^\omega + \alpha^{\langle \text{DEU}, \text{B}, 1 \rangle}{}^\omega + \alpha^{\langle \text{DEU}, \text{C}, 1 \rangle}{}^\omega = 0 \quad (6.88)$$

$$-1 + \alpha^{\langle \text{DEU}, \text{A}, 2 \rangle}{}^\omega + \alpha^{\langle \text{DEU}, \text{B}, 2 \rangle}{}^\omega + \alpha^{\langle \text{DEU}, \text{C}, 2 \rangle}{}^\omega = 0 \quad (6.89)$$

$$-1 + \alpha^{\langle \text{DEU}, \text{A}, 3 \rangle}{}^\omega + \alpha^{\langle \text{DEU}, \text{B}, 3 \rangle}{}^\omega + \alpha^{\langle \text{DEU}, \text{C}, 3 \rangle}{}^\omega = 0 \quad (6.90)$$

$$-1 + \alpha^{\langle \text{SVN}, \text{A}, 1 \rangle}{}^\omega + \alpha^{\langle \text{SVN}, \text{B}, 1 \rangle}{}^\omega + \alpha^{\langle \text{SVN}, \text{C}, 1 \rangle}{}^\omega = 0 \quad (6.91)$$

$$-1 + \alpha^{\langle \text{SVN}, \text{A}, 2 \rangle}{}^\omega + \alpha^{\langle \text{SVN}, \text{B}, 2 \rangle}{}^\omega + \alpha^{\langle \text{SVN}, \text{C}, 2 \rangle}{}^\omega = 0 \quad (6.92)$$

$$-1 + \alpha^{\langle \text{SVN}, \text{A}, 3 \rangle}{}^\omega + \alpha^{\langle \text{SVN}, \text{B}, 3 \rangle}{}^\omega + \alpha^{\langle \text{SVN}, \text{C}, 3 \rangle}{}^\omega = 0 \quad (6.93)$$