# Package 'npExact'

# September 18, 2015

npExact-package	Nonparametric hypothesis tests	
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License GPL-2		
do not make assumption <b>Depends</b> R ( $>= 2.10.0$ ), state	ons on the underlying distributions.	
Date 2015-09-14  Description This package co	ontains several new hypothesis tests, which	
Version 0.2		
• '	ribution-free) hypothesis tests	
Type Package		

# Description

npExact provides distribution-free hypothesis tests.

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#### **Details**

Package: npExact Type: Package Version: 0.2

Date: 2013-09-26 License: GPL-2

This package contains several new hypothesis tests, which do not require that the user makes assumptions on the underlying distributions.

However, all tests except npStochin can only be applied if there are exogenously given bounds known to the user before gathering the data such that it is known by definition of the underlying process that all observations lie within these bounds.

So for instance, if the data involves percentages then the lower bound is 0 and the upper bound is 100, by definition of the data and not something (like normality) that cannot be deduced from the properties of the data.

### Author(s)

Karl Schlag, Oliver Reiter, Peter Saffert, Christian Pechhacker, Simona Jokubauskaite, Tautvilas Janusauskas

#### References

Karl Schlag, A New Method for Constructing Exact Tests without Making any Assumptions (August, 2008) Department of Economics and Business Working Paper 1109, Universitat Pompeu Fabra

#### See Also

```
http://homepage.univie.ac.at/karl.schlag/research/statistics/exacthypothesistesting8.
pdf
http://homepage.univie.ac.at/karl.schlag/research/statistics.html
```

# **Examples**

```
## npMeanPaired
## test whether pain after the surgery is less than before the surgery
data(pain)
npMeanPaired(pain$before, pain$after, lower = 0, upper = 100)

## npMeanSingle
## test whether Americans gave more than 5 dollars in a round of
## the Ultimatum game
data(bargaining)
us_offers <- bargaining$US
npMeanSingle(us_offers, mu = 5, lower = 0, upper = 10, alternative =
"greater", ignoreNA = TRUE) ## no rejection

## npMeanUnpaired
## test whether countries with french origin score lower than
## countries with no french origin</pre>
```

bargaining 3

```
data(french)
npMeanUnpaired(french[,1], french[,2], alternative = "less", ignoreNA =
TRUE)

## npStochin
data(french)
x <- french[, 1]
y <- french[, 2]
npStochinUnpaired(x, y, ignoreNA = TRUE)

## npVarianceSingle
## see if the minority share holder shores have a variance greater
## than 0.05
data(mshscores)
scores <- as.vector(as.matrix(mshscores))
npVarianceSingle(scores, lower = 0, upper = 1, v = 0.05, ignoreNA = TRUE)</pre>
```

bargaining

Amount sent in the Ultimatum Game

# **Description**

The Ultimatum game was played separately in four different countries. This data contains the offers of 30 students in Israel and 27 in the United States on a scale from 0 to 10. This dataset is taken from Roth et al. (1991).

# Usage

bargaining

#### **Format**

A data frame containing 30 observations for Israel and 27 for the US.

# References

Roth, A. E., Prasnikar, V., Okuno-Fujiwara, M., & Zamir, S. (1991). Bargaining and market behavior in Jerusalem, Ljubljana, Pittsburgh, and Tokyo: An experimental study. The American Economic Review, 1068-1095.

french

Indices of minority shareholder protection of countries with civil law with and without french origin.

# **Description**

This data contains the indices of minority shareholder protection on a scale from 0 to 1 in 51 countries with civil law, differentiating between those with (32 observations) and those without (19 observations) french origin. A higher value of the index means that country is more protected. The data set is taken from Djankov et al. (2008).

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# Usage

french

#### **Format**

A dataframe containing 32 observations of countries with french origin and 19 countries without french origin.

#### References

Djankov, S., La Porta, R., Lopez-de-Silanes, F., & Shleifer, A. (2008). The law and economics of self-dealing. Journal of financial economics, 88(3), 430-465.

mshscores	Indices of minority shareholder protection of countries with common and with civil law.

# Description

This data contains the indices of minority shareholder protection on a scale from 0 to 1 in 51 countries with civil law and 21 countries with common loaw. A higher value of the index means that country is more protected. The data set is taken from Djankov et al. (2008).

#### Usage

mshscores

#### **Format**

A dataframe containing 51 observations for civil law and 21 for common law.

#### References

Djankov, S., La Porta, R., Lopez-de-Silanes, F., & Shleifer, A. (2008). The law and economics of self-dealing. Journal of financial economics, 88(3), 430-465.

npMeanPaired	A test for the mean difference between two bounded random variables given matched pairs.
	given matched pairs.

# Description

This test requires that the user knows bounds before gathering the data such that the properties of the data generating process imply that all observations will be within these bounds. The data input consists of pairs of observations, each pair consisting of an observation of each random variable, different pairs being independently generated. No further distributional assumptions are made.

Under alternative = "greater", it is a test of the null hypothesis  $H_0: E(x_1) \leq E(x_2)$  against the alternative hypothesis  $H_1: E(x_1) > E(x_2)$ .

npMeanPaired 5

#### **Usage**

#### **Arguments**

x1, x2 the (non-empty) numerical data vectors which contain the variables to be tested.

The first values of the vectors are assumed to be the first matched pair of obser-

vations, the second values the second matched pair and so on.

lower, upper the theoretical lower and upper bounds on the data outcomes known ex-ante

before gathering the data.

alpha the type I error.

alternative a character string describing the alternative hypothesis, can take values "greater",

"less" or "two.sided".

iterations the number of iterations used, should not be changed if the exact solution should

be derived

epsilon the tolerance in terms of probability of the Monte Carlo simulations.

max.iterations the maximum number of iterations that should be carried out. This number could

be increased to achieve greater accuracy in cases where the difference between

the threshold probability and theta is small. Default: 10000

#### **Details**

This test uses the known bounds of the variables to transform the data into [0, 1]. Then a random transformation is used to turn the data into binary-valued variables. On this variables the exact McNemar Test with level pseudoalpha is performed and the result recorded. The random transformation and the test are then repeated iterations times. If the average rejection probability probrej of the iterations is at least theta, then the null hypothesis is rejected. If however probrej is too close to the threshold theta then the number of iterations is increased. The algorithm keeps increasing the number of iterations until the bound on the mistake involved by running these iterations is below epsilon. This error epsilon is incorporated into the overall level alpha in order to maintain that the test is exact.

theta (and a value mu of the difference between the two means in the set of the alternative hypothesis) is found in an optimization procedure. theta and mu are chosen as to maximize the set of data generating processes belonging to the alternative hypothesis that yield type II error probability below 0.5. Please see the cited paper below for further information.

#### Value

A list with class "nphtest" containing the following components:

method a character string indicating the name and type of the test that was performed.

data.name a character string giving the name(s) of the data.

alternative a character string describing the alternative hypothesis.

estimate the sample means of the given data.

probrej numerical estimate of the rejection probability of the randomized test, derived

by taking an average of iterations realizations of the rejection probability.

bounds the lower and upper bounds of the variables.

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null.value the specified hypothesized value of the difference of the variable means.

alpha the type I error.

theta the parameter that minimizes the type II error.

pseudoalpha theta\*alpha, this is the level used when calculating the average rejection prob-

ability during the iterations.

rejection logical indicator for whether or not the null hypothesis can be rejected.

iterations the number of iterations that were performed.

# Author(s)

Karl Schlag, Christian Pechhacker and Oliver Reiter

#### References

Schlag, Karl H. 2008, A New Method for Constructing Exact Tests without Making any Assumptions, Department of Economics and Business Working Paper 1109, Universitat Pompeu Fabra. Available at http://www.econ.upf.edu/en/research/onepaper.php?id=1109.

#### See Also

http://homepage.univie.ac.at/karl.schlag/research/statistics.html

# **Examples**

```
## test whether pain after the surgery is less than before the surgery
data(pain)
npMeanPaired(pain$before, pain$after, lower = 0, upper = 100)

## when the computer was used in the surgery
before_pc <- pain[pain$pc == 1, "before"]
after_pc <- pain[pain$pc == 1, "after"]
npMeanPaired(before_pc, after_pc, lower = 0, upper = 100)

## test whether uncertainty decreased from the first to the second round
data(uncertainty)
npMeanPaired(uncertainty$w1, uncertainty$w2, upper = 60) ## or
with(uncertainty, npMeanPaired(w1, w2, upper = 60))</pre>
```

npMeanSingle A test for the mean of a bounded random variable based on a single sample of iid observations.

# **Description**

This test requires that the user knows upper and lower bounds before gathering the data such that the properties of the data generating process imply that all observations will be within these bounds. The data input consists of a sequence of observations, each being an independent realization of the random variable. No further distributional assumptions are made.

For any  $\mu$  that lies between the two bounds, under alternative = "greater", it is a test of the null hypothesis  $H_0: E(X) \leq \mu$  against the alternative hypothesis  $H_1: E(X) > \mu$ .

npMeanSingle 7

#### **Usage**

## **Arguments**

x a (non-empty) numeric vector of data values. mu threshold value for the null hypothesis.

lower, upper the theoretical lower and upper bounds on the data outcomes known ex-ante

before gathering the data.

iterations the number of iterations used, should not be changed if the exact solution should

be derived

alpha the type I error.

alternative a character string describing the alternative hypothesis, can take values "greater",

"less" or "two.sided".

epsilon the tolerance in terms of probability of the Monte Carlo simulations.

ignoreNA if TRUE, NA values will be omitted. Default: FALSE

max.iterations the maximum number of iterations that should be carried out. This number could

be increased to achieve greater accuracy in cases where the difference between

the threshold probability and theta is small. Default: 10000

#### **Details**

Using the known bounds, the data is transformed to lie in [0, 1] using an affine transformation. Then the data is randomly transformed into a new data set that has values 0, mu and 1 using a mean preserving transformation. The exact randomized binomial test is then used to calculate the rejection probability of this under new data when level is theta\*alpha. This random transformation is repeated iterations times. If the average rejection probability is greater than theta, one can reject the null hypothesis. If however the average rejection probability is too close to theta then the iterations are continued. The values of theta and a value of mu in the alternative hypothesis is found in an optimization procedure to maximize the set of parameters in the alternative hypothesis under which the type II error probability is below 0.5. Please see the cited paper below for further information.

#### Value

A list with class "nphtest" containing the following components:

method a character string indicating the name and type of the test that was performed.

data. name a character string giving the name(s) of the data.

alternative a character string describing the alternative hypothesis.

estimate the estimated mean or difference in means depending on whether it was a one-

sample test or a two-sample test.

probrej numerical estimate of the rejection probability of the randomized test, derived

by taking an average of iterations realizations of the rejection probability.

bounds the lower and upper bounds of the variables.

null.value the specified hypothesized value of the correlation between the variables.

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alpha the type I error

theta the parameter that minimizes the type II error.

pseudoalpha theta\*alpha, this is the level used when calculating the average rejection prob-

ability during the iterations.

rejection logical indicator for whether or not the null hypothesis can be rejected.

iterations the number of iterations that were performed.

#### Author(s)

Karl Schlag, Peter Saffert and Oliver Reiter

#### References

Schlag, Karl H. 2008, A New Method for Constructing Exact Tests without Making any Assumptions, Department of Economics and Business Working Paper 1109, Universitat Pompeu Fabra. Available at http://www.econ.upf.edu/en/research/onepaper.php?id=1109.

#### See Also

```
http://homepage.univie.ac.at/karl.schlag/research/statistics.html
```

#### **Examples**

```
## test whether Americans gave more than 5 dollars in a round of
## the Ultimatum game
data(bargaining)
us_offers <- bargaining$US
npMeanSingle(us_offers, mu = 5, lower = 0, upper = 10, alternative =
"greater", ignoreNA = TRUE) ## no rejection

## test if the decrease in pain before and after the surgery is smaller
## than 50
data(pain)
pain$decrease <- with(pain, before - after)
without_pc <- pain[pain$pc == 0, "decrease"]
npMeanSingle(without_pc, mu = 50, lower = 0, upper = 100,
alternative = "less")</pre>
```

npMeanUnpaired

A test for comparing the means of two bounded random variables given two independent samples

# **Description**

This test requires that the user knows upper and lower bounds before gathering the data such that the properties of the data generating process imply that all observations will be within these bounds. The data input consists of a sequence of independent observations for each random variable, the two sequences being generated independently. No further distributional assumptions are made.

This is a test of the null hypothesis:  $H_0: E(X_1) \leq E(X_2)$  against  $H_1: E(X_1) > E(X_2)$ .

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#### **Usage**

#### **Arguments**

x1, x2 the (non-empty) numerical data vectors which contain the variables to be tested.

lower, upper the theoretical lower and upper bounds on the data outcomes known ex-ante

before gathering the data.

iterations the number of iterations used, should not be changed if the exact solution should

be derived.

alpha the type I error.

alternative a character string describing the alternative hypothesis, can take values "greater",

"less" or "two.sided".

epsilon the tolerance in terms of probability of the Monte Carlo simulations.

ignoreNA if TRUE, NA values will be omitted. Default: FALSE

max.iterations the maximum number of iterations that should be carried out. This number could

be increased to achieve greater accuracy in cases where the difference between

the threshold probability and theta is small. Default: 10000

#### **Details**

This test uses the known bounds of the variables to transform the data into [0, 1]. Then a random transformation is used to turn the data into binary-valued variables. On this variables the exact Fischer-Tocher Test with level pseudoalpha is performed and the result recorded. The random transformation and the test are then repeated iterations times. If the average rejection probability probrej of the iterations is at least theta, then the null hypothesis is rejected. If however probrej is too close to the threshold theta then the number of iterations is increased. The algorithm keeps increasing the number of iterations until the bound on the mistake involved by running these iterations is below epsilon. This error epsilon is incorporated into the overall level alpha in order to maintain that the test is exact.

theta is found in an optimization procedure. theta is chosen as to bring the type II error to 0.5. Please see the cited paper below for further information.

# Value

A list with class "nphtest" containing the following components:

method a character string indicating the name and type of the test that was performed.

data.name a character string giving the name(s) of the data.

alternative a character string describing the alternative hypothesis.

estimate the sample means of the two variables.

probrej numerical estimate of the rejection probability of the randomized test, derived

by taking an average of iterations realizations of the rejection probability.

bounds the lower and upper bounds of the variables.

null.value the specified hypothesized value of the correlation between the variables.

alpha the type I error.

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the ta the parameter that minimizes the type II error.

pseudoalpha theta\*alpha, this is the level used when calculating the average rejection prob-

ability during the iterations

rejection logical indicator for whether or not the null hypothesis can be rejected

iterations the number of iterations that were performed.

### Author(s)

Karl Schlag, Christian Pechhacker, Peter Saffert and Oliver Reiter

#### References

Karl Schlag (2008), A New Method for Constructing Exact Tests without Making any Assumptions. Available at http://www.econ.upf.edu/en/research/onepaper.php?id=1109.

#### See Also

```
http://homepage.univie.ac.at/karl.schlag/research/statistics.html
```

#### **Examples**

```
## test whether countries with french origin score lower than
## countries with no french origin
data(french)
npMeanUnpaired(french[,1], french[,2], alternative = "less", ignoreNA =
TRUE)

## test whether American tend to be more generous than Isrealis
## in a round of the Ultimatum game
data(bargaining)
npMeanUnpaired(bargaining$US, bargaining$IS, lower = 0, upper = 10, ignoreNA = TRUE)
```

npStochinUnpaired

A test of a stochastic inequality given two independent samples

# Description

The data input consists of a sequence of independent realizations observations of each random variable, observations of the different sequences also being independent.

```
Given -1 < d < 1 it is a test of the null hypothesis H_0: P(X_2 > X_1) \le P(X_2 < X_1) + d against the alternative hypothesis H_1: P(X_2 > X_1) > P(X_2 < X_1) + d.
```

# Usage

```
npStochinUnpaired(x1, x2, d = 0, alternative = "two.sided", iterations = 5000, alpha = 0.05, epsilon = 1 * 10^{-6}, ignoreNA = FALSE, max.iterations = 10^{-6}
```

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#### **Arguments**

x1, x2 the (non-empty) numerical data vectors which contain the variables to be tested. d the maximal difference in probabilities assumed  $H_0: P(X_2 > X_1) - P(X_2 <$ 

 $X_1$ )  $\leq d$ . Default is 0.

alternative a character string describing the alternative hypothesis. Default is "greater". If

"less" is given, x1 and x2 are switched for each other.

iterations the number of iterations used, should not be changed if the exact solution should

be derived.

alpha the type I error.

epsilon the tolerance in terms of probability of the Monte Carlo simulations.

ignoreNA if TRUE, NA values will be omitted. Default: FALSE

max.iterations the maximum number of iterations that should be carried out. This number could

be increased to achieve greater accuracy in cases where the difference between

the threshold probability and theta is small. Default: 10000

#### **Details**

The data is randomly matched into pairs and then treats them as matched pairs. The number of pairs is equal to the number of observations in the smaller sequence. The exact randomized test is then used to determine if sufficiently many occurrences of  $x_2 > x_1$  occur when compared to how often  $x_2 < x_1$  occurs, using level theta\*alpha. The matching into pairs is repeated iterations times. The test gives a rejection of the average rejection probability in these iterations lies above theta. If the average rejection probability lies too close to theta then the number of iterations is increased.

theta is determined to maximize the set of differences  $P(X_2 > X_1) - P(X_2 < X_1)$  belonging to the alternative hypothesis in which the type II error probability lies below 0.5. For more details see the paper.

#### Value

A list with class "nphtest" containing the following components:

method a character string indicating the name and type of the test that was performed.

data. name a character string giving the name(s) of the data.

alternative a character string describing the alternative hypothesis.

estimate an estimate of  $P(x_2 > x_1) - P(x_2 < x_1)$ .

probrej numerical estimate of the rejection probability of the randomized test, derived

by taking an average of iterations realizations of the rejection probability.

bounds the lower and upper bounds of the variables.

null.value the specified hypothesized value of the correlation between the variables.

alpha the type I error.

theta the parameter that minimizes the type II error.

pseudoalpha theta\*alpha, this is the level used when calculating the average rejection prob-

ability during the iterations.

rejection logical indicator for whether or not the null hypothesis can be rejected.

iterations the number of iterations that were performed.

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#### Author(s)

Karl Schlag, Peter Saffert and Oliver Reiter

#### References

Schlag, Karl H. 2008, A New Method for Constructing Exact Tests without Making any Assumptions, Department of Economics and Business Working Paper 1109, Universitat Pompeu Fabra. Available at http://www.econ.upf.edu/en/research/onepaper.php?id=1109.

#### See Also

```
http://homepage.univie.ac.at/karl.schlag/research/statistics.html
```

#### **Examples**

```
data(french)
x <- french[, 1]
y <- french[, 2]
npStochinUnpaired(x, y, ignoreNA = TRUE)</pre>
```

npVarianceSingle

A test for the variance of a bounded random variable based on a single sample of iid observations.

# **Description**

This test requires that the user knows upper and lower bounds before gathering the data such that the properties of the data generating process imply that all observations will be within these bounds. The data input consists of a sequence of observations, each being an independent realization of the random variable. No further distributional assumptions are made.

This is a test of the null hypothesis  $H_0: Var(X) \leq v$  against  $H_1: Var(X) > v$ .

# Usage

# **Arguments**

x a (non-empty) numeric vector of data values. v the value of the variance to be tested as  $H_0: Var(x) \leq v$ . lower, upper the theoretical lower and upper bounds on the data outcomes known ex-ante

to the description of the data of the data

before gathering the data.

alternative a character string describing the alternative hypothesis, can take values "greater",

"less" or "two.sided"

alpha the type I error.

iterations the number of iterations used, should not be changed if the exact solution should

be derived.

npVarianceSingle 13

epsilon the tolerance in terms of probability of the Monte Carlo simulations.

ignoreNA if TRUE, NA values will be omitted. Default: FALSE

max.iterations the maximum number of iterations that should be carried out. This number could

be increased to achieve greater accuracy in cases where the difference between

the threshold probability and theta is small. Default: 10000

#### **Details**

This test randomly matches the data into pairs, then computes for each pair the square of the difference and continues with the resulting sequence with half as many observations as npMeanSingle. See the cited paper for more information.

#### Value

A list with class "nphtest" containing the following components:

method a character string indicating the name and type of the test that was performed.

data. name a character string giving the name(s) of the data.

alternative a character string describing the alternative hypothesis.

estimate the estimated mean or difference in means depending on whether it was a one-

sample test or a two-sample test.

probrej numerical estimate of the rejection probability of the randomized test, derived

by taking an average of iterations realizations of the rejection probability.

bounds the lower and upper bounds of the variables.

null.value the specified hypothesized value of the correlation between the variables.

alpha the type I error.

theta the parameter that minimizes the type II error.

pseudoalpha theta\*alpha, this is the level used when calculating the average rejection prob-

ability during the iterations.

rejection logical indicator for whether or not the null hypothesis can be rejected.

iterations the number of iterations that were performed.

#### Author(s)

Karl Schlag and Oliver Reiter

#### References

Karl Schlag (2008). Exact tests for correlation and for the slope in simple linear regressions without making assumptions. Available at http://www.econ.upf.edu/en/research/onepaper.php?id=1097.

### See Also

http://homepage.univie.ac.at/karl.schlag/research/statistics.html

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#### **Examples**

```
## see if the minority share holder shores have a variance greater
## than 0.05
data(mshscores)

scores <- as.vector(as.matrix(mshscores))
npVarianceSingle(scores, lower = 0, upper = 1, v = 0.05, ignoreNA = TRUE)</pre>
```

pain

Pain experienced before and after a knie operation

#### **Description**

There are two ways to determine where to start an operation on a knee, either with a computer or manually. The data describes the pain experienced by the patients before and after the surgery.

# Usage

pain

#### **Format**

A dataframe containing 50 observations. Column "pc" indicates if a computer was used (coded with "1") or not (coded with "0")

#### References

Sabeti-Aschraf, M., Dorotka, R., Goll, A., & Trieb, K. (2005). Extracorporeal shock wave therapy in the treatment of calcific tendinitis of the rotator cuff. The American journal of sports medicine, 33(9), 1365-1368.

uncertainty

Uncertainty in a game theoretical experiment.

# **Description**

In an experiment, subjects played a similar game twice. Choices could be between 110 and 170. Each time, before they made their own choice, they had to indicate an interval  $[L,\,U]$  that they believed would contain the choice of their opponent. They paid some additional money if the choice of their opponent was in the interval they specified, and were paid more the smaller this interval was. So the width  $W_i$  of this interval in round i gives an indication of how uncertain they are in round i. The data contains the interval width in round 1 and 2 which makes this a sample of matched pairs.

### Usage

uncertainty

#### **Format**

A dataframe containing the 25 intervals in each round of the game.

uncertainty 15

# References

Galbiati, R., Schlag, K., & van der Weele, J. Sanctions that Signal: an Experiment. Journal of Economic Behavior and Organization, Forthcoming

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