

Round 3 2010

A. De-RNG-ed

B. Fence

C. Hot Dog Proliferation

#### D. Different Sum

# **Contest Analysis**

**Questions** asked

## Submissions

## De-RNG-ed

4pt Not attempted 273/325 users correct (84%)

10pt | Not attempted 179/231 users correct (77%)

#### Fence

7pt | Not attempted 250/299 users correct (84%)

22pt | Not attempted 77/177 users correct (44%)

### Hot Dog Proliferation

6pt Not attempted 217/249 users correct (87%)

22pt Not attempted 20/95 users correct (21%)

## Different Sum

7pt Not attempted 102/125 users correct (82%)

22pt Not attempted 23/47 users correct (49%)

#### Top Scores Burunduk1 100 100 winger 100 Eryx **RAVEman** 78 Gennady.Korotkevich 78 78 nika 78 eatmore pashka 78 78 Vasvl iakubr 72

## Problem D. Different Sum

This contest is open for practice. You can try every problem as many times as you like, though we won't keep track of which problems you solve. Read the Quick-Start Guide to get started.

Small input 7 points

Large input 22 points

Solve D-small

Solve D-large

### Problem

We have come up with a wonderful problem for Google Code Jam 2010 that involves contestants solving a cryptarithm. But we need your help in creating testcases for the problem; more precisely, we're concerned with addition equations that are good enough (in the sense defined below) for conversion into cryptarithms.

You don't need to know what a cryptarithm is to solve this problem, as we'll provide all required definitions. We define a cryptarithm equation to be an addition equation written in such a way that all summands (numbers being added) and the sum are aligned to the same right border like this:

124 31 25				
180				

Additionally, for each column of a cryptarithm equation, all digits of the summands in that column must be different. Note that we don't include the sum in this constraint. So for example in the above equation the first column contains only digit 1, the second column contains digits 2,3 and 2, and the third column contains digits 4, 1 and 5. This equation is not a cryptarithm equation since the second column contains two 2's. However, it would be a cryptarithm equation if we replaced the last summand with 15 (and the sum with 170).

Note that summands in a cryptarithm equation are always positive and written without leading zeros. The order of summands is not important (in other words, two equations which differ only in the order of the summands are considered the same)

The example above was in base 10, but we're also interested in cryptarithm equations in other bases. Note that a "digit" in base b could mean any integer between 0 and b-1. Here is a cryptarithm equation in base 23:

	_
I7B	
I7B JJJ	
1F47	

In this example, "I" stands for digit 18, "B" stands for digit 11, "J" stands for digit 19, and "F" stands for digit 15. In decimal notation, the two summands are  $18*23^2 + 7*23 + 11 = 9694$  and  $19*23^2 + 19*23 + 19 = 10507$ , and the sum is  $1*23^3 + 15*23^2 + 4*23 + 7 = 20201$ . Please note that denoting digits of 10 and more with letters was done purely for the clarity of the example; it doesn't really matter in this problem how exactly we denote such digits in writina.

How many cryptarithm equations are there with the given sum  $\mathbf{N}$  in the given base B?

Since the answer might be very large, please output it modulo 1000000007.

## Input

The first line of the input gives the number of test cases, T. T lines follow. Each contains two positive integers N and B. All input numbers are given in base 10.

## Output

For each test case, output one line containing "Case #x: y", where x is the case number (starting from 1) and y is the number of different cryptarithm equations with the given sum. Since this number can be very big, please output it modulo 100000007. Of course, the output itself should be in base 10.

Limits

 $1 \le \mathbf{T} \le 20$ .

Small dataset

 $1 \le \mathbf{N} \le 100.$  $2 \le \mathbf{B} \le 10.$ 

Large dataset

```
1 \le \mathbf{N} \le 10^{18}. 2 \le \mathbf{B} \le 70.
```

## Sample

## Explanation

Here are the 4 cryptarithm equations with sum 6:

```
6 1 2 1

- 5 4 2

6 - - 3

6 6 -
```

And here are the 4 cryptarithm equations in base 4 with sum  $8=20_4$ :

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