

Round 2 2011

A. Airport Walkways

B. Spinning Blade

C. Expensive Dinner

D. A.I. War

Contest Analysis

Questions asked

- Submissions

Airport Walkways

8pt Not attempted 2130/2490 users correct (86%)

Spinning Blade

8pt Not attempted 1363/1667 users correct (82%)

12pt Not attempted 516/957 users correct (54%)

Expensive Dinner

Not attempted 491/645 users correct (76%)

A.I. War

Not attempted 261/452 users correct (58%)

Not attempted 87/219 users correct (40%)

Top Scores

ilyaraz

Ahyangyi

ACRushTC	100
mystic	100
meret	100
austrin	100
msg555	100
bmerry	100
wata	100
Gennady.Korotl	kevich 100

Problem B. Spinning Blade

This contest is open for practice. You can try every problem as many times as you like, though we won't keep track of which problems you solve. Read the <u>Quick-Start Guide</u> to get started.

Small input 8 points

...+

Large input 12 points

Solve B-large

Solve B-small

Problem

Being bored with the traps in your secret hideout design, you decided to go for something classical, but always enjoyable - the *spinning blade*. You ordered a really heavy metal sheet out of which you will cut the blade; a uniform square C-by-R grid will be painted on the sheet. You have determined the best shape for the blade -- you will first cut a large square consisting of K-by-K grid cells, where $K \ge 3$. Then, you will cut out the four 1-by-1 corner cells out of the square to end up with a *blade*. After determining all this, you started waiting for the sheet to arrive.

When the sheet arrived, you were shocked to find out that the sheet had imperfections in it! You expected each cell to have mass \mathbf{D} , but it turned out that the mass can vary a bit because of differences in thickness. This is bad because you want to insert a shaft exactly in the center of the blade and spin it very fast, so the center of mass of the blade must be exactly in its center as well. The definition of the center of mass of a flat body can be found below.

Given the grid and the mass of each cell, what is the largest possible size of the blade you can make so that the center of mass is exactly in its center?

Input

The first line of the input gives the number of test cases, \mathbf{T} . \mathbf{T} test cases follow. Each one starts with a line containing 3 integers: \mathbf{R} , \mathbf{C} and \mathbf{D} — the dimensions of the grid and the mass you expected each cell to have. The next \mathbf{R} lines each contain \mathbf{C} digits $\mathbf{w_{ij}}$ each, giving the differences between the actual and the expected mass of the grid cells. Each cell has a uniform density, but could have an integer mass between $\mathbf{D} + \mathbf{0}$ and $\mathbf{D} + \mathbf{9}$, inclusive.

Output

For each test case, output one line containing "Case #x: K", where x is the case number (starting from 1) and K is the largest possible size of the blade you can cut out. If no acceptable blade of size at least 3 can be found, print "IMPOSSIBLE" instead.

Limits

 $1 \leq \mathbf{T} \leq 20$.

 $0 \le \mathbf{w_{ij}} \le 9$.

The size of the input file will not exceed 625KB.

Small dataset

 $3 \leq \mathbf{R} \leq 10.$

 $3 \le \mathbf{C} \le 10.$ $1 \le \mathbf{D} \le 100.$

100

100

Large dataset

 $3 \le \mathbf{R} \le 500$.

 $3 \le \mathbf{C} \le 500.$

 $1 \le \mathbf{D} \le 10^6.$

Sample

Input	Output
2 6 7 2 1111111 1122271 1211521 1329131 1242121 1122211 3 3 7 123 234 345	Case #1: 5 Case #2: IMPOSSIBLE

Note

The *center of mass* of a 2D object is formally defined as a point $\bf c$. If you compute the sum of $(\bf p \cdot c)$ * mass $(\bf p)$ for all points $\bf p$ in the object, you must get $\bf 0$. Here, $\bf p$, $\bf c$ and $\bf 0$ are two-dimensional vectors. This definition also works if you treat each grid cell as a "point", with all of its mass at its center.

In real life, you could place your finger under a flat object's center of mass, and balance that object on your finger. It would not fall.

To illustrate with an example, the only blade that is possible to cut out in the second sample test case, the 3x3 blade created by cutting away the corners, has its center of mass at the point (1.54, 1.46), where we assume the bottom-left corner of the sheet has coordinates (0, 0), and the coordinates grow right and up, respectively. This is verified by checking the following equality: (-1.04, 0.04) * 9 + (-0.04, 1.04) * 9 + (-0.04, 0.04) * 10 + (-0.04, -0.96) * 11 + (0.96, 0.04) * 11 = (0, 0).

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