

Qualification Round 2012

[A. Speaking in Tongues](#)[B. Dancing With the Googlers](#)[C. Recycled Numbers](#)**D. Hall of Mirrors**[Contest Analysis](#)[Questions asked](#)

Submissions

Speaking in Tongues

15pt Not attempted
17356/19464
 users correct (89%)

Dancing With the Googlers

10pt Not attempted
12384/13899
 users correct (89%)

10pt Not attempted
10762/12138
 users correct (89%)

Recycled Numbers

10pt Not attempted
11747/12327
 users correct (95%)

15pt Not attempted
6811/10604 users
 correct (64%)

Hall of Mirrors

15pt Not attempted
551/879 users
 correct (63%)

25pt Not attempted
184/259 users
 correct (71%)

Top Scores

hos.lyric	100
qnighy	100
DjinnKahn	100
levlam	100
iwiskimo	100
mystic	100
TripleM	100
aleksey	100
royf	100
krijgertje	100

Problem D. Hall of Mirrors

This contest is open for practice. You can try every problem as many times as you like, though we won't keep track of which problems you solve. Read the [Quick-Start Guide](#) to get started.

Small input
15 points

Solve D-small

Large input
25 points

Solve D-large

Problem

You live in a 2-dimensional plane, and one of your favourite places to visit is the Hall of Mirrors. The Hall of Mirrors is a room (a 2-dimensional room, of course) that is laid out in a grid. Every square on the grid contains either a square mirror, empty space, or you. You have width 0 and height 0, and you are located in the exact centre of your grid square.

Despite being very small, you can see your reflection when it is reflected back to you exactly. For example, consider the following layout, where '#' indicates a square mirror that completely fills its square, '.' indicates empty space, and the capital letter 'X' indicates you are in the center of that square:

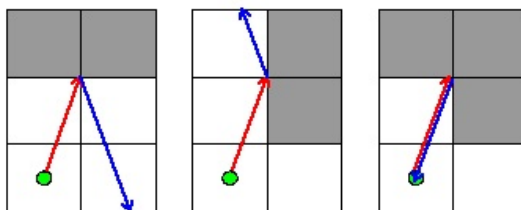
```
#####
#..X.#
#.#..#
#...##
#####
```

If you look straight up or straight to the right, you will be able to see your reflection.

Unfortunately in the Hall of Mirrors it is very foggy, so you can't see further than **D** units away. Suppose **D**=3. If you look up, your reflection will be 1 unit away (0.5 to the mirror, and 0.5 back). If you look right, your reflection will be 3 units away (1.5 to the mirror, and 1.5 back), and you will be able to see it. If you look down, your reflection will be 5 units away and you won't be able to see it.

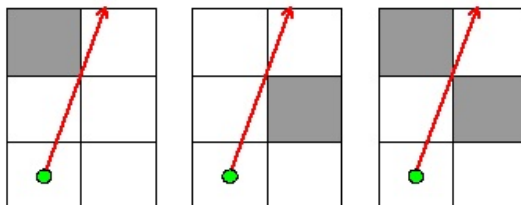
It's important to understand how light travels in the Hall of Mirrors. Light travels in a straight line until it hits a mirror. If light hits any part of a mirror but its corner, it will be reflected in the normal way: it will bounce off with an angle of reflection equal to the angle of incidence. If, on the other hand, the light would touch the corner of a mirror, the situation is more complicated. The following diagrams explain the cases:

In the following cases, light approaches a corner and is reflected, changing its direction:



In the first two cases, light approached two adjacent mirrors at the point where they met. Light was reflected in the same way as if it had hit the middle of a long mirror. In the third case, light approached the corners of three adjacent mirrors, and returned in exactly the direction it came from.

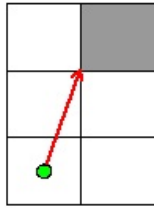
In the following cases, light approaches the corners of one or more mirrors, but does not bounce, and instead continues in the same direction:



This happens when light reaches distance 0 from the corner of a mirror, but would not have to pass through the mirror in order to continue in the same

direction. In this way, a ray of light can pass between two mirrors that are diagonally adjacent to each other -- effectively going through a space of size 0. Good thing it's of size 0 too, so it fits!

In the final case, light approaches the corner of one mirror and is destroyed:



The mirror was in the path of the light, and the ray of light didn't approach the corners of any other mirrors.

Note that light stops when it hits you, but it has to hit the exact centre of your grid square.

How many images of yourself can you see?

Input

The first line of the input gives the number of test cases, **T**. **T** test cases follow. Each test case starts with a line containing three space-separated integers, **H**, **W** and **D**. **H** lines follow, and each contains **W** characters. The characters constitute a map of the Hall of Mirrors for that test case, as described above.

Output

For each test case, output one line containing "Case #x: y", where x is the case number (starting from 1) and y is the number of reflections of yourself you can see.

Limits

$1 \leq T \leq 100$.

$3 \leq H, W \leq 30$.

$1 \leq D \leq 50$.

All characters in each map will be '#', '.', 'X', or ' '.

Exactly one character in each map will be 'X'.

The first row, the last row, the first column and the last column of each map will be entirely filled with '#' characters.

Small dataset

There will be no more than $2W+2H-4$ '#' characters.

Large dataset

The restriction from the Small dataset does not apply.

Sample

Input	Output
6	Case #1: 4
3 3 1	Case #2: 8
###	Case #3: 68
#X#	Case #4: 0
###	Case #5: 2
3 3 2	Case #6: 28
###	
#X#	
###	
4 3 8	
###	
#X#	
#.#	
###	
7 7 4	
#####	
#.....#	
#.....#	
#..X..#	
#....##	
#.....#	
#####	
5 6 3	
#####	
#..X..#	
#.#..#	
#...##	
#####	
5 6 10	
#####	

```
#.X.#  
#.#.#  
#...##  
#####
```

In the first case, light travels exactly distance 1 if you look directly up, down, left or right.

In the second case, light travels distance 1.414... if you look up-right, up-left, down-right or down-left. Since light does not travel through you, looking directly up only shows you one image of yourself.

In the fifth case, while the nearby mirror is close enough to reflect light back to you, light that hits the corner of the mirror is destroyed rather than reflected.

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