

Minimizing Page Faults on Bloom Filters

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Abstract

Bloom filters [1] are used ubiquitously due to their speed and memory efficiency in theory and in practice. However, the standard implementation of sufficiently large bloom filters suffers from page faults. In this paper we propose a bloom filter implementation that guarantees one page access per insert or query. This minimizes page faults, thereby drastically improving efficiency. We will show theoretically and empirically that our hierarchical implementation is expected to be faster than the standard implementation.

Keywords: probabilistic data structures, bloom filters, memory hierarchy, implementation, page fault analysis

1 Introduction

In this section I will describe the proposed hierarchical bloom filter implementation in detail.

Our hierarchical bloom filter will be a collection of bloom filters of the computer systems page size (4096 bytes). We will have as many bloom filters as it takes to occupy M bits. M should be $10N$ where N is the number of expected keys to be in the bloom filter. We will generate 8 independent hash functions. 1 hash function will be used to select the sub-bloom filter; the other 7 will be used to set bits in the baby bloom filter as the standard implementation.

The idea behind this is that we minimize page faults, as we only need to access one page of memory to set bits instead of up to 7.

The numbers selected will be justified in the *Theoretical Justification* section.

2 Implementations

2.1 Standard Implementation

Before we discuss the proposed solution, let us highlight the weakness of the standard implementation. The standard implementation allocates a bit vector of size m bits. Typically, this is set to be $\times 10$ the expected number of elements it will hold. The figure below represents the bit vector of length m .

Standard Bloom Filter

Bit Vector:

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 ...

Per the standard implementation, to insert an element we hash the element k times and set the corresponding bit in the vector. To query, we simply read instead of set the bit. Notice, that if m is sufficiently large, it will span across multiple pages of memory. Thus, when we read and write to the underlying bit vector, we may page fault for every bit set, slowing down our insertions or queries.

2.2 Proposed Hierarchical Implementation

Our proposal is to allocate w bit vectors of size P bits, where P is computer system's page size in bits and w is an integer such that $m = wP$. Notice, our proposed implementation uses the same amount of memory, but splits the bit vector into page size chunks.

Bit Vector 1:

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 Bit Vector 2:

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 ... Bit Vector w :

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To insert, hash the element l times mod w and insert the element per the standard bloom filter operations to the corresponding bit vector. Each bit vector (bloom filter) has k hash functions associated with it. Here l is a pre-determined parameter of the datastructure; we will discuss what the optimal setting is in a following section. To query, we simply query the corresponding bit vector instead of inserting. In essence, our proposal to create a bloom filter of bloom filters, hence the name.

Notice, for any given insertion or query, we have to perform l more hash operations than the standard implementation. This is not a concern if we select sufficiently cheap hash functions. More importantly, since each bit vector is on its own page of memory, we expect to page fault at most l times. Thus, if we minimize l without sacrificing effectiveness, we will reduce the expected number of page faults and increase the data structures efficiency.

3 Theoretical Work

4 Experiments

We will now empirically validate that the hierarchical implementation is more time efficient than the standard implementation without sacrificing accuracy. Two experiments will be conducted.

First, we will **measure elapsed time as insertions scale** of each implementation. We anticipate that the hierarchical implementation will take less time than the standard implementation for any sufficiently large value of insertions. Second, we will **measure false positives as we scale bits allocated per element** of each implementation. We anticipate that the hierarchical and standard implementation will be approximately same as the theoretical false positive rate discussed before.

For both of these sections, we pseudorandomly generate keys to both insert and query. Discussion on exactly how these keys are generated is outlined in the appendix.

4.1 Comparing Time Efficiency

For this experiment, we seek to validate that the hierarchical implementation performs better than the standard implementation as the number of insertions grow. *Hypothesis:* The hierarchical bloom filter will take less time than the standard implementation to insert n keys for any n .

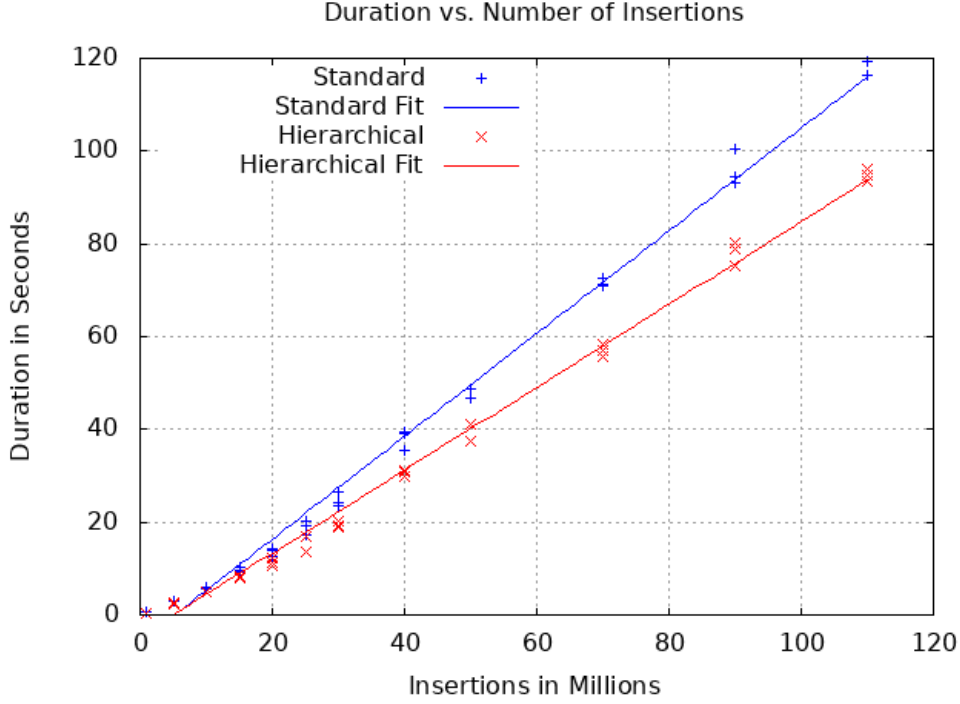
4.1.1 Experimental Settings

The experiment will run as follows. For each implementation run the following procedure:

1. Generate n random keys.
2. Generate a bloom filter of both variants of size $10n$. Use the optimal theoretical configuration for each bloom filter (i.e, $k = 7$, $l = 1$).
3. Time how long it takes to insert all n keys into each of the bloom filters. Report this number.
4. Repeat for various sizes of n .

Repeat this entire process 3 times.

4.1.2 Results



The slope of the line of best fits that are plotted are as follows where n is millions of insertions:

- The best fit line for the standard implementation is: $t = (1.1078 \pm 0.01446) \cdot n - (5.78611 \pm 0.7407)$
- The best fit line for the hierarchical implementation is: $t = (0.893221 \pm 0.01166) \cdot n - (4.52759 \pm 0.597)$

We will disregard the constant as we care about how these data structures perform as input volume scales. We can compute the efficiency difference by dividing the slopes:

Hierarchical Implementation Slope/Standard Implementation Slope = Efficiency Difference

$$(0.893221 \pm 0.01166 \text{ seconds/operation}) / (1.1078 \pm 0.01446 \text{ seconds/operation}) = 0.806301679 \approx 80\%$$

In other words, our implementation takes 80% less time per operation to complete. Thus, for any time frame, if the standard implementation performs one operation, the hierarchical implementation is expected to perform $1/80\% = 1.25$ operations. Thus, our experiment shows that the hierarchical implementation performs 25% more operations per second than the standard implementation!

4.2 Comparing False Positive Rate

For this experiment, we seek to validate that the hierarchical implementation does not have a worse false positive rate than the standard implementation. *Hypothesis:* We expect them to have approximately the same false positive rate as the theoretical expectation discussed earlier.

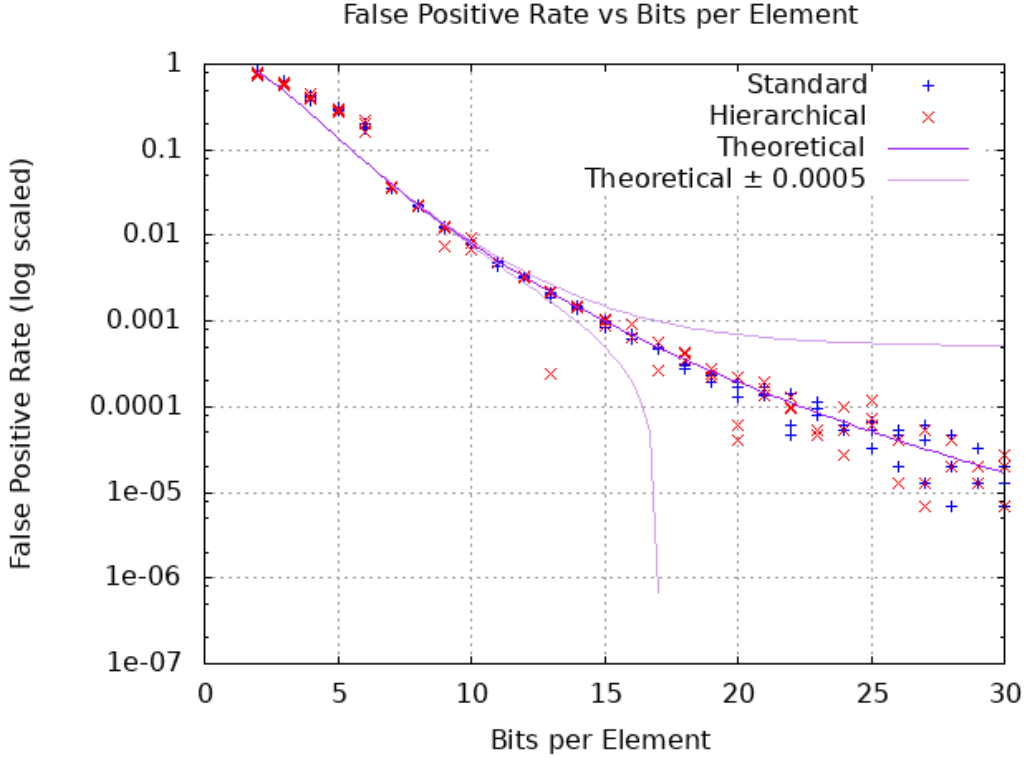
4.2.1 Experimental Settings

The experiment will run as follows.

1. Generate 150,000 random “insertion” keys (of length 16).
2. Generate 150,000 random “false” keys to query distinct from the insertion keys (of length 15).
3. For each implementation run the following procedure:
 - (a) Let BPE be the bits per element (e.g $BPE = 1$ or $BPE = 10$).
 - (b) Generate a bloom filter of size $150,000 \cdot BPE$.

- (c) Insert all the ‘insertion’ keys and query all the “false” keys and measure how many of them the bloom filter return. Report this number.
 - (d) Repeat for various values of BPE .
4. Repeat this procedure again 3 times with different insertion and false keys.

4.2.2 Results



As we can see, both the standard and hierarchical implementation closely match the theoretical expectation. Both implementations do worse than theoretically expected if bloom filters are overpacked, but after Bits per Elements is greater than 6, both implementations are very close to theoretical expectation (± 0.0005) or better.

4.3 Conclusion

Our experiments have supported both of our theoretically justified hypotheses. We have demonstrated that the hierarchical implementation is more efficient than the standard implementation; it can perform 25% more operations per second! Additionally, we have verified our that our implementation is just as effective as the standard implementation.

5 Application

6 Literature Survey

In my literature survey, I discovered a similar approach except making bloom filters hierarchial. Tim Kaler’s proposed cache-efficient bloom filters [3] makes sub-bloom filters of size cache-size; thus, their idea is very similar to mine except they do it on a smaller unit of memory.

Evgeni Krimer and Mattan Erez used a power-of-two choice principle within blocked-bloom filters to decrease the false positive rate. Instead of simply selecting one block to write into, they choose multiple. [2].

7 Conclusion

References

- [1] Burton H. Bloom. Space/time trade-offs in hash coding with allowable errors. *Communications of the ACM*, 1970.
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