
RESEARCH PROPOSAL FOR IGP(A) PROGRAM AT TOKYO INSTITUTE OF TECHNOLOGY

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ABSTRACT

This research proposal focuses on the development of state-of-the-art Quantum Computing algorithms for Machine Learning and Signal Processing. More detailed studies lie in the field of quantum machine learning algorithms, with a combination of data analysis techniques in Riemannian Manifolds. Meanwhile, the research expects to expand the application of Quantum Fourier Transform in signal processing field. The encoding in quantum computing will also be included as a supplementary study.

Keywords Quantum Signal Processing · Quantum Fourier Transform · Quantum Machine Learning · Variational Quantum Circuit · Variational Shadow Quantum Learning · Quantum Kernel Method · Quantum Block Encoding

*The citation is not precisely managed.

1 Your research topic in Japan: Describe articulately the research you wish to carry out in Japan.

Research theme: Quantum Computing Algorithms for Machine Learning and Signal Processing.

Quantum Computing was postulated in the early 1980s as way to perform computations that would not be tractable with a classical computer. Currently, at Noisy Intermediate-Scale Quantum (NISQ) era, 50 to hundreds of qubits are available for algorithm designs [1]. In 2019, Google built quantum processor, Sycamore processor, with programmable superconducting qubits to create quantum states on 53 qubits, which also experimentally demonstrated the realization of quantum supremacy [2]. So far, companies like D-wave implemented quantum computers specialized quantum annealing and Xanadu implemented Photonic Quantum Computers with 216 qubits available. Within decades of research, a universal fault-tolerant quantum computer that can solve efficiently problems such as integer factorization and unstructured database search using millions of qubits are expected to be developed [3]. Meanwhile, many quantum algorithms have already been developed with the aim at exploiting the capacity of the hardware for machine learning and signal processing application. The research I would like to carry out at Tokyo institute of Technology is the development of the quantum computing algorithms, which could exponentially increase the computational speed compared to classical algorithms. I expect the study of such quantum algorithms in machine learning and signal processing using large Hilbert space may bring various perspective in the field of Information and Communication Engineering. **Latest Update:** The IBM Quantum System Two will have a remarkable 16,632 qubits system in Late 2023 revealed. Youtube Link!

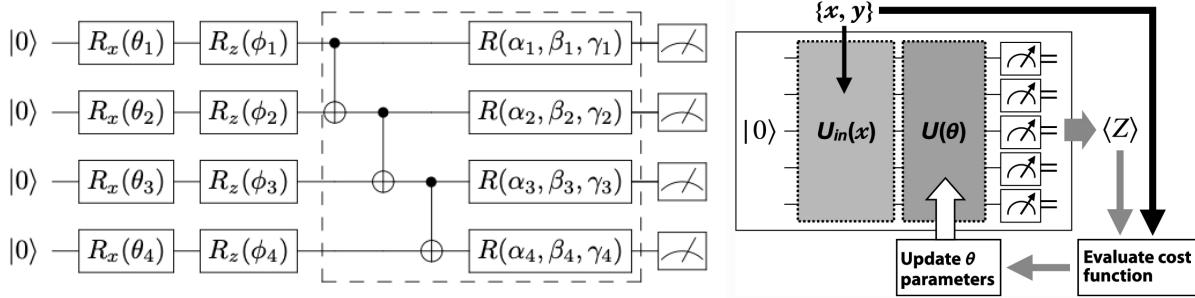
Notations Clarification:

1. Hilbert space: in quantum mechanics, the state of a physical system is represented by a vector in a *Hilbert space*: a complex vector space with an inner product.
2. *Dirac notation* is used to represent the vectors in the Hilbert space, denoted by $|v\rangle$, called ket, where v is some symbol which identifies the vector. One could equally well use something like \vec{v} or v . A multiple of a vector by a complex number c is written as $c|v\rangle \implies$ think of it as analogous to $c\vec{v}$ or cv .

3. In Dirac notation the inner product of the vectors $|v\rangle$ with $|w\rangle$ is written as $\langle v|w\rangle$. This resembles the ordinary dot product $\vec{v} \cdot \vec{w}$, thus think of $\vec{v}^* \cdot \vec{w}$.

1.1 Prior Literature and Current Development on Quantum Computing Algorithms

Quantum Machine Learning Machine learning has been used in various fields for a long time, with algorithms like BDT, CNN, GAN and etc developed for classification and image recognition task. With advancement in Quantum Computers, an interesting question is whether there are efficient quantum machine learning algorithms could approach or outperform the existing machine learning algorithms on classical computers. Recent years, the robust development of quantum computing has also brought people Variational Quantum Circuits (VQC), Quantum Kernel Methods [4] [5], Variational Shadow Quantum Learning (VSQD)[6], and Quantum Generative Adversarial Network (Quantum-GAN) [7].



The generic variational quantum circuit architecture and procedure for optimization. The inputs go through encoding, the unitary matrices, measurement, cost function evalution and then update parameters.

These new approaches solve the clustering, classification, discrimination problems with Quantum Computing Algorithm. Most of them take advantages of exponential improvement in computational speed of quantum computer and are expected to have better performance than the classical version of algorithms. The VQC shown in Figure 1 demonstrated to approximate the Deep Reinforcement Learning for decision-making and policy-selection [8].

Quantum Signal Processing The Fourier transform occurs in many different classical computing fields, especially signal processing. The decompose of wave from silicon detectors, image processing from CMOS detector, the noise filtering and more all require use of Fourier Transform. Borrowed from Qiskit's notation, the classical discrete Fourier Transforms act on vector $x = (x_0, x_1, \dots, x_n)$ and its mapping to vector $y = (y_0, y_1, \dots, y_n)$ according to formula:

$$y_k = \frac{1}{\sqrt{N}} \sum_{j=0}^{N-1} x_j \omega_N^{jk} \quad (1)$$

where $\omega_N^{jk} = e^{2\pi i \frac{jk}{N}}$. The quantum Fourier transform is the quantum implementation of the discrete Fourier transform over the amplitudes of a wavefunction. It is part of many quantum algorithms, most notably Shor's factoring algorithm [9] and quantum phase estimation [10]. Similar to discrete Fourier transform, the quantum state $|X\rangle = \sum_{j=0}^{N-1} x_j |j\rangle$ and its mapping to $|Y\rangle = \sum_{k=0}^{N-1} y_k |k\rangle$ and the map could therefore be expressed as the summation of state or multiplication of the unitary matrix:

$$|j\rangle = \frac{1}{\sqrt{N}} \sum_{k=0}^{N-1} \omega_N^{jk} |k\rangle \implies U_{QFT} = \frac{1}{\sqrt{N}} \sum_{j=0}^{N-1} \sum_{k=0}^{N-1} \omega_N^{jk} |k\rangle \langle j| \quad (2)$$

There are already well published paper and books for quantum Fourier transform [11].

1.2 Motivation for working on Quantum Machine Learning and Quantum Signal Processing

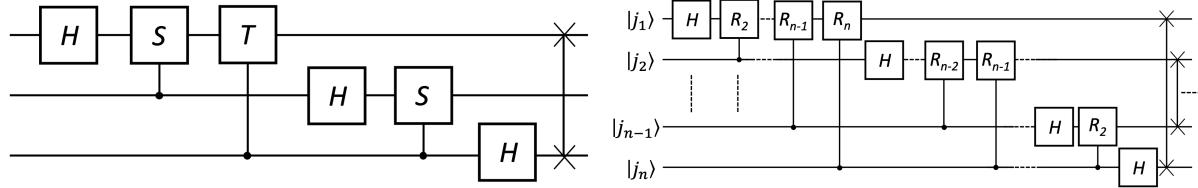
Quantum Machine Learning: Before the robust development of machine learning, people question about what to do with machine learning. Now it turns similar question to quantum machine learning. What is the advantages of quantum version of machine learning over the classical machine learning in data analysis? What is the benefit if one just "translate" the classical algorithm? If current quantum algorithms could solve some problems, is there any quantum algorithm that have better performance? In exploration of these questions, we need to study various possibilities of

QML framework with the existing approach. One interesting way for exploration is to combine quantum machine learning algorithms with Manifold Learning. For example, in Riemannian Manifold, reproducing Kernel Hilbert space(RKHS) plays important role in extracting the features. Also in quantum kernel method, RKHS is also formed for input data before processing in the quantum circuit for further learning [4]. The shared procedure provides idea to improve the existing algorithms using Riemannian Manifold and combine it to quantum kernel method, either deriving the completely new algorithm for clustering and feature extraction or improving the existing clustering algorithms using Manifold, which would be quite interesting work to explore [12] [13].

Quantum Signal Processing: Moreover, with quantum Fourier transform, could we benefit from formation of Hilbert space in quantum computer and bring it to signal processing field and more? Could we actually prove the universal advantages of quantum computing algorithms over the classical algorithms in signal processing as Shor's algorithm? These questions lead us to the discussion below:

1. **QFT ready Original Signal State** One important question is: *Can we use the quantum Fourier transform to speed up the computation of the Fast Fourier Transform or Discrete Fourier Transform?* In Issac Chuang's book, he considered the amplitude in a quantum computer cannot be directly accessed by measurement. Moreover, Chuang thinks there is no way of determining the Fourier transformed amplitudes of the original states. However, in image processing field, different Quantum Image Representation were proposed and some quantum analog representation of classical images is demonstrated. Such progress in recent year motivates me to rethink about the possible application of QFT in signal processing.

2. **Efficiency Improvement** The Shor's algorithm is a quantum computer algorithm for finding the prime factors of



The quantum Fourier Transform Circuit for 3 qubits only and n different qubits

an integer. Shor's algorithm runs polynomial time and allows us to find prime decomposition of very big numbers in $O((\log N)^3)$. One of the important factors such algorithm is so efficient is due to the efficiency of quantum Fourier transform. The discrete Fourier transform on 2^n amplitudes can be implemented as quantum circuit consisting of only $O(n^2)$ Hadamard gates and controlled phase shift gates using n qubits. Compared with discrete Fourier transform, which takes $O(n2^n)$ bits in classical computer. Such exponentially improvement efficiency using quantum Fourier transform, motivates me to think how to apply this to imaging processing, noise filtering and more. With more detailed study on classical algorithms in signal processing, the exploration of quantum Fourier transforms and formation of quantum signal processing framework based on this idea would be really interesting.

Conclusion: In general the content above is strongly correlated with background of the research I would like to carry out in Japan. The detailed research method and ultimate goals will be included in the next question.

2 Study program in Japan: (Describe in detail and with specifics - particularly concerning the ultimate goal(s) of your research in Japan)

2.1 Research Objectives

The ultimate target is to develop breakthrough algorithms in quantum machine learning and quantum signal processing. Especially in quantum machine learning, finding the one outperforms current classical machine learning algorithms in a specific task would be one of the ultimate goals for researchers in this field. Quite commonly observed, the quantum algorithms have better performance than the classical algorithms when data sample is low [3] [6]. When the dataset is large, classical algorithm has better performance in accuracy than the current quantum algorithms. In quantum signal processing part, I wish to develop algorithms using quantum Fourier transform to complete tasks considered not possible in the past. Therefore, the objectives below come to the table:

A Quantum Machine Learning: Quantum Manifold Learning Algorithms

B Quantum Signal Processing: Quantum Fourier Convolutional Neural Network

A. The existing Kernel or Reproducing Kernel Hilbert space in the Riemann Manifold Method will be enhanced or improved models for data analysis using Quantum Kernel Method. Combination of these two algorithms could possibly solve the clustering problems in Riemannian Manifold and improve the time and space exponentially.

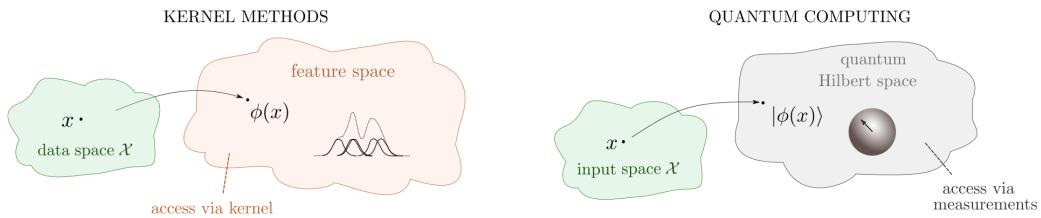
B. In imaging analysis, Fourier transform is definitely an unavoidable technique. Some algorithms analyze the data in Fourier Space and transform them back to real space to extract the features [14]. In analog signal processing, we could not apply the quantum Fourier transform. However, similar to the phase estimation algorithms. We could try to set neural network as "phase" to use QFT and inverse QFT for estimation the parameters. Later, several goals for working on Quantum Fourier Transform and its application in Quantum Convolutional Neural Network listed below[15]:

1. Forming algorithms could possibly enhance the classical discrete Fourier transform. Such replacement may improve classical algorithms to achieve better performance in feature extraction, like noise filtering, image processing and etc.
2. By the theory of Big-O, the quantum Fourier transform is exponentially faster than classical discrete Fourier transform. Verification the efficiency improvement adding Quantum Fourier Transform to existing quantum algorithms would also be a nice work to get started.

2.2 Research Method

With motivation in last section, the method to achieve research objectives will be explained in more details.

Quantum Kernel Method Among all the Quantum Machine learning algorithms, Quantum Kernel Method plays an important role for classification problem using large dimension of quantum Hilbert space. Traditionally, kernel methods for machine learning are ubiquitous for pattern recognition, with support vector machines (SVMs) being the most well-known method for classification problems [16]. In kernel methods, the access to the feature space is facilitated through kernels or inner products of feature vectors. In quantum computing, access to the Hilbert space of quantum states is given by measurements, which can also be expressed by inner products of quantum states. [5] There are



Overview of the link between quantum models and kernel methods.

limitations to the successful solution to such problems when the feature space becomes large, and the kernel functions become computationally expensive to estimate. Then, people start to think of computational speed-ups afforded by quantum algorithms. The exploitation of an exponentially large quantum state space through controllable entanglement and interference could resolve current limitations.

Clustering Problems in Riemannian Manifolds Currently in Machine Learning and Signal Processing field, people study the learning from data/features which Numerous well-known features in signal processing and machine learning belong to Riemannian manifolds, like correlation matrices, orthogonal matrices, fixed rank linear subspaces and etc [17]. Many learning tasks could be studied with forming feature space and Riemannian Manifold. The state clustering, connectivity among network nodes that stays fixed over a time interval. The community detection, subgroup detection of nodes within a single state/layer. Subnetwork-sequence clustering, sequence of subgroups of nodes with changing state. The algorithms study benefits understanding of the brain networks and its relation with Alzheimer disease, autism, depression and more [17].

Quantum Machine Learning: Quantum Manifold Learning Algorithm In practice, the feature space's demensionality sometimes can be extremely large. While not tackling these feature vectors directly, we implicitly analyze the feature vectors by only accessing their inner products in the feature space, which gives the classical kernel functions $K(\cdot)$. With SVM, a given dataset $T = \{(x_1, y_1), \dots, (x_m, y_m)\}$ in Z_2 , and a hyperplane (w, b) , a SVM can assign labels through signs of the decision function, y_{pred} :

$$K(x_i, x_j) = \phi(x_j)^T \phi(x_i) , \quad y_{\text{pred}} = \text{sign}(\langle w, x \rangle + b) \quad (3)$$

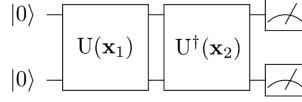
Also, separation by mapping them into a feature space is another solution, where $y_{\text{pred}} = \text{sign}(\langle w', \phi(x) \rangle + b')$ and $w' = \sum_i \alpha_i \phi(x_i)$. with Lagrangian multipliers α_i . Then, under constraints $\alpha_i \leq 0$ and $\sum_i y_i \alpha_i = 0$, we can compute the optimal α_i^* , thus the optimal hyperplane by maximizing: $\sum_i \alpha_i - \frac{1}{2} \sum_{i,j} \alpha_i \alpha_j y_i y_j \phi(x_j)^T \phi(x_i)$ Then, we only need the inner product of feature vectors $\phi(x_j)^T \phi(x_i) = K(x_i, x_j)$, which is the above mentioned kernel function. With such idea, y_{pred} is:

$$y_{\text{pred}} = \text{sign}\left(\sum_i \alpha_i^* K(x, x') + b'\right) \quad (4)$$

With the idea of classical methods, the essentials of quantum kernel methods are the same, if we map a classical data vector x into quantum state $|\phi(x)\rangle$ by encoding circuit $U(x)$ and the quantum kernel function is the inner products of two quantum feature vectors in the Hilbert space:

$$U(x) |0^N\rangle = |\phi(x)\rangle \implies K_{ij}^Q = |\langle \phi(x_j) | \phi(x_i) \rangle|^2 = |\langle 0^{\otimes N} | U^\dagger(x_j) U(x_i) | 0^{\otimes N} \rangle|^2 \quad (5)$$

This kind of kernel manipulation could then feed into the common VQC learning method mentioned previously. and then go through the training as the circuit below. Then, the idea for combination of the Quantum Kernel Method in



Simple two qubits demo for quantum circuit in kernel method

RKHS with the Fast Sequential Clustering in Riemannian Manifolds will be illustrated.

Combine with Algorithms on Manifold In paper Fast Sequential Clustering in Riemannian manifolds for Dynamic and Time-series-Annotated Multilayer Networks [17], this work focus on building a sequential-clustering framework able to address a wide variety of clustering tasks in dynamic multilayer (brain) networks via the information extracted from their nodal time-series. I consider two essential algorithms are here:

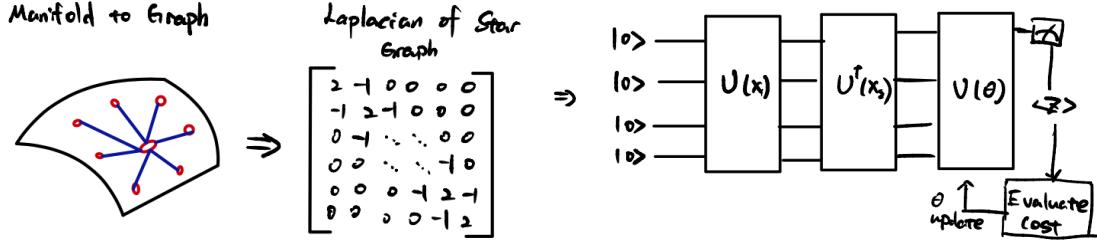
1. feature extraction from time-series
2. Riemannian Manifolds

This work claims that the rich geometry of (not necessarily embedded in Euclidean spaces) Riemannian manifolds allows latent feature patterns to unfold to the benefit of all of the aforementioned network-clustering tasks [17]. Based on the idea we introduce here, it shows new possibilities to work on Manifold Learning and Analysis. In usual Manifold Learning theory or Manifold Regularization problem, one's observed data lie on a low-dimensional manifold embedded in a higher-dimensional space [18]. We could possible define the new algorithm based on this feature:

1. Define the manifold, submanifold and their dimensions
2. Construct Graphs based on the manifold [19].
3. Calculate the Laplacian of the data graph and form appropriate Kernel function in VQC.

4. Optimized the regularized objective function (Loss function)

We could try to bring the low dimensional data to higher dimension then form graph and process through the quantum computer. Based on processing result through quantum kernel method, the features could be well discovered through time interval or more. Quantum kernel method could operates together on data and features and carries through all of the network clustering tasks on manifolds. For technical details like dimension conversion and Laplacian of a graph, demos are shown in the Figure 5. The Quantum Manifold Learning here is suppose to work in field of semi-supervised learning.



Simple flow diagram for demonstrating the algorithm I am trying to form. The kernel formed in the circuit could be heat kernel, Gaussian Kernel, SVM based on needs and experiment effect [18]. The graph converted from the Manifold could be converted to the quantum state [20].

Quantum Signal Processing: Quantum Fourier Transform and Image Processing

The structure for the development of Quantum Signal Processing starts from measurement. The wave break down by using Fourier transform's quantum analog part, Quantum Fourier Transform (QFT). The Quantum Fourier transform could particularly decompose into a product of simpler unitary matrices. With Simple decomposition, the discrete Fourier transform on 2^n amplitudes can be implemented as a quantum circuit consisting of $O(n^2)$ Hadamard gates and controlled phase shift gates.

Image Processing: The quantum-analog representation of classical images, the pixel value of i^{th} row and the j^{th} column can be stored as: $|pixel_{i,j}\rangle = \cos\left(\frac{\theta_{i,j}}{2}\right)|0\rangle + \sin\left(\frac{\theta_{i,j}}{2}\right)|1\rangle$ as formed in **Qubit Lattice** model. Other image representations like **Flexible Representation of Quantum Images** (FRQI) exists:

$$|I(\theta)\rangle = \frac{1}{2^n} \sum_{i=0}^{2^n-1} (\sin(\theta_i)|0\rangle + \cos(\theta_i)|1\rangle)|i\rangle \quad (6)$$

it actually maps each pixel's grayscale value to the amplitude as well as captures the corresponding positions in an image and integrate them into a quantum state. Where θ encodes pixel value of the corresponding position $|i\rangle$. The FRQI representation maintains a normalized state and the representation space decreases exponentially compared to the classical image due to the quantum states' superposition effect. Moreover, image representation like **Novel Enhanced Quantum Representation** (NEQR) exists:

$$|I\rangle = \frac{1}{2^n} \sum_{y=0}^{2^{2n}-1} \sum_{x=0}^{2^{2n}-1} |f(y, x)\rangle |yx\rangle \quad (7)$$

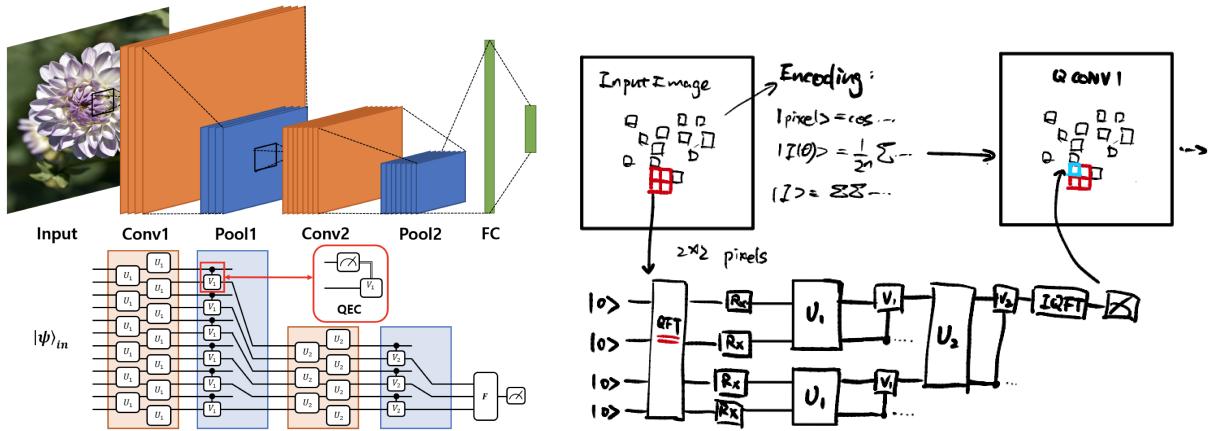
Such method uses the basis state of a qubit sequence to store the grayscale value of every pixel instead of probability amplitude encoded in a qubit in FRQI. These representations for images provide possible application on quantum Fourier transform. There are already some study using quantum kernel method to work on classification. If properly organized, edge detection, filtering and more could be realized in thoroughly different method from today. The data for testing the new algorithm could use public dataset like **MNIST** dataset or **CIFAR-10** dataset. If the overall new algorithm works with exceptional performance, the dataset with fMRI could be used.

More importantly, the Quntum Convolutional Neural Network (QCNN) exists for classification and image processing [21]. Parameterized QCNN was benchmarked for classical data classification with high accuracy and the best case being about 99% for MNIST and about 94% for Fashion MNIST [22] [23]. With combination of QCNN, quantum Fourier Transform, and Quantum Representation of Images. Setup of Quantum Fourier Convolutional Neural Network (Q-FCNN) is possible. The big picture for such algorithm is:

1. Classical Image Data Encoding to Quantum Image Representation

- (a) build up kernels for images then convert each kernel to Quantum Representation
 - (b) Directly take input images to Quantum Representation
2. Using Quantum Fourier Transform take Image Representations to Fourier Space
 3. MERA QCNN take QFT transferred data [24] [25]
 4. Inverse Quantum Fourier Transform

Here is just one possibility for new quantum algorithm in field of signal processing. Other simpler models using previously mentioned VQC is also an option.



The overall illustration for QCNN and Quantum Fourier CNN. [18]

2.3 Tentative Plan/Timetable

The first two years are filled with more details and later three years would be planned at later stage.

Year	Content	Outcome
2023 - 2024	Signal Processing and Differential Geometry Theory Courses Seminars on Quantum Machine Learning Simple Research on Application Oriented Studies	Learn basics work with Labmates Local Conference Talks
2024 - 2025	Algebraic Geometry and Quantum Computing Theory Courses Seminars on Quantum Manifold Learning Summarize First two years of study	Learn basics work with Labmates Journal/Conf Publication Master Thesis
2025 - 2026	Research on Quantum Signal Processing	Journal/Conf Publication
2026 - 2027	Research on QSP and Related Encoding Theory	Journal/Conf Publication
2027 - 2028	Research on Quantum Image Processing Summarize Five years of study	International Conference Talks PhD Thesis and Graduation

Research Originality: Quantum computing and quantum information science became a hot topics in recent years. [3] Once there is breakthrough on Noise intermediate Scale quantum era NISQ. All the research could take the data analysis, machine learning, signal processing to next level. Currently, due to availability of quantum computer, most of the algorithms research could be performed on super computer and the algorithms above could be developed through self defined python packages. Moreover, as Tokyo Institute of Technology has quite strong bond with IBM and development of quantum computer, I expect the new methods I provide would not only run on the emulators on super computer, but also on latest real quantum computers.

Furthermore, with connection globally, not only using the fMRI data in brain locally at Tokyo Institute of Technology, collaboration with people from international institute like MIT, University of Chicago, University of Hong Kong, CERN, KEK and more are all possible. The clustering algorithms anti-kt is already the default on clustering analysis for jets in colliders and there are so many possibilities my research could create a new methodology for all types of study in natural science and broader human society.

3 Present Field of Study

The pixel hit information plays vital rule for the charge particle track reconstructions, especially for flavor tagging such as c-, b-quark jets or hadronic tau identifications, where they form as a colimated spray of the charged particles. The track reconstruction software has been developed to identify such particles in the dense environment of the very narrow space using the neural network technique. Meanwhile, the pixel detector has been experienced significant radiation damage that degrades the performance. The pixel hits will be lost at most 50% of efficiency in b-layer in the end of RUN3, in turn lost the performance for the cluster classification to split or merge the associated cluster in the dense track reconstruction. The evaluation of the radiation damage of the pixel detector and modeling of the pixel cluster classification in the simulation is thus critical to improve the systematic uncertainties through RUN3. The task devotes to monitor the pixel cluster classification performance using the $Z \rightarrow \tau\tau$ events. The hadronic tau with 3-prong decay mode is a clean source for the dense tracking. The task first constructs clean dataset of the $Z \rightarrow \tau\tau$ with 3-prong final state, then the pixel clustering is compared with the simulation in a various view in term of the radiation damage. The produced dataset would be useful for many area for the tracking aspect as further optimization of the neural network training [26].

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Summary of the Thesis

Large Hadron Collider (LHC) and A Toroidal LHC Apparatus (ATLAS) experiment are built on understanding Standard Model and exploring the new phenomena in the field of High Energy Physics. A significant upgrade of the Large Hadron Collider at CERN to High Luminosity Large Hadron Collider (HL-LHC) is planned to occur before 2030. One upgrade occurs in the ATLAS experiment's pixel detector region. The current inner detector will be entirely replaced by the newer Inner Tracking Detector, with advanced Complementary Metal-oxide Semiconductor (CMOS) 65 nm technology and state-of-art Application Specific Integrated Circuits (ASIC).

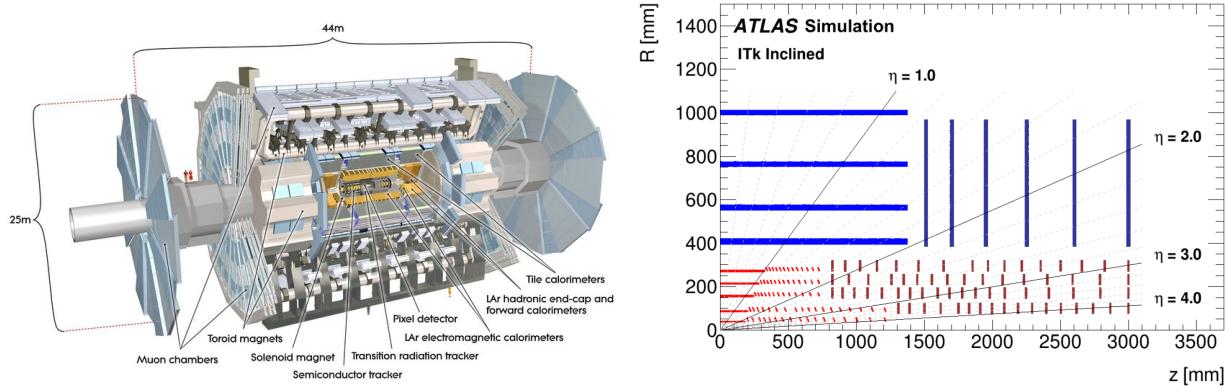


Figure a. Left: overview of the ATLAS detector; Right: Schematic of the inner tracking detector and each red dot represent a small detector module piece, which also shown in later figure.

In the upgrade, the size of each pixel inside is five times smaller. With a smaller pixel size, the readout speed needed to be ten times faster. Also, the radiation damage per year increases, which requires better radiation resistance compared to the old detector. To achieve the above goals, quality control of each module during production is necessary. **My thesis focuses on establishing and evaluating the Quality control sequence of a single piece of silicon detector.** The research could facilitate the production process, especially the electrical test, in accuracy and rapidity aspects. The time is also estimated for the 2200 modules production requirement in Japan. By the end of 2025, the 2200 module production is expected to be finished within 220 days or less.

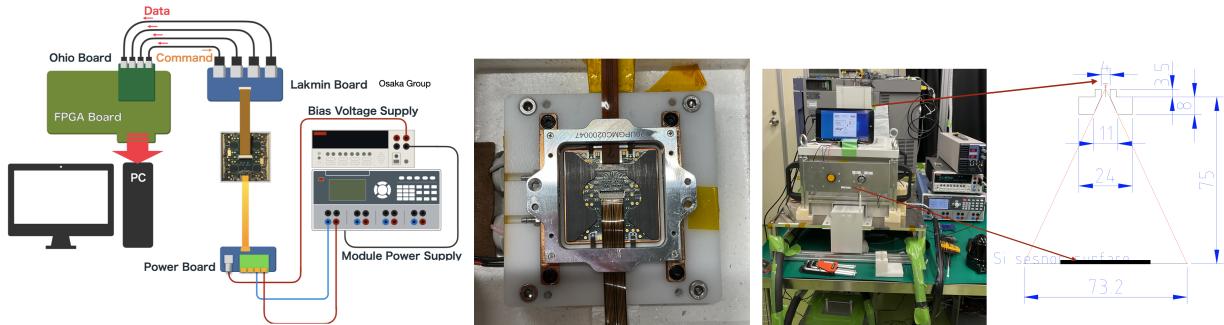


Figure b. From left to right: Overview of the DAQ system, which composed of the power supply, data readout adaptor; $4 \times 4 \text{ cm}^2$ module installed inside the cooling system; display of Xray under working condition; dimension of the Xray in milimeters

Specifically, the research work set up the test environment for testing the functionality of the semiconductor detector module. First, with existing hardware like Ohio board, Osaka board, and FPGA, the output analog signal is converted to a digital signal. Such signal is processed with supplementary digital signal loss. After processing the digital signal from each pixel on the detector, the whole map will be generated for analysis. Based on the readout system, a digital map and an analog map are created to guarantee the function of each chip in the semiconductor detector module. Moreover, radiation and bump disconnection inside the semiconductor device were analyzed with generated map. The radiation region is calculated with an external X-ray setup outside the cooling and readout system, excluding the board's resistor

component. Then for comparison and verification, the amount of radiation is calculated through emulation of the readout system using GEANT4 software.

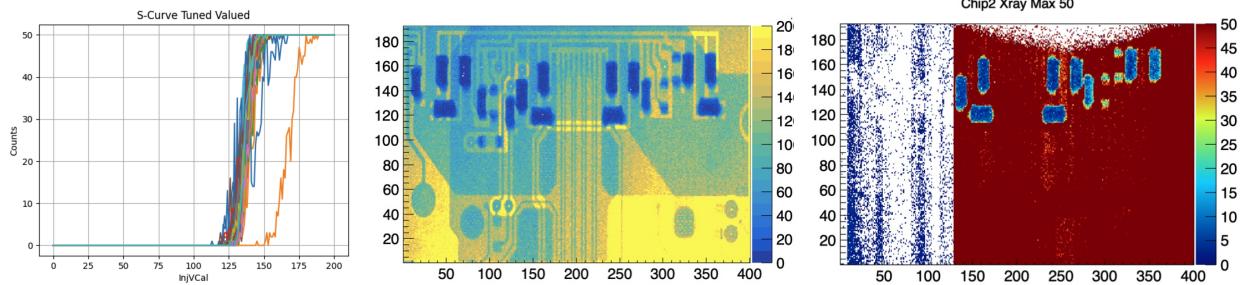


Figure c. Analysis of data from the semiconductor detector. From left to right: the threshold and signal analysis on each pixel on semiconductor detector; The result X-ray scan detecting photons hitting the detector; the bump disconnection scan for detecting the failed pixel regions.

In the complete thesis, the working principle of semiconductors is described, and the Data Acquisition System is explained in detail. The testing procedure for each module is also illustrated in detail, focusing on the electrical test. With the enhancement of the system and testing procedure, we expect better improvement in the future quality control sequence for the entire ATLAS Japan community.

Back Up

Some notes and materials to help people understand the basics. Hope this section could explain bit more on how we construct a Variational Quantum Circuit and how to use or understand each gate, and the position of my research.

Quantum Gates, Quantum Circuit, and Quantum Computation

Classical computer consists of wires and logic gates. Similarly, the quantum computer takes quantum version and logic gates and act on each qubit. The most famous Pauli Matrices, X are used as NOT gates:

$$X = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, Y = \begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}, Z = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \quad (8)$$

Z gate flips the sign of $|1\rangle$ to give $-|1\rangle$ and Hadamard gate,

$$H = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}, S = \begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix}, T = \begin{bmatrix} 1 & 0 \\ 0 & \exp(i\pi/4) \end{bmatrix} \quad (9)$$

Hadamard gate turns $|0\rangle$ into $(|0\rangle + |1\rangle)/\sqrt{2}$, and $|1\rangle$ into $(|0\rangle - |1\rangle)/\sqrt{2}$, phase gate S and $\pi/8$ gate T have some algebraic relation with H that $H = (X + Z)/\sqrt{2}$ and $S = T^2$. For rotation matrix around X, Y, Z, rotates around x, y, z axes, they are defined by equation:

$$R_\eta(\theta) = e^{-i\theta\eta/2} = \cos \frac{\theta}{2} I - i \sin \frac{\theta}{2} \eta, \quad \eta \in \{X, Y, Z\}$$

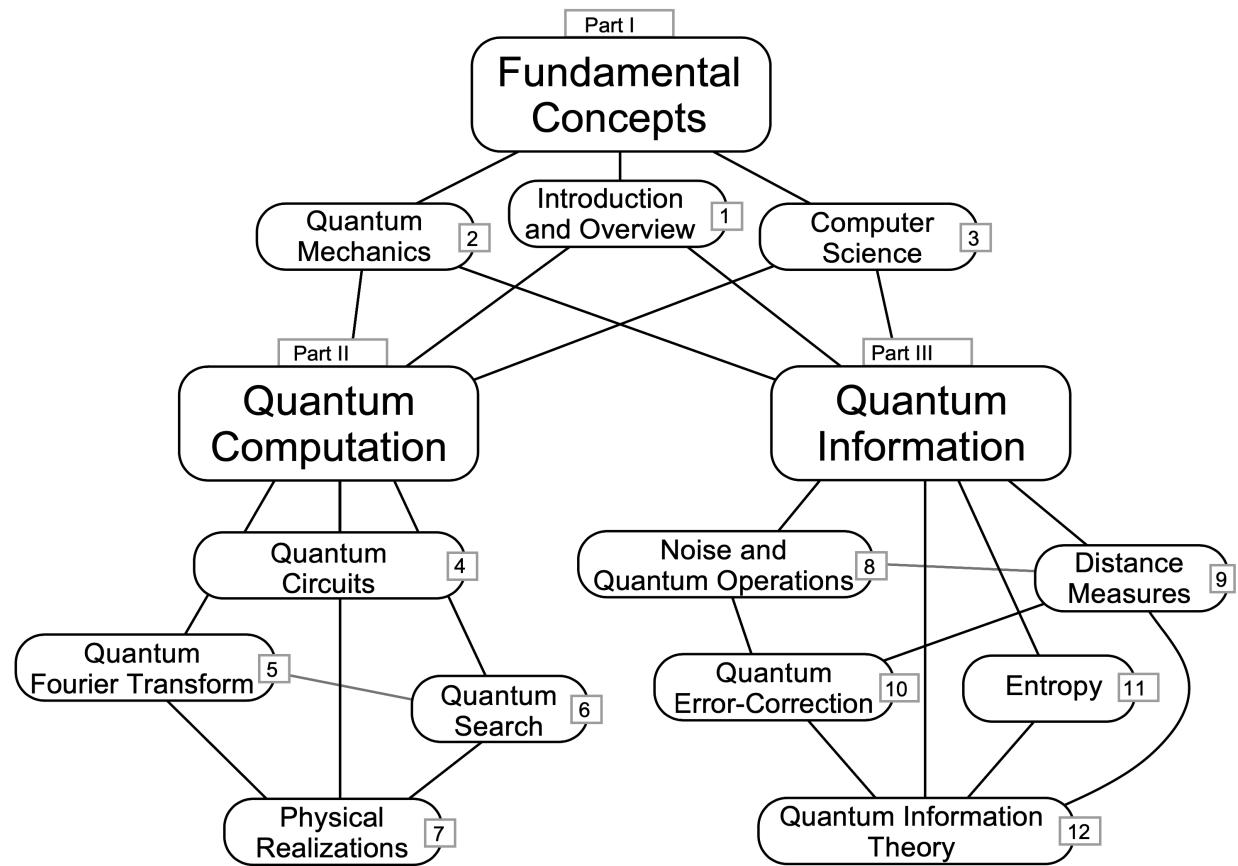
Some important theorem like Z-Y decomposition for a single qubit exists. Suppose U is a unitary operation on a single qubit. Then there exist real numbers $\alpha, \beta, \gamma, \delta$ such that

$$U = e^{i\alpha} R_z(\beta) R_y(\gamma) R_z(\delta) \quad (10)$$

Controlled Operations

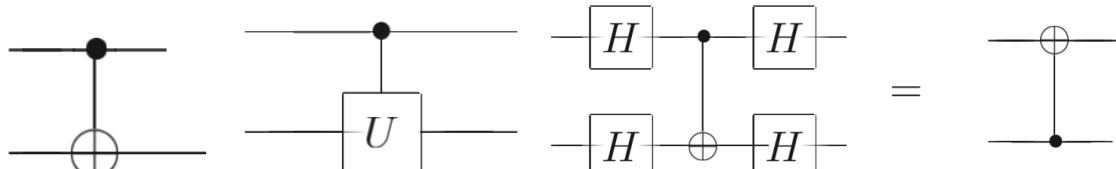
Here are some controlled operations with CNOT gate. The core idea for controlled operation is "If A is true, then do B". On single qubit, in terms of the computational basis, the action of the CNOT is given by $|c\rangle |t\rangle \rightarrow |c\rangle |t\rangle \oplus |c\rangle$, which means that the control qubit is set to $|1\rangle$ then the target qubit is flipped, otherwise the target qubit is left alone. Thus, in the computational basis $|control, target\rangle$ the matrix representation of CNOT is:

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \quad (11)$$



A big picture for the quantum computation and quantum information field in Issac Chuang's book. The proposal here focuses more on quantum circuits and quantum fourier transform study.

which could also replace by *controlled-U* operation.



Some circuit representation of control operation

Encoding Classical Data into Quantum States

Quantum Encoding is a process to transform classical information into quantum states. In order to use quantum algorithms to solve classical problems, such encoding is unavoidable. The simple concept is quantum circuit acts on $|0^n\rangle$ state, where n is the number of qubits. Based on different requirements, the style of requirement is different. The first three are most basic ones and the last two require more depth.

Basis Encoding

Conceptually the simplest one, encodes an n-bit binary string to an n-qubit quantum state $|x\rangle = |i_x\rangle$, where $|i_x\rangle$ is a computational basis state. Concrete example: $x = 1011$ maps to $|1011\rangle$

Amplitude Encoding

Vector x of length N into amplitudes of an n -qubit quantum state with $n = \lceil \log_2(N) \rceil$ and $|x\rangle = \sum_i x_i |i\rangle$ and $|i\rangle$ is the computational basis for the Hilbert space. Since the classical information forms the amplitudes of a

quantum state, the input needs to satisfy the normalization condition. For instance, $x1 = \begin{bmatrix} 1/2 \\ 1/2 \\ -1/2 \\ -1/2 \end{bmatrix}$, the quantum

state will be written as: $|x1\rangle = \frac{1}{2}|00\rangle + \frac{1}{2}|01\rangle - \frac{1}{2}|10\rangle - \frac{1}{2}|11\rangle$ similarly, for $x2 = \begin{bmatrix} 1/\sqrt{3} \\ 1/\sqrt{3} \\ -1/\sqrt{3} \end{bmatrix}$ the state would be:

$$|x2\rangle = \frac{1}{\sqrt{3}}|00\rangle + \frac{1}{\sqrt{3}}|01\rangle - \frac{1}{\sqrt{3}}|10\rangle$$

Angle Encoding

Angle encoding uses rotation gates to encode the classical information x . The classical information determines angles of rotation gates:

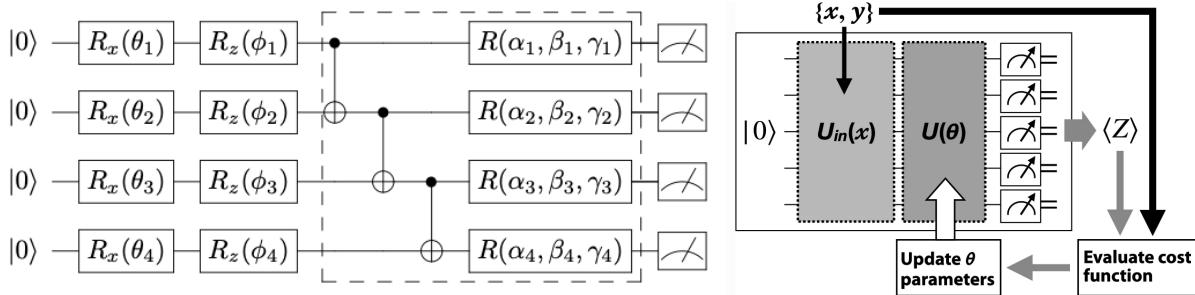
$$|x\rangle = \bigotimes_i^n R(x_i) |0^n\rangle \quad (12)$$

R can be one of the rotation gate R_x , R_y , and R_z . Usually, the number of qubits used for encoding is equal to the dimension of vector. For example, if $x = \begin{bmatrix} \pi \\ \pi \\ \pi \end{bmatrix}$, angle encoding rotates every qubit around Y-axis (if we choose R_y) for degree π , the corresponding quantum state is then $|x\rangle = Ry(\pi)|0\rangle Ry(\pi)|0\rangle Ry(\pi)|0\rangle$, which indicates the result is $|111\rangle$.

IQP Style Encoding

Hamiltonian Evolution Ansatz Encoding

Quantum Classifier



The generic variational quantum circuit architecture and procedure for optimization. The inputs go through encoding, the unitary matrices, measurement, lost function evalution and then update parameters.

The lost function could be the simplest one:

$$L(\theta) = \sum_{k=1}^N \frac{1}{N} |\tilde{y}^k - y^k|^2 \quad (13)$$

Quantum Fourier Transform Phase Estimation

Suppose a unitary operator U has an eigenvalue $|u\rangle$ with eigenvalue $e^{2\pi i \varphi}$, where the value of φ is unknown. The goal of the phase estimation algorithm is to estimate φ .

Inputs: (1) A black box which performs a controlled- U^j operation, for integer j . (2) an eigenstate $|u\rangle$ of U with

eigenvalue $e^{2\pi i \varphi}$, and (3) $t = n + [\log(2 + \frac{1}{2\epsilon})]$ qubits initialized to $|0\rangle$

Outputs: An n -bit approximation $\tilde{\varphi}_u$ to φ_u

Runtime: $O(t^2)$ operations and one call to controlled- U^j black box. Succeeds with probability at least $1 - \epsilon$.

Procedure:

1. $|0\rangle |u\rangle$ initial state
2. $\rightarrow \frac{1}{\sqrt{2^t}} \sum_{j=0}^{2^t-1} |j\rangle |u\rangle$ create superposition
3. $\rightarrow \frac{1}{\sqrt{2^t}} \sum_{j=0}^{2^t-1} |j\rangle U^j |u\rangle$ apply black box
4. $= \frac{1}{\sqrt{2^t}} \sum_{j=0}^{2^t-1} e^{2\pi i j \varphi_u} |j\rangle |u\rangle$ result of black box
5. $\rightarrow |\tilde{\varphi}_u\rangle |u\rangle$
6. $\rightarrow \tilde{\varphi}_u$

Quantum Fourier Transform Shor's Algorithm

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