

# Household Labor Supply and Child-Related Transfers

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# Plan for today

- Dynamic labor supply of **couples** + children  
Guner, Kaygusuz and Ventura (2020): "Child-Related Transfers, Household Labor Supply and Welfare"  
Related paper: Wang (2022, R&R, ReStud)

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- **Reading guide:**
  1. What are the main *research questions*?
  2. What is the (*empirical*) *motivation*?
  3. What are the central *mechanisms in the model*?
  4. What is the *simplest model* in which we could capture these?

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  1. What are the main *research questions*?
    - How do different child-related transfers affect labor supply?
    - Could alternative combinations increase welfare?
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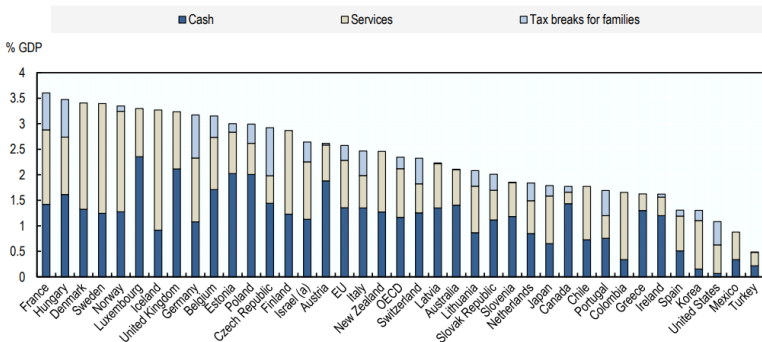
# Empirical Motivation: I

## ● Large differences in governmental spending on child-related policies

[https://www.oecd.org/els/soc/PF1\\_1\\_Public\\_spending\\_on\\_family\\_benefits.pdf](https://www.oecd.org/els/soc/PF1_1_Public_spending_on_family_benefits.pdf)

**Chart PF1.1.A. Public spending on family benefits**

Public expenditure on family benefits by type of expenditure, in per cent of GDP, 2017 and latest available



Note: Public spending accounted for here concerns public support that is exclusively for families (e.g. child payments and allowances, parental leave benefits and childcare support), only. Spending in other social policy areas such as health and housing support also assists families, but not exclusively, and is not included here. Coverage of spending on family and community services in the OECD Social Expenditure data may be limited as such services are often provided and/or co-financed by local governments. The latter may receive general block grants to finance their activities, and reporting requirements may not be sufficient for central statistical agencies to have a detailed view of the nature of local spending. In Nordic countries (where local government is heavily involved in service

# Empirical Motivation: II

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- **Many ways** to subsidize families, however

- Conditional on work ("Unconditional"/"Conditional")  
(incentivize work)
- Means-tested on income ("Universal"/"Means-tested")  
(re-distribution but dis-incentivize work a bit)
- Conditional on childcare usage ("Transfer"/"Subsidy")  
(incentivize work through co-payment)

→ Need a **unified framework** (model) to evaluate them!

# Taxonomy (my modifications)

		Universal	Means-Tested
Unconditional	1	Transfer Child benefits DK (mild means-tested from 2014)	2 Child Credits
	1b	Subsidy	2b Childcare subsidy in DK: co-payment ~25%
Conditional	3	Subsidy Childcare Credits	4 Subsidy Childcare Subsidy
	5	Transfer	6 Transfer

FIGURE 1

Taxonomy of child-related transfers.

- Guner, Kaygusuz and Ventura (2020) do not entertain 1b and 2b.

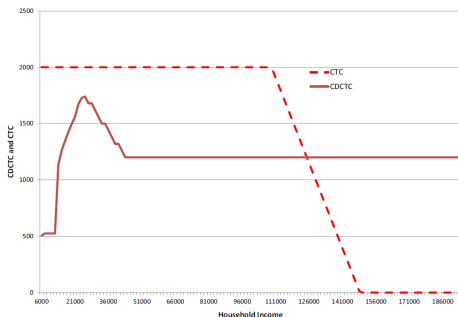


# US Background

- **Childcare subsidies (4):** Child Care Development Fund (CCDF)  
~75% childcare subsidy to low-income employed households  
(useful for working people with childcare expenses)

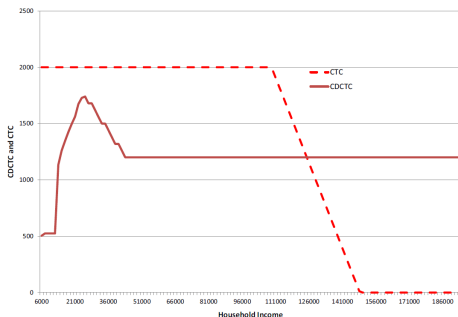
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~\$1,200-\$2,100 (dep. on income) tax deduction of childcare expenses.  
(useful for working people with childcare expenses)
- **Child Credits (2):** Child Tax Credit (CTC) + Additional CTC (ACTC)  
~\$1,000 per child but is a tax-credit (reason for ACTC).



# Outline

## 1 Model Overview

## 2 Simulation Results

## 3 Simple Model

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General equilibrium ( $w$  and  $r$ )

Overlapping generations (OLG)

Period is 5 years,  $j$  is period

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- **Childcare:**

If a woman works, the household has to pay childcare costs.

Access to informal childcare ( $g = 1$ ) reduces cost



# Model Overview

- **Types:**  $x, z$  is educational type of men and women
- **Income:**

$$\text{men} : w\omega_m(z, j)\varepsilon_z l_m$$

$$\text{women} : wh\varepsilon_x l_f$$

$$\log h' = \log h + \alpha_j^x \chi(l_f) - \delta_x (1 - \chi(l_f))$$

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If women work, they incur costs of

$$D = wk(z, x)d(s, x, z, g)$$

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where  $s$  is age of child,  $g$  is informal childcare availability.

- **Childcare subsidies:** Parents pay  $(1 - \theta)$  of childcare costs if working:

$$(1 - \theta)D\chi(l_f)$$

if household income less than  $\hat{l}$  (determined endo. to match take-up).

# Model Overview: Preferences

- **Individual** preferences [my notation]

$$U(c, l, k_y) = \log c - \phi(l + k_y \eta)^{1 + \frac{1}{\gamma}}$$

where  $k_y = 1$  if there is a young child present

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- **Household** utility is sum

$$U(c, l_f, l_m, k_y, q) = U(c, l_f, k_y) + U(c, l_m, 0) - q\chi(l_f)$$

where  $q$  is a (random) household-specific cost of “joint work”  
(but should it then be  $q\chi(l_f)\chi(l_m)$ ?)

- **Imposes** that women are less likely to work when children.

# Bellman Equation, Working Couple.

**3.7.2. The problem of married households.** Like singles, married couples decide how much to consume, how much to save, and how much to work. They also decide whether the female member of the household should work. Their problem is given by

$$V^M(a, h, s^M, j) = \max_{a', l_f, l_m} \{ [U_f^M(c, l_f, q, k_y) + U_m^M(c, l_m, l_f, q)] + \beta V^M(a', h', s^M, j+1) \},$$

subject to

(i) *With kids:* if  $b = \{1, 2\}$ ,  $j \in \{b, b+1, b+2\}$ , then the household has  $k(x, z)$  children and

$$c + a' = \begin{cases} a(1+r(1-\tau_k)) + w(\varpi_m(z, j)\varepsilon_z l_m + h\varepsilon_x l_f)(1-\tau_p) \\ \quad - T^M(I, k(x, z)) + TR^M(I, D(1-\theta), k(x, z)) \\ \quad - D(1-\theta)\chi(l_f), \text{ if } I \leq \hat{I} \\ a(1+r(1-\tau_k)) + w(\varpi_m(z, j)\varepsilon_z l_m + h\varepsilon_x l_f)(1-\tau_p) \\ \quad - T^M(I, k(x, z)) + TR^M(I, D, k(x, z)) \\ \quad - D\chi(l_f), \text{ otherwise} \end{cases},$$

where  $I = w\varpi_m(z, j)\varepsilon_z l_m + wh\varepsilon_x l_f + ra$  and  $D = wd(j+1-b, x, z, g)k(x, z)$ . Furthermore, if  $b=j$ , then  $k_y=1$ .

- $s^M = (x, z, \varepsilon_x, \varepsilon_z, q, b, g)$ .  $b \in \{1, 2\}$ , where 2 is child-bearing
- $TR$ : transfers

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- 2 Simulation Results**
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# Simulation Results, Guner, Kaygusuz and Ventura (2020)

**Q1: What happens if we change current system** (spread on three types) by using all expenditures in one single type only?



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- **keeps** government budget fixed (I think).  
Meant to illustrate the incentives
- **Implies that the current system is not optimal** (if fixed budget)  
Could still be optimal to have a mix (not analyzed)  
What about the 1b and 2b alternatives? Co-payments encourage work.

# Counterfactual Reforms

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**1. Universal subsidies:**

Remove means-testing in 75% childcare subsidy (CCDF and 1.2% tax)  
[by setting income threshold  $\hat{I} = \infty$ ]

**2. Child credit expansion:**

Increase CTC from \$1,000 to \$1,800 per child, unchanged income threshold (and 1.2% tax)

**3. Childcare credit expansion:**

Increase the CDCTC by factor  $\sim 2$   
(non-usable tax credit payed out and 1.2% tax)

**4. New child credit:**

Increase CTC from \$1,000 to \$2,000 per child, increased income threshold (and 1.35% tax)

# Counterfactual Reforms, Labor Supply

TABLE 4  
*Expansion of child-related transfers (% changes relative to benchmark)*

	Universal subsidies (75%)	Child credit expansion	Childcare credit expansion	New child credit
Participation of married females	10.2	-2.4	10.6	-2.6
Total hours	1.8	-1.4	1.5	-1.5
Total hours (married females)	8.6	-3.1	8.6	-3.3
Hours per worker (all females)	-1.1	-1.1	-1.6	-1.3
Hours per worker (married females)	-1.8	-0.7	-2.2	-0.9
Hours per worker (single females)	0.2	-1.5	-0.3	-1.9
Hours per worker (all males)	-1.5	-0.7	-1.7	-0.7
Human capital (married females)	2.8	-0.8	2.5	-0.8
Output	0.5	-1.7	0.7	-1.5
Tax rate (%)	1.2	1.2	1.2	1.35
Participation of married females:				
By education				
<HS	25.4	-6.4	32.0	-7.2
HS	13.3	-4.4	16.9	-4.8
SC	9.1	-2.5	10.4	-2.8
COL	9.4	-1.2	7.0	-1.3
COL+	5.2	-0.7	2.8	-0.3
By child bearing status				
Early	14.9	-4.0	17.0	-4.4
Late	8.2	-1.5	6.9	-1.4

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TABLE 5  
*Expansion of child-related transfers: welfare effects (newborns, %)*

	Childcare subsidy (75%)	Child credit	Childcare credit	New child credit
Single F				
No children	-1.41	-1.40	-1.46	-1.62
Early	4.25	5.99	10.06	6.71
Late	3.40	3.58	7.40	4.25
Informal care	4.15	5.44	9.62	6.03
No informal care	3.69	5.23	8.84	6.15
<HS	1.85	8.43	6.95	9.55
HS	2.54	4.93	6.66	5.62
SC	2.41	2.39	6.40	2.65
COL	1.08	0.33	2.43	0.37
COL+	0.56	-0.54	1.19	-0.56
Non-mothers always lose				
Married				
No children	-3.16	-3.14	-3.29	-3.61
Early	2.90	3.59	5.80	4.76
Late	0.50	0.85	1.51	1.41
Informal care	2.02	2.09	3.84	3.96
No informal care	1.18	2.95	3.74	2.93
All newborns	0.84	1.28	2.51	1.73
(%) winners	48.0	54.3	50.9	57.7
All newborns (weighted welfare)	0.04	0.04	0.14	~0

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but majority of voters and the government might prefer it

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# Our simple model

- **Dual-earner model from last time**

- **Modification:**

A child can arrive with probability

$$p(n_t) = \begin{cases} p_n & \text{if } n_t = 0 \\ 0 & \text{if } n_t = 1 \end{cases}$$

- **Taxes and transfers:**

Taxes on household level

Childcare costs if both work

Child credits

- **Reform of interest:**

Child-related transfers

# Our simple model: **Recursive formulation**

$$V_t(n_t, K_{1,t}, K_{2,t}) = \max_{h_{1,t}, h_{2,t}} U(c_t, h_{1,t}, h_{2,t}, n_t) \\ + \beta \mathbb{E}_t[V_{t+1}(n_{t+1}, K_{1,t+1}, K_{2,t+1})]$$

$$c_t = Y_t - T(Y_t + \mathcal{C}) + \mathcal{C}$$

$$Y_t = \sum_{j=1}^2 w_{j,t} h_{j,t}$$

$$n_{t+1} = \begin{cases} 1 & \text{with prob. } p(n_t) \\ 0 & \text{with prob. } 1 - p(n_t) \end{cases}$$

$$\log w_{j,t} = \alpha_{j,0} + \alpha_{j,1} K_{j,t}, \quad j \in \{1, 2\}$$

$$K_{j,t+1} = (1 - \delta) K_{j,t} + h_{j,t}, \quad j \in \{1, 2\}$$

- **Child-related transfers**

$$\mathcal{C}(n_t, h_{1,t}, h_{2,t}, w_{1,t}, w_{2,t}) = \mathcal{C}_1(n_t) + \mathcal{C}_2(n_t, Y_t) \\ + [\mathcal{C}_3(n_t) + \mathcal{C}_4(n_t, Y_t)] \cdot \mathbf{1}(h_{1,t} \cdot h_{2,t} > 0)$$

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$$U(c_t, h_{1,t}, h_{2,t}) = 2 \frac{(c_t/2)^{1+\eta}}{1+\eta} - \rho_1(n_t) \frac{h_{1,t}^{1+\gamma}}{1+\gamma} - \rho_2(n_t) \frac{h_{2,t}^{1+\gamma}}{1+\gamma}$$

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- **Expected value** is

$$\begin{aligned} \mathbb{E}_t[V_{t+1}(n_{t+1}, K_{1,t+1}, K_{2,t+1})] &= p(n_t) V_{t+1}(n_t + 1, K_{1,t+1}, K_{2,t+1}) \\ &\quad + (1 - p(n_t)) V_{t+1}(n_t, K_{1,t+1}, K_{2,t+1}) \end{aligned}$$



# Next Time

- **Next time:**

Models of Household Behavior.

- **Literature:**

Chiappori and Mazzocco (2017): "Static and Intertemporal Household Decisions"

+ my guide

- **Read** before lecture

- **Reading guide:**

Section 1: Introduction + overview. Read.

Section 2: Static models. Read. Read details fast.

Section 3: Dynamic models. Get the idea of limited commitment. Do not get stuck.

Section 4: Tests. We won't cover this, you can skip.

Section 5: Policies. Short, might be worth a read.

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- CHIAPPORI, P.-A. AND M. MAZZOCCO (2017): “Static and Intertemporal Household Decisions,” *Journal of Economic Literature*, 55(3), 985–1045.
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