

# 677 HW1

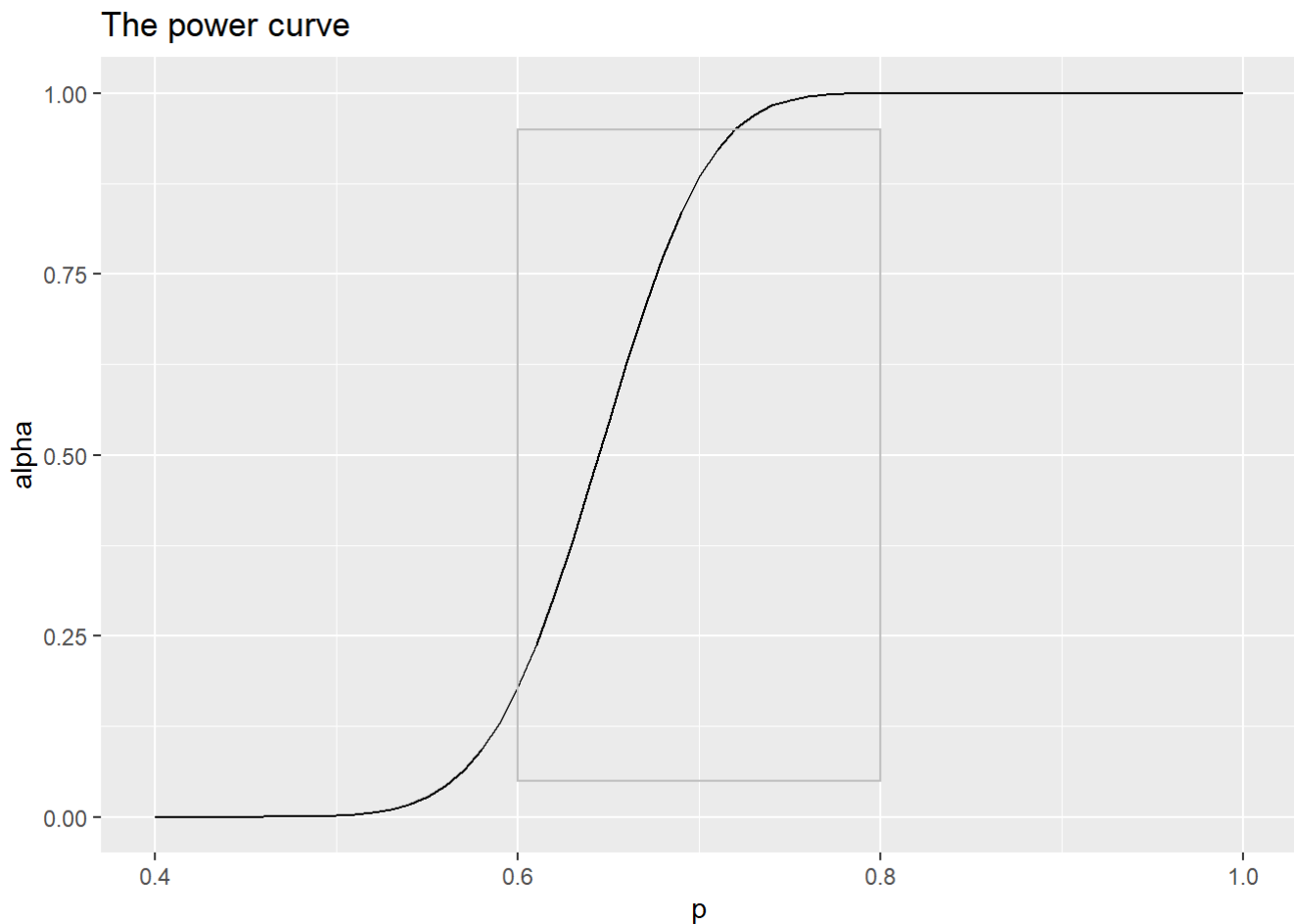
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To show how did the author of the book get critical value  $m$  that while  $m=69$  to thwarts type 1 error and  $m=73$  to thwarts type 2 error, I write a function named Plot to show the process of finding these two critical value. I set  $p$  as a sequence from 0.4 to 1 by 0.01 each. I used probability density function to get desired  $a(p)$ , the sum probability we reject the null hypothesis is true.

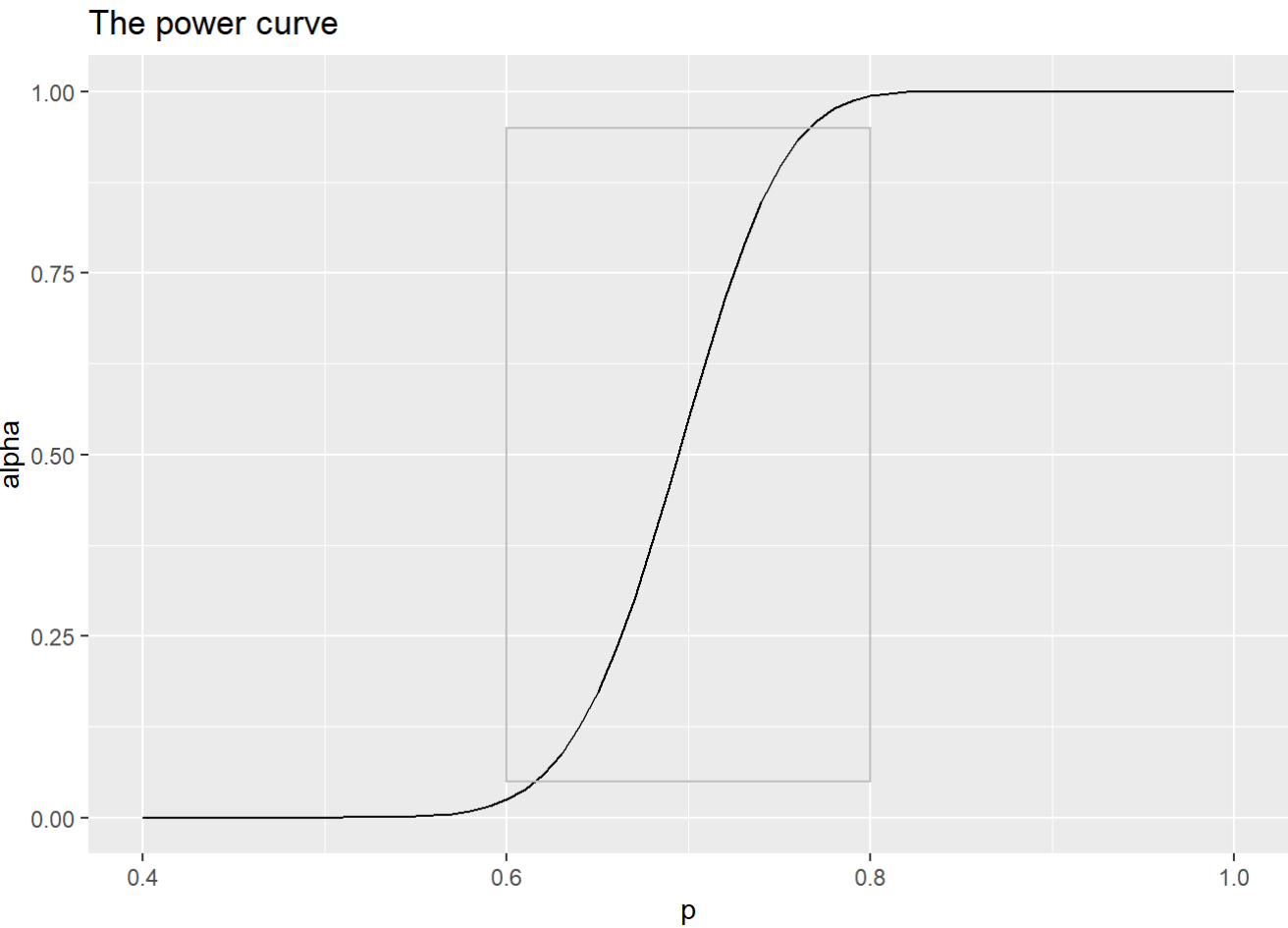
```
library(ggplot2)
Plot <-function(m) {
  n <-100
  p <-seq(0.4, 1, 0.01)
  ap <-c()
  for (i in p){
    a <- sum(dbinom(m:n,n, i))
    ap <-c(ap, a)
  }
  ggplot()+geom_line(aes(p, ap))+geom_rect(aes(xmin = 0.6, xmax = 0.8, ymin = 0.05, ymax = 0.95), alpha=0, color="grey")+ggtitle("The power curve")+ylab("alpha")
}
```

I started to plug value of  $m$  from 0-100 to find the critical values which pass the bottom left and top right of the rectangle in Figure 3.7. As the  $m$  increases, the line moves to the right. Examples of  $m=65, 70, 75$ .

Plot (65)

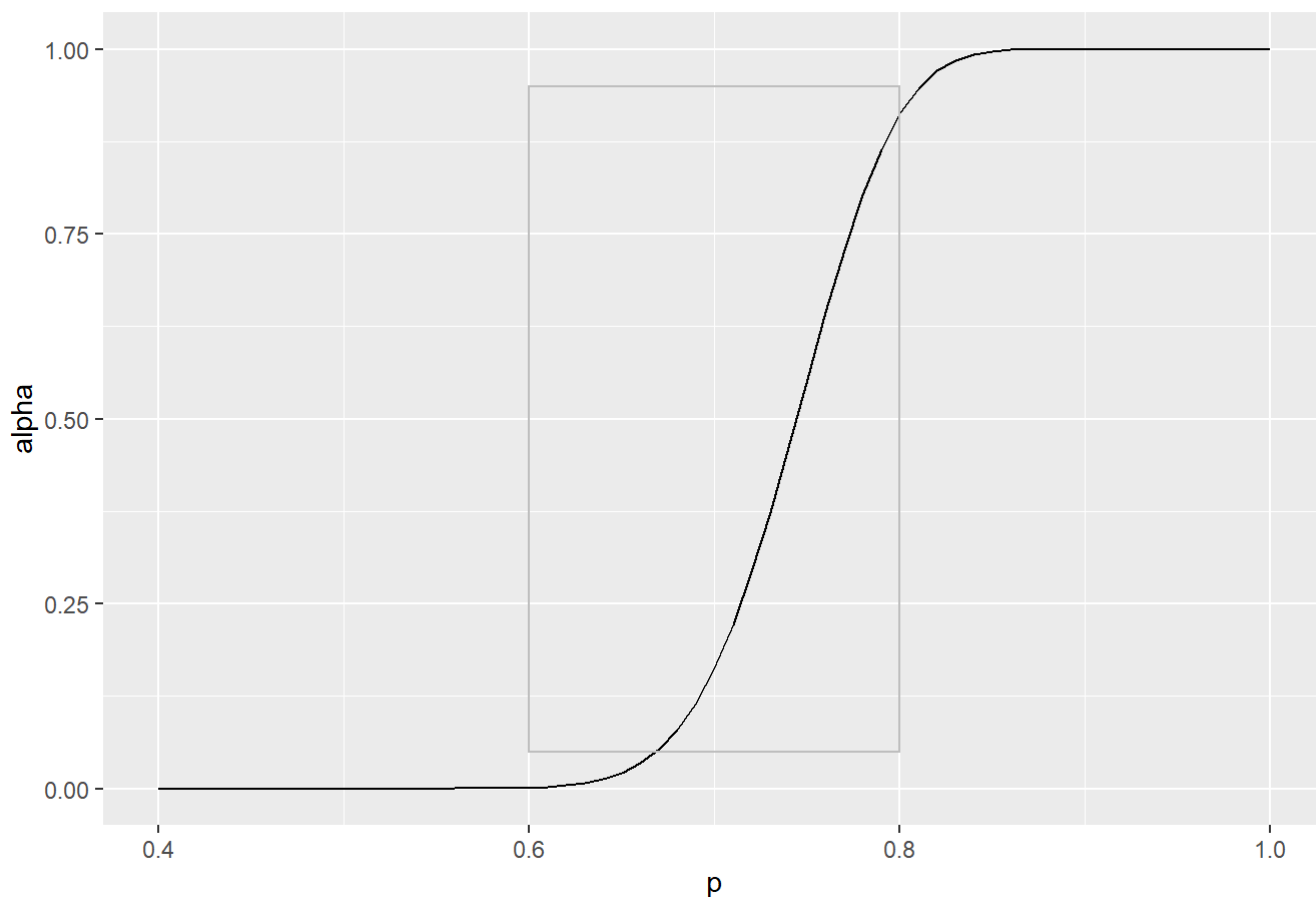


Plot (70)



Plot (75)

## The power curve



After narrowing down numbers, I found while  $m=69$ , the line just enters the bottom, and while  $m=73$ , the line just leaves from the top. Therefore, 69 is the smallest  $m$  thwarts type 1 error and 73 is the largest which thwarts a type 2 error.

```
n <- 100
p <- seq(0.4, 1, 0.01)
ap69 <- c()
for (i in p) {
  a <- sum(dbinom(69:n, n, i))
  ap69 <- c(ap69, a)
}
ap73 <- c()
for (i in p) {
  a <- sum(dbinom(73:n, n, i))
  ap73 <- c(ap73, a)
}
ggplot()+geom_line(aes(p, ap69))+geom_line(aes(p, ap73))+geom_rect(aes(xmin = 0.6, xmax = 0.8, ymin = 0.05, ymax = 0.95), alpha=0, color="grey")+ggtitle("The power curve")+ylab("alpha")
```

The power curve

