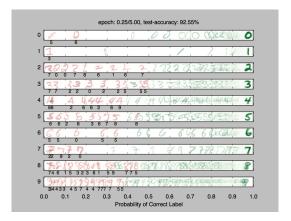
# Project 5: Machine Learning (due 12/3 at 4:00pm)

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In this project you will build a neural network to classify digits, and more!

# Introduction

This project will be an introduction to machine learning.

The code for this project contains the following files, available as a zip archive (assets/files/machinelearning.zip).

Note: In this project you only need to submit the token generated by submission\_autograder.py . See Submission for details.

Files you'll edit:		
models.py	Perceptron and neural network models for a variety of applications	
Files you should read but NOT edit:		
nn.py	Neural network mini-library	
Files you will not edit:		
autograder.py	Project autograder	
backend.py	Backend code for various machine learning tasks	
data	Datasets for digit classification and language identification	
submission_autograder.py	Submission autograder (generates tokens for submission)	

Files to Edit and Submit: You will fill in portions of models.py during the assignment. Please do not change the other files in this distribution

Note: You only need to submit machinelearning.token, generated by running submission\_autograder.py. It contains the evaluation results from your local autograder, and a copy of all your code. You do not need to submit any other files.

**Evaluation:** Your code will be autograded for technical correctness. Please *do not* change the names of any provided functions or classes within the code, or you will wreak havoc on the autograder. However, the correctness of your implementation -- not the autograder's judgements -- will be the final judge of your score. If necessary, we will review and grade assignments individually to ensure that you receive due credit for your work.

Academic Dishonesty. We will be checking your code against other submissions in the class for logical redundancy. If you copy someone else's code and submit it with minor changes, we will know. These cheat detectors are quite hard to fool, so please don't try. We trust you all to submit your own work only; please don't let us down. If you do, we will pursue the strongest consequences available to us.

**Proper Dataset Use:** Part of your score for this project will depend on how well the models you train perform on the test set included with the autograder. We do not provide any APIs for you to access the test set directly. Any attempts to bypass this separation or to use the testing data during training will be considered cheating.

**Getting Help:** You are not alone! If you find yourself stuck on something, contact the course staff for help. Office hours, section, and the discussion forum are there for your support; please use them. If you can't make our office hours, let us know and we will schedule more. We want these projects to be rewarding and instructional, not frustrating and demoralizing. But, we don't know when or how to help unless you ask.

Discussion: Please be careful not to post spoilers.

### Installation

For this project, you will need to install the following two libraries:

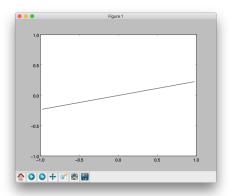
- numpy (http://www.numpy.org/), which provides support for large multi-dimensional arrays installation instructions (https://docs.scipy.org/doc/numpy-1.13.0/user/install.html)
- matplotlib (https://matplotlib.org/), a 2D plotting library installation instructions (https://matplotlib.org/users/installing.html)

You will not be using these libraries directly, but they are required in order to run the provided code and autograder.

To test that everything has been installed, run:

python autograder.py --check-dependencies

If numpy and matplotlib are installed correctly, you should see a window pop up where a line segment spins in a circle:



### Provided Code (Part I)

For this project, you have been provided with a neural network mini-library (nn.py) and a collection of datasets (backend.py).

The library in nn.py defines a collection of node objects. Each node represents a real number or a matrix of real numbers.

Operations on Node objects are optimized to work faster than using Python's built-in types (such as lists).

Here are a few of the provided node types:

- nn. Constant represents a matrix (2D array) of floating point numbers. It is typically used to represent input features or target outputs/labels. Instances of this type will be provided to you by other functions in the API; you will not need to construct them directly
- nn.Parameter represents a trainable parameter of a perceptron or neural network
- nn.DotProduct computes a dot product between its inputs

Additional provided functions:

• nn.as\_scalar can extract a Python floating-point number from a node.

When training a perceptron or neural network, you will be passed a dataset object. You can retrieve batches of training examples by calling dataset.iterate\_once(batch\_size):

```
for x, y in dataset.iterate_once(batch_size):
...
```

For example, let's extract a batch of size 1 (i.e. a single training example) from the perceptron training data:

The input features x and the correct label y are provided in the form of nn.Constant nodes. The shape of x will be batch\_size x num\_features, and the shape of y is batch\_size x num\_outputs. Here is an example of computing a dot product of x with itself, first as a node and then as a Python number.

```
>>> nn.DotProduct(x, x)
<DotProduct shape=1x1 at 0x11a89edd8>
>>> nn.as_scalar(nn.DotProduct(x, x))
1.9756581717465536
```

#### Question 1 (6 points): Perceptron

Before starting this part, be sure you have numpy and matplotlib installed!

In this part, you will implement a binary perceptron. Your task will be to complete the implementation of the PerceptronModel class in models.py.

For the perceptron, the output labels will be either 1 or -1, meaning that data points (x, y) from the dataset will have y be a nn. Constant node that contains either 1 or -1 as its entries.

We have already initialized the perceptron weights self.w to be a 1x dimensions parameter node. The provided code will include a bias feature inside x when needed, so you will not need a separate parameter for the bias.

Your tasks are to:

- Implement the run(self, x) method. This should compute the dot product of the stored weight vector and the given input, returning an nn.DotProduct object.
- Implement get\_prediction(self, x), which should return 1 if the dot product is non-negative or -1 otherwise. You should use nn.as\_scalar to convert a scalar Node into a Python floating-point number.
- Write the train(self) method. This should repeatedly loop over the data set and make updates on examples that are misclassified. Use the update method of the nn.Parameter class to update the weights. When an entire pass over the data set is completed without making any mistakes, 100% training accuracy has been achieved, and training can terminate.

In this project, the only way to change the value of a parameter is by calling <code>parameter.update(direction, multiplier)</code>, which will perform the update to the weights:

 $weights \leftarrow weights + direction \cdot multiplier$ 

The direction argument is a Node with the same shape as the parameter, and the multiplier argument is a Python scalar.

To test your implementation, run the autograder:

python autograder.py -q q1

**Note:** the autograder should take at most 20 seconds or so to run for a correct implementation. If the autograder is taking forever to run, your code probably has a bug.

#### **Neural Network Tips**

In the remaining parts of the project, you will implement the following models:

- · Q2: Regression
- Q3: Handwritten Digit Classification
- Q4: Language Identification

### **Building Neural Nets**

Throughout the applications portion of the project, you'll use the framework provided in nn.py to create neural networks to solve a variety of machine learning problems. A simple neural network has layers, where each layer performs a linear operation (just like perceptron). Layers are separated by a non-linearity, which allows the network to approximate general functions. We'll use the ReLU operation for our non-linearity, defined as  $relu(x) = \max(x,0)$ . For example, a simple two-layer neural network for mapping an input row vector  $\mathbf{x}$  to an output vector  $\mathbf{f}(\mathbf{x})$  would be given by the function:

$$\mathbf{f}(\mathbf{x}) = relu(\mathbf{x} \cdot \mathbf{W_1} + \mathbf{b_1}) \cdot \mathbf{W_2} + \mathbf{b_2}$$

where we have parameter matrices  $\mathbf{W_1}$  and  $\mathbf{W_2}$  and parameter vectors  $\mathbf{b_1}$  and  $\mathbf{b_2}$  to learn during gradient descent.  $\mathbf{W_1}$  will be an  $i \times h$  matrix, where i is the dimension of our input vectors  $\mathbf{x}$ , and h is the hidden layer size.  $\mathbf{b_1}$  will be a size h vector. We are free to choose any value we want for the hidden size (we will just need to make sure the dimensions of the other matrices and vectors agree so that we can perform the operations). Using a larger hidden size will usually make the network more powerful (able to fit more training data), but can make the network harder to train (since it adds more parameters to all the matrices and vectors we need to learn), or can lead to overfitting on the training data.

We can also create deeper networks by adding more layers, for example a three-layer net:

$$f(\mathbf{x}) = relu(relu(\mathbf{x} \cdot \mathbf{W_1} + \mathbf{b_1}) \cdot \mathbf{W_2} + \mathbf{b_2}) \cdot \mathbf{W_3} + \mathbf{b_3}$$

### Note on Batching

For efficiency, you will be required to process whole batches of data at once rather than a single example at a time. This means that instead of a single input row vector x with size i, you will be presented with a batch of b inputs represented as a  $b \times i$  matrix X. We provide an example for linear regression to demonstrate how a linear layer can be implemented in the batched setting.

# Note on Randomness

The parameters of your neural network will be randomly initialized, and data in some tasks will be presented in shuffled order. Due to this randomness, it's possible that you will still occasionally fail some tasks even with a strong architecture -- this is the problem of local optima! This should happen very rarely, though -- if when testing your code you fail the autograder twice in a row for a question, you should explore other architectures.

# Practical tips

Designing neural nets can take some trial and error. Here are some tips to help you along the way:

- <u>Be systematic.</u> Keep a log of every architecture you've tried, what the hyperparameters (layer sizes, learning rate, etc.) were, and what the resulting performance was. As you try more things, you can start seeing patterns about which parameters matter. If you find a bug in your code, be sure to cross out past results that are invalid due to the bug.
- Start with a shallow network (just two layers, i.e. one non-linearity). Deeper networks have exponentially more hyperparameter combinations, and getting even a single one wrong can ruin your performance. Use the small network to find a good learning rate and layer size; afterwards you can consider adding more layers of similar size.
- If your learning rate is wrong, none of your other hyperparameter choices matter. You can take a state-of-the-art model from a research paper, and change the learning rate such that it performs no better than random.
- Smaller batches require lower learning rates. When experimenting with different batch sizes, be aware that the best learning rate
  may be different depending on the batch size.
- Making the network too wide generally doesn't hurt accuracy too much. If you keep making the network wider accuracy will
  gradually decline, but computation time will increase quadratically in the layer size -- you're likely to give up due to excessive
  slowness long before the accuracy falls too much. The full autograder for all parts of the project takes 2-12 minutes to run with

staff solutions; if your code is taking much longer you should check it for efficiency.

- If your model is returning Infinity or NaN, your learning rate is probably too high for your current architecture.
- Recommended values for your hyperparameters:
  - Hidden layer sizes: between 10 and 400
  - Batch size: between 1 and the size of the dataset. For Q2 and Q3, we require that total size of the dataset be evenly divisible
    by the batch size.
  - Learning rate: between 0.001 and 1.0
  - o Number of hidden layers: between 1 and 3

#### **Provided Code (Part II)**

Here is a full list of nodes available in nn.py. You will make use of these in the remaining parts of the assignment:

- nn. Constant represents a matrix (2D array) of floating point numbers. It is typically used to represent input features or target outputs/labels. Instances of this type will be provided to you by other functions in the API; you will not need to construct them directly
- nn.Parameter represents a trainable parameter of a perceptron or neural network. All parameters must be 2-dimensional.
  - $\circ$  Usage: nn.Parameter(n, m) constructs a parameter with shape n imes m
- nn.Add adds matrices element-wise
  - Usage: nn.Add(x, y) accepts two nodes of shape batch\_size x num\_features and constructs a node that also has shape batch\_size x num\_features
- nn.AddBias adds a bias vector to each feature vector
  - Usage: nn.AddBias(features, bias) accepts features of shape batch\_size x num\_features and bias of shape
     1 x num\_features, and constructs a node that has shape batch\_size x num\_features.
- nn.Linear applies a linear transformation (matrix multiplication) to the input
  - Usage: nn.Linear(features, weights) accepts features of shape batch\_size x num\_input\_features and weights of shape num\_input\_features x num\_output\_features, and constructs a node that has shape batch size x num output features.
- nn.ReLU applies the element-wise Rectified Linear Unit nonlinearity relu(x) = max(x, 0). This nonlinearity replaces all negative entries in its input with zeros.
  - Usage: nn.ReLU(features), which returns a node with the same shape as the input.
- nn.SquareLoss computes a batched square loss, used for regression problems
  - Usage: nn.SquareLoss(a, b), where a and b both have shape batch\_size x num\_outputs.
- nn.SoftmaxLoss computes a batched softmax loss, used for classification problems
  - Usage: nn.SoftmaxLoss(logits, labels), where logits and labels both have shape batch\_size x num\_classes. The
    term "logits" refers to scores produced by a model, where each entry can be an arbitrary real number. The labels, however,
    must be non-negative and have each row sum to 1. Be sure not to swap the order of the arguments!
- Do not use nn.DotProduct for any model other than the perceptron

The following methods are available in nn.py:

- nn.gradients computes gradients of a loss with respect to provided parameters.
  - Usage: nn.gradients(loss, [parameter\_1, parameter\_2, ..., parameter\_n]) will return a list [gradient\_1, gradient\_2, ..., gradient\_n], where each element is an nn.Constant containing the gradient of the loss with respect to a parameter.
- nn.as\_scalar can extract a Python floating-point number from a loss node. This can be useful to determine when to stop training
  - $\circ$  Usage: nn.as\_scalar(node) , where node is either a loss node or has shape  $1 \times 1$ .

The datasets provided also have two additional methods:

- dataset.iterate\_forever(batch\_size) yields an infinite sequences of batches of examples.
- dataset.get\_validation\_accuracy() returns the accuracy of your model on the validation set. This can be useful to determine
  when to stop training.

### **Example: Linear Regression**

As an example of how the neural network framework works, let's fit a line to a set of data points. We'll start four points of training data constructed using the function  $y = 7x_0 + 8x_1 + 3$ . In batched form, our data is:

$$\mathbf{X} = \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix} \text{ and } \mathbf{Y} = \begin{bmatrix} 3 \\ 11 \\ 10 \\ 18 \end{bmatrix}$$

Suppose the data is provided to us in the form of nn. Constant nodes:

```
>>> x
<Constant shape=4x2 at 0x10a30fe80>
>>> y
<Constant shape=4x1 at 0x10a30fef0>
```

Let's construct and train a model of the form  $f(x) = x_0 \cdot m_0 + x_1 \cdot m_1 + b$ . If done correctly, we should be able to learn than  $m_0 = 7$ ,  $m_1 = 8$ , and b = 3.

First, we create our trainable parameters. In matrix form, these are:

$$\mathbf{M} = \left[egin{array}{c} m_0 \ m_1 \end{array}
ight]$$
 and  $\mathbf{B} = \left[\,b\,
ight]$ 

Which corresponds to the following code:

```
m = nn.Parameter(2, 1)
b = nn.Parameter(1, 1)
```

Printing them gives:

```
>>> m
<Parameter shape=2x1 at 0x112b8b208>
>>> b
<Parameter shape=1x1 at 0x112b8beb8>
```

Next, we compute our model's predictions for y:

```
xm = nn.Linear(x, m)
predicted_y = nn.AddBias(xm, b)
```

Our goal is to have the predicted y-values match the provided data. In linear regression we do this by minimizing the square loss:  $\mathcal{L} = \frac{1}{2N} \sum_{(x,y)} (y - f(x))^2$ 

We construct a loss node:

```
loss = nn.SquareLoss(predicted_y, y)
```

In our framework, we provide a method that will return the gradients of the loss with respect to the parameters:

```
grad_wrt_m, grad_wrt_b = nn.gradients(loss, [m, b])
```

Printing the nodes used gives:

```
>>> xm

<Linear shape=4x1 at 0x11a869588>
>>> predicted_y

<AddBias shape=4x1 at 0x11c23aa90>
>>> loss

<SquareLoss shape=() at 0x11c23a240>
>>> grad_wrt_m

<Constant shape=2x1 at 0x11a8cb160>
>>> grad_wrt_b

<Constant shape=1x1 at 0x11a8cb588>
```

We can then use the update method to update our parameters. Here is an update for m, assuming we have already initialized a multiplier variable based on a suitable learning rate of our choosing:

```
m.update(grad_wrt_m, multiplier)
```

If we also include an update for **b** and add a loop to repeatedly perform gradient updates, we will have the full training procedure for linear regression.

#### Question 2 (6 points): Non-linear Regression

For this question, you will train a neural network to approximate  $\sin(x)$  over  $[-2\pi, 2\pi]$ .

You will need to complete the implementation of the RegressionModel class in models.py. For this problem, a relatively simple architecture should suffice (see Neural Network Tips for architecture tips.) Use nn.SquareLoss as your loss.

Your tasks are to:

- Implement RegressionModel.run to return a batch\_size x 1 node that represents your model's prediction.
- Implement RegressionModel.get\_loss to return a loss for given inputs and target outputs.
- Implement RegressionModel.train, which should train your model using gradient-based updates.

There is only a single dataset split for this task, i.e. there is only training data and no validation data or test set. Your implementation will receive full points if it gets a loss of 0.02 or better, averaged across all examples in the dataset. You may use the training loss to determine when to stop training (use nn.as\_scalar to convert a loss node to a Python number).

python autograder.py -q q2

#### Question 3 (6 points): Digit Classification

For this question, you will train a network to classify handwritten digits from the MNIST dataset.

Each digit is of size  $28 \times 28$  pixels, the values of which are stored in a 784-dimensional vector of floating point numbers. Each output we provide is a 10-dimensional vector which has zeros in all positions, except for a one in the position corresponding to the correct class of the digit.

Complete the implementation of the DigitClassificationModel class in models.py. The return value from DigitClassificationModel.run() should be a batch\_size x 10 node containing scores, where higher scores indicate a higher probability of a digit belonging to a particular class (0-9). You should use nn.SoftmaxLoss as your loss.

For both this question and Q4, in addition to training data there is also validation data and a test set. You can use dataset.get\_validation\_accuracy() to compute validation accuracy for your model, which can be useful when deciding whether to stop training. The test set will be used by the autograder.

To receive points for this question, your model should achieve an accuracy of at least 97% on the test set. For reference, our staff implementation consistently achieves an accuracy of 98% on the validation data after training for around 5 epochs.

To test your implementation, run the autograder:

python autograder.py -q q3

### Question 4 (7 points): Language Identification

Language identification is the task of figuring out, given a piece of text, what language the text is written in. For example, your browser might be able to detect if you've visited a page in a foreign language and offer to translate it for you. Here is an example from Chrome (which uses a neural network to implement this feature):



In this project, we're going to build a smaller neural network model that identifies language for one word at a time. Our dataset consists of words in five languages, such as the table below:

Word	Language	
discussed	English	
eternidad	Spanish	
itseänne	Finnish	
paleis	Dutch	
mieszkać	Polish	

Different words consist of different numbers of letters, so our model needs to have an architecture that can handle variable-length inputs. Instead of a single input x (like in the previous questions), we'll have a separate input for each character in the word:  $x_0, x_1, \ldots, x_{L-1}$  where L is the length of the word. We'll start by applying a network  $f_{\text{initial}}$  that is just like the feed-forward networks in the previous problems. It accepts its input  $x_0$  and computes an output vector  $h_1$  of dimensionality d:

$$h_1 = f_{\text{initial}}(x_0)$$

Next, we'll combine the output of the previous step with the next letter in the word, generating a vector summary of the the first two letters of the word. To do this, we'll apply a sub-network that accepts a letter and outputs a hidden state, but now also depends on the previous hidden state  $h_1$ . We denote this sub-network as f.

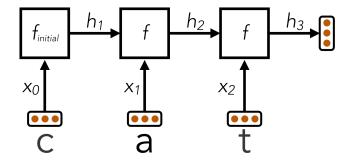
$$h_2=f(h_1,x_1)$$

This pattern continues for all letters in the input word, where the hidden state at each step summarizes all the letters the network has processed thus far:

$$h_3 = f(h_2, x_2)$$

Throughout these computations, the function  $f(\cdot,\cdot)$  is the same piece of neural network and uses the same trainable parameters;  $f_{\text{initial}}$  will also share some of the same parameters as  $f(\cdot,\cdot)$ . In this way, the parameters used when processing words of different length are all shared. You can implement this using a for loop over the provided inputs xs, where each iteration of the loop computes either  $f_{\text{initial}}$  or f.

The technique described above is called a Recurrent Neural Network (RNN). A schematic diagram of the RNN is shown below:



Here, an RNN is used to encode the word "cat" into a fixed-size vector  $h_3$ .

After the RNN has processed the full length of the input, it has encoded the arbitrary-length input word into a fixed-size vector  $h_L$ , where L is the length of the word. This vector summary of the input word can now be fed through additional output layers to generate classification scores for the word's language identity.

### Batching

Although the above equations are in terms of a single word, in practice you must use batches of words for efficiency reasons. For simplicity, our code in the project ensures that all words within a single batch have the same length. In batched form, a hidden state  $h_i$  is replaced with the matrix  $H_i$  of dimensionality  $\mathrm{batch\_size} \times d$ .

### **Design Tips**

The design of the recurrent function f(h, x) is the primary challenge for this task. Here are some tips:

- Start with a feed-forward architecture f<sub>initial</sub>(x) of your choice, as long as it has at least one non-linearity.
- You should use the following method of constructing f(h,x) given  $f_{\text{initial}}(x)$ . The first layer of  $f_{\text{initial}}$  will begin by multiplying the vector  $x_0$  by some weight matrix  $\mathbf W$  to produce  $z_0=x_0\cdot \mathbf W$ . For subsequent letters, you should replace this computation with  $z_i=x_i\mathbf W+h_i\mathbf W_{\text{hidden}}$  using an nn.Add operation. In other words, you should replace a computation of the form z=nn.Linear(x,w) with a computation of the form z=nn.Add(nn.Linear(x,w),nn.Linear(h,w).
- ullet If done correctly, the resulting function f will be non-linear in both x and h
- ullet The hidden size d should be sufficiently large
- Start with a shallow network for f, and figure out good values for the hidden size and learning rate before you make the network deeper. If you start with a deep network right away you will have exponentially more hyperparameter combinations, and getting any single hyperparameter wrong can cause your performance to suffer dramatically.

# Your task

 $\label{lem:complete} \textbf{Complete the implementation of the LanguageIDModel class}.$ 

To receive full points on this problem, your architecture should be able to achieve an accuracy of at least 81% on the test set.

To test your implementation, run the autograder:

python autograder.py -q q4

**Disclaimer.** this dataset was generated using automated text processing. It may contain errors. It has also not been filtered for profanity. However, our reference implementation can still correctly classify over 89% of the validation set despite the limitations of the data. Our reference implementation takes 10-20 epochs to train.

### **Submission**

Submit machinelearning.token, generated by running submission\_autograder.py, to Project 5 on Gradescope.

python3 submission\_autograder.py

The full project autograder takes 2-12 minutes to run for the staff reference solutions to the project. If your code takes significantly longer, consider checking your implementations for efficiency.

Note: You only need to submit machinelearning.token, generated by running submission\_autograder.py. It contains the evaluation results from your local autograder, and a copy of all your code. You do not need to submit any other files.

Please specify any partner you may have worked with and verify that both you and your partner are associated with the submission after submitting.

Congratulations! This was the last project for CS 188!