# Homework 2

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# Knapsack

## Generating Knapsack Problems

In order to get a random knapsack problem, I wanted to make sure that we had a variety of different kinds of Items. So I created 5 different classifications of items: Small Items with weights and values between 1 and 32, Medium Items with weights and values between 1 and 128, Large Items with weights and values between 1 and 512, High Value Items with weights between 1 and 64 and values between 256 and 512, and High Weight Items with weights between 256 and 512 and values between 1 and 64. A Knapsack problem is composed of 256 Small Items, 256 MediumItems, 128 LargeItems, 128 HighValueItems, and 128HighWeightItems randomly shuffled together. The capacity of the knapsack is 1024. The values and weights are randomly generated.

### **Running Times**

The running times for the knapsack problem are as follows:

Algorithm: Greedy Knapsack (Double)

Minimum Time: 1.385 ms

Algorithm: 0/1 Dynamic Programming

Minimum Time: 0.377 ms Maximum Time: 8.188 ms

Algorithm: Minimum Cost Knapsack

Minimum Time: 709.389 ms Maximum Time: 780.577 ms

Average Time: 733.50929999999999999 ms

Algorithm: FPTAS Knapsack Minimum Time: 1579.941 ms Maximum Time: 12269.074 ms Average Time: 3685.9759 ms

These results mostly make sense, the Greedy algorithm should definetly be the fastest although we can see that the fastest time for maximum knapsack did manage to be faster then the fastest greedy time somehow. It should be noted that the Greedy algorithm is at a slight disadvantage as it has to convert its results into integers, which the other algorithms do not have to do.

Minimum Cost taking more time then the maximum solution just means that the sums of the values were larger then the maximum weight of the knapsack which is definetly the case. FPTAS taking twice as long as minimum cost is not terribly suprising the constants in FPTAS are much larger then the constants in Minimum Cost and epsilon was set to between 0.1 and 0.9.

### **Quality of Solutions**

I didn't take the time to specifically test what the averages of FPTAS or Greedy returned compared to what the real optimal solutions returned by maximum or minimum knapsack but in the FuzzTesting file I did make sure that Greedy always got at least within 1/2 of the true answer and that FPTAS always got within the expected range based on the epsilon value.

## Traveling Salesman

The traveling salesman problems I tested on at worst were 1.8 times optimal and at best were 1.41 times optimal.

```
tsp\_problemsburma14.tsp.gz:\ 4704.0-3323.0-1.4155883238037918\\ tsp\_problemsali535.tsp.gz:\ 345022.0-202310.0-1.7054124857891355\\ tsp\_problemsberlin52.tsp.gz:\ 12156.0-7542.0-1.6117740652346857\\ tsp\_problemsbier127.tsp.gz:\ 189412.0-118282.0-1.6013594629783061\\ tsp\_problemsch130.tsp.gz:\ 10332.0-6110.0-1.6909983633387888\\ tsp\_problemsch150.tsp.gz:\ 11756.0-6528.0-1.8008578431372548\\ tsp\_problemsd198.tsp.gz:\ 23476.0-15780.0-1.4877059569074778\\ tsp\_problemsd493.tsp.gz:\ 58542.0-35002.0-1.6725329981143935\\ tsp\_problemsell51.tsp.gz:\ 750.0-426.0-1.7605633802816902\\ tsp\_problemsd657.tsp.gz:\ 84982.0-48912.0-1.737446843310435
```

### SAT Solver

For sat solvers the dpll runtimes varied dramatically. Unsatisfiable problems took significantly longer then satisfiable problems as they had to check every possible combination of variables. GSAT took a pretty constant time to run as every time it was run with 100 tries and 100 flips for each try. Randomized

rounding saw its runtimes increased with numver of clauses as expected but remained incredibly fast.

In terms of clause satisfaction, DPLL returned either 0 for unsatisfiable problem or 1 for completely satisfied. GSAT and Randomized Rounding were consistently able to satisfy upwards of 90% of the clauses.

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#### Generating test cases with 32 variables...

Running benchmarks...

Benchmarking with 16 clauses... DPLL-32-vars/16 clauses: 0.882 ms DPLL-32-vars/16 clauses: 4.7e-2 ms

DPLL-32-vars/16 clauses: 4.50000000000000005e-2 ms

DPLL-32-vars/16 clauses: 6.1e-2 ms DPLL-32-vars/16 clauses: 4.7e-2 ms

GSAT-32-vars/16 clauses: 35.429 ms

GSAT-32-vars/16 clauses: 31.9470000000000000 ms

GSAT-32-vars/16 clauses: 40.659 ms

Randomized-Rounding-32-vars/16 clauses:  $0.153~\mathrm{ms}$  Randomized-Rounding-32-vars/16 clauses:  $9.2\mathrm{e}\text{-}2~\mathrm{ms}$  Randomized-Rounding-32-vars/16 clauses:  $8.0\mathrm{e}\text{-}2~\mathrm{ms}$  Randomized-Rounding-32-vars/16 clauses:  $7.4\mathrm{e}\text{-}2~\mathrm{ms}$  Randomized-Rounding-32-vars/16 clauses:  $8.2\mathrm{e}\text{-}2~\mathrm{ms}$ 

Average time for 16 clauses:

DPLL: 0.2164 ms

GSAT: 33.8002000000000004 ms Randomized Rounding: 9.62e-2 ms

Average clause satisfaction:

DPLL: 1.0 GSAT: 0.9625

Randomized Rounding:1.0

Individual Problem Clause Satisfactions:

DPLL: [1.0,1.0,1.0,1.0,1.0]

GSAT: [1.0,1.0,0.9375,1.0,0.875]

Randomized Rounding:[1.0,1.0,1.0,1.0,1.0]

Benchmarking with 32 clauses...

DPLL-32-vars/32 clauses: 0.747 ms

DPLL-32-vars/32 clauses: 9.3e-2 ms DPLL-32-vars/32 clauses: 7.6e-2 ms

DPLL-32-vars/32 clauses: 8.0e-2 ms  $\,$ 

DPLL-32-vars/32 clauses: 1.278 ms GSAT-32-vars/32 clauses: 61.439 ms

GSAT-32-vars/32 clauses: 51.49 ms

GSAT-32-vars/32 clauses: 67.028 ms

GSAT-32-vars/32 clauses: 69.155 ms

Average time for 32 clauses:

DPLL: 0.4548 ms GSAT: 63.1816 ms

Average clause satisfaction:

DPLL: 1.0 GSAT: 0.95

Randomized Rounding:0.99375

Individual Problem Clause Satisfactions:

DPLL: [1.0,1.0,1.0,1.0,1.0]

GSAT: [0.96875,1.0,0.9375,0.90625,0.9375] Randomized Rounding: [0.96875,1.0,1.0,1.0,1.0]

Benchmarking with 48 clauses... DPLL-32-vars/48 clauses: 0.219 ms

DPLL-32-vars/48 clauses: 0.138999999999999 ms

DPLL-32-vars/48 clauses: 0.254 ms DPLL-32-vars/48 clauses: 0.242 ms DPLL-32-vars/48 clauses: 94.821 ms GSAT-32-vars/48 clauses: 95.959 ms GSAT-32-vars/48 clauses: 74.661 ms GSAT-32-vars/48 clauses: 98.428 ms GSAT-32-vars/48 clauses: 92.166 ms GSAT-32-vars/48 clauses: 81.239 ms

Randomized-Rounding-32-vars/48 clauses: 0.187 ms Randomized-Rounding-32-vars/48 clauses: 0.212 ms Randomized-Rounding-32-vars/48 clauses: 0.289 ms

Average time for 48 clauses: DPLL: 19.1349999999999 ms

GSAT: 88.4906 ms

Randomized Rounding:0.2346 ms

Average clause satisfaction:

DPLL: 1.0

GSAT: 0.954166666666666

 $Randomized\ Rounding: 0.995833333333333333$ 

Individual Problem Clause Satisfactions:

DPLL: [1.0,1.0,1.0,1.0,1.0]

GSAT: [0.9375,1.0,0.91666666666666666,0.9375,0.9791666666666666]

Randomized Rounding:[1.0,1.0,0.97916666666666666,1.0,1.0]

Benchmarking with 64 clauses... DPLL-32-vars/64 clauses: 0.17 ms DPLL-32-vars/64 clauses: 2.904 ms DPLL-32-vars/64 clauses: 1.175 ms DPLL-32-vars/64 clauses: 23.757 ms

GSAT-32-vars/64 clauses: 131.994 ms GSAT-32-vars/64 clauses: 139.638 ms GSAT-32-vars/64 clauses: 107.107 ms GSAT-32-vars/64 clauses: 110.901 ms

Randomized-Rounding-32-vars/64 clauses: 0.428 ms Randomized-Rounding-32-vars/64 clauses: 0.328 ms Randomized-Rounding-32-vars/64 clauses: 0.296 ms Randomized-Rounding-32-vars/64 clauses: 0.251 ms

Randomized-Rounding-32-vars/64 clauses: 0.335999999999999 ms

Average time for 64 clauses:

DPLL: 5.6358 ms GSAT: 120.4598 ms

Randomized Rounding:0.3278 ms Average clause satisfaction:

DPLL: 1.0 GSAT: 0.94375

Randomized Rounding:0.978125

Individual Problem Clause Satisfactions:

DPLL: [1.0,1.0,1.0,1.0,1.0]

 $\begin{aligned} & \text{GSAT:} \; [0.96875, 0.90625, 0.890625, 0.984375, 0.96875] \\ & \text{Randomized Rounding:} [1.0, 0.96875, 1.0, 1.0, 0.921875] \end{aligned}$ 

Benchmarking with 80 clauses...

DPLL-32-vars/80 clauses: 9.506 ms

DPLL-32-vars/80 clauses: 1061.566 ms DPLL-32-vars/80 clauses: 33.116 ms GSAT-32-vars/80 clauses: 175.507 ms GSAT-32-vars/80 clauses: 136.125 ms GSAT-32-vars/80 clauses: 168.984 ms GSAT-32-vars/80 clauses: 209.985 ms

Randomized-Rounding-32-vars/80 clauses: 0.4929999999999999 ms

Randomized-Rounding-32-vars/80 clauses: 0.352 ms Randomized-Rounding-32-vars/80 clauses: 0.389 ms Randomized-Rounding-32-vars/80 clauses: 0.61 ms

Average time for 80 clauses:

DPLL: 235.4172 ms

GSAT: 166.115799999999998 ms

Average clause satisfaction:

DPLL: 1.0

GSAT: 0.9324999999999999

Randomized Rounding: 0.9574999999999999

Individual Problem Clause Satisfactions:

DPLL: [1.0,1.0,1.0,1.0,1.0]

GSAT: [0.8875,0.975,0.975,0.9,0.925]

Randomized Rounding: [0.95,1.0,0.975,0.9125,0.95]

Benchmarking with 96 clauses...
DPLL-32-vars/96 clauses: 5.178 ms
DPLL-32-vars/96 clauses: 150.953 ms
DPLL-32-vars/96 clauses: 21.064 ms
DPLL-32-vars/96 clauses: 0.519 ms

DPLL-32-vars/96 clauses: 5456.076999999999 ms

GSAT-32-vars/96 clauses: 157.202 ms GSAT-32-vars/96 clauses: 149.988 ms GSAT-32-vars/96 clauses: 161.729 ms

GSAT-32-vars/96 clauses: 200.02900000000000 ms

GSAT-32-vars/96 clauses: 167.922 ms

Randomized-Rounding-32-vars/96 clauses: 0.513 ms Randomized-Rounding-32-vars/96 clauses: 0.636 ms

Randomized-Rounding-32-vars/96 clauses: 0.524 ms

Average time for 96 clauses:

DPLL: 1126.7582 ms GSAT: 167.374 ms

Randomized Rounding: $0.5352~\mathrm{ms}$ 

Average clause satisfaction:

DPLL: 1.0 GSAT: 0.9625

#### Randomized Rounding:0.925

Individual Problem Clause Satisfactions:

DPLL: [1.0,1.0,1.0,1.0,1.0]

Benchmarking with 112 clauses...

DPLL-32-vars/112 clauses: 3843.378 ms DPLL-32-vars/112 clauses: 25.213 ms DPLL-32-vars/112 clauses: 152.993 ms DPLL-32-vars/112 clauses: 6.569 ms

DPLL-32-vars/112 clauses: 300.78700000000000 ms

GSAT-32-vars/112 clauses: 220.592 ms GSAT-32-vars/112 clauses: 223.528 ms GSAT-32-vars/112 clauses: 204.514 ms

GSAT-32-vars/112 clauses: 190.021 ms

Randomized-Rounding-32-vars/112 clauses: 0.709 ms Randomized-Rounding-32-vars/112 clauses: 0.636 ms

Randomized-Rounding-32-vars/112 clauses: 0.617 ms Randomized-Rounding-32-vars/112 clauses: 0.656 ms

Average time for 112 clauses: DPLL: 865.7880000000001 ms GSAT: 215.00300000000001 ms Randomized Rounding:0.6794 ms Average clause satisfaction:

DPLL: 0.8

GSAT: 0.9285714285714285 Randomized Rounding:0.9125

Individual Problem Clause Satisfactions:

DPLL: [0.0,1.0,1.0,1.0,1.0]

Benchmarking with 128 clauses...

DPLL-32-vars/128 clauses: 121.8579999999999 ms

DPLL-32-vars/128 clauses: 1739.051 ms

DPLL-32-vars/128 clauses: 360.153 ms GSAT-32-vars/128 clauses: 255.803 ms

GSAT-32-vars/128 clauses: 217.31 ms GSAT-32-vars/128 clauses: 226.433 ms GSAT-32-vars/128 clauses: 249.277 ms GSAT-32-vars/128 clauses: 253.206 ms

Randomized-Rounding-32-vars/128 clauses: 0.9840000000000001 ms

Randomized-Rounding-32-vars/128 clauses: 0.726 ms Randomized-Rounding-32-vars/128 clauses: 0.848 ms Randomized-Rounding-32-vars/128 clauses: 0.876 ms

Randomized-Rounding-32-vars/128 clauses: 0.6920000000000001 ms

Average time for 128 clauses:

DPLL: 1610.5762 ms GSAT: 240.4058 ms

Randomized Rounding:0.8252 ms  $\,$ 

Average clause satisfaction:

DPLL: 0.6

GSAT: 0.9359375

Randomized Rounding:0.9203125

Individual Problem Clause Satisfactions:

DPLL: [1.0,1.0,0.0,0.0,1.0]

GSAT: [0.921875,0.96875,0.953125,0.921875,0.9140625]

 $Randomized\ Rounding: [0.90625, 0.90625, 0.9296875, 0.953125, 0.90625]$ 

Benchmarking with 144 clauses...

DPLL-32-vars/144 clauses: 235.2509999999999 ms DPLL-32-vars/144 clauses: 1103.305999999999 ms DPLL-32-vars/144 clauses: 1473.419999999999 ms

DPLL-32-vars/144 clauses: 1116.245 ms DPLL-32-vars/144 clauses: 57.836 ms GSAT-32-vars/144 clauses: 251.973 ms

GSAT-32-vars/144 clauses: 253.41200000000003 ms

GSAT-32-vars/144 clauses: 237.662 ms GSAT-32-vars/144 clauses: 248.292 ms GSAT-32-vars/144 clauses: 288.089 ms

Randomized-Rounding-32-vars/144 clauses: 1.0150000000000001 ms

Randomized-Rounding-32-vars/144 clauses:  $1.014~\mathrm{ms}$  Randomized-Rounding-32-vars/144 clauses:  $0.923~\mathrm{ms}$  Randomized-Rounding-32-vars/144 clauses:  $1.067~\mathrm{ms}$ 

Average time for 144 clauses:

DPLL: 797.2116 ms GSAT: 255.8856 ms

Average clause satisfaction:

DPLL: 0.6

GSAT: 0.954166666666666

Randomized Rounding: 0.926388888888889

Individual Problem Clause Satisfactions:

DPLL: [1.0,1.0,0.0,0.0,1.0]

 $Randomized\ Rounding: [0.94444444444444444444, 0.930555555555556, 0.944444444444444, 0.875, 0.9375]$ 

Benchmarking with 160 clauses...

DPLL-32-vars/160 clauses: 1964.972 ms DPLL-32-vars/160 clauses: 528.207 ms DPLL-32-vars/160 clauses: 753.749 ms DPLL-32-vars/160 clauses: 335.703 ms DPLL-32-vars/160 clauses: 397.697 ms

GSAT-32-vars/160 clauses: 268.383 ms GSAT-32-vars/160 clauses: 308.187 ms GSAT-32-vars/160 clauses: 338.716 ms GSAT-32-vars/160 clauses: 336.769 ms

Randomized-Rounding-32-vars/160 clauses: 1.383 ms Randomized-Rounding-32-vars/160 clauses: 0.934 ms Randomized-Rounding-32-vars/160 clauses: 1.346 ms Randomized-Rounding-32-vars/160 clauses: 1.365 ms Randomized-Rounding-32-vars/160 clauses: 1.119 ms

Average time for 160 clauses:

DPLL: 796.0656 ms

GSAT: 322.3300000000000004 ms

Randomized Rounding:1.229399999999998 ms

Average clause satisfaction:

**DPLL**: 0.2

Individual Problem Clause Satisfactions:

DPLL: [0.0,1.0,0.0,0.0,0.0]

GSAT: [0.86875,0.96875,0.93125,0.8875,0.89375]

Randomized Rounding: [0.9, 0.98125, 0.8875, 0.88125, 0.925]

Benchmarking with 176 clauses...

DPLL-32-vars/176 clauses: 681.767 ms DPLL-32-vars/176 clauses: 1251.112 ms

DPLL-32-vars/176 clauses: 171.1979999999999 ms DPLL-32-vars/176 clauses: 635.237999999999 ms

DPLL-32-vars/176 clauses: 1953.365 ms

GSAT-32-vars/176 clauses: 369.99100000000000 ms GSAT-32-vars/176 clauses: 408.275999999999 ms

GSAT-32-vars/176 clauses: 404.742 ms GSAT-32-vars/176 clauses: 877.287 ms GSAT-32-vars/176 clauses: 461.234 ms

Randomized-Rounding-32-vars/176 clauses: 5.008 ms Randomized-Rounding-32-vars/176 clauses: 5.834 ms

Randomized-Rounding-32-vars/176 clauses: 2.05000000000000000 ms Randomized-Rounding-32-vars/176 clauses: 2.546999999999999 ms

Randomized-Rounding-32-vars/176 clauses: 1.881 ms

Average time for 176 clauses: DPLL: 938.5360000000001 ms GSAT: 504.305999999999 ms Randomized Rounding:3.464 ms Average clause satisfaction:

DPLL: 0.0 GSAT: 0.925

Randomized Rounding: 0.9068181818181819

Individual Problem Clause Satisfactions:

DPLL: [0.0,0.0,0.0,0.0,0.0]

Benchmarking with 192 clauses...

DPLL-32-vars/192 clauses: 222.199 ms DPLL-32-vars/192 clauses: 1451.341 ms DPLL-32-vars/192 clauses: 1615.375 ms DPLL-32-vars/192 clauses: 6137.663 ms DPLL-32-vars/192 clauses: 233.73 ms GSAT-32-vars/192 clauses: 427.745 ms GSAT-32-vars/192 clauses: 388.444 ms GSAT-32-vars/192 clauses: 395.62 ms GSAT-32-vars/192 clauses: 437.53 ms

GSAT-32-vars/192 clauses: 400.96500000000000 ms

Randomized-Rounding-32-vars/192 clauses: 1.704999999999999 ms

Randomized-Rounding-32-vars/192 clauses: 1.474 ms Randomized-Rounding-32-vars/192 clauses: 1.673 ms Randomized-Rounding-32-vars/192 clauses: 1.846 ms Randomized-Rounding-32-vars/192 clauses: 1.717 ms

Average time for 192 clauses: DPLL: 1932.06160000000002 ms GSAT: 410.060800000000003 ms

Randomized Rounding:1.683000000000000 ms

Average clause satisfaction:

**DPLL:** 0.0

GSAT: 0.894791666666668

Randomized Rounding: 0.88958333333333334

Individual Problem Clause Satisfactions:

DPLL: [0.0,0.0,0.0,0.0,0.0]

GSAT: [0.875, 0.911458333333334, 0.90625, 0.864583333333334, 0.9166666666666666]

Benchmarking with 208 clauses...

DPLL-32-vars/208 clauses: 712.27 ms

DPLL-32-vars/208 clauses: 799.8340000000001 ms

DPLL-32-vars/208 clauses: 1034.313 ms

DPLL-32-vars/208 clauses: 1506.1970000000001 ms

DPLL-32-vars/208 clauses: 453.745 ms GSAT-32-vars/208 clauses: 397.515 ms GSAT-32-vars/208 clauses: 446.038 ms GSAT-32-vars/208 clauses: 384.513 ms GSAT-32-vars/208 clauses: 376.902 ms GSAT-32-vars/208 clauses: 454.65 ms

Randomized-Rounding-32-vars/208 clauses: 1.916 ms

Randomized-Rounding-32-vars/208 clauses: 1.8940000000000001 ms

Randomized-Rounding-32-vars/208 clauses: 1.764 ms Randomized-Rounding-32-vars/208 clauses: 2.053 ms

Average time for 208 clauses: DPLL: 901.2717999999999 ms GSAT: 411.9235999999996 ms Randomized Rounding:1.92 ms Average clause satisfaction:

DPLL: 0.0 GSAT: 0.925

Randomized Rounding: 0.8971153846153845

Individual Problem Clause Satisfactions:

DPLL: [0.0,0.0,0.0,0.0,0.0]

 $GSAT: [0.9567307692307693, 0.8894230769230769, 0.9471153846153846, 0.9471153846153846, 0.8846153846153846153846] \\ Randomized Rounding: [0.8846153846153846, 0.875, 0.9134615384615384, 0.9038461538461538461539, 0.908653846153846] \\ Randomized Rounding: [0.8846153846153846, 0.875, 0.9134615384615384, 0.9038461538461539, 0.908653846153846] \\ Randomized Rounding: [0.8846153846153846, 0.875, 0.91346153846, 0.903846153846, 0.903846153846] \\ Randomized Rounding: [0.8846153846, 0.875, 0.91346153846, 0.903846153846, 0.903846153846] \\ Randomized Rounding: [0.8846153846, 0.875, 0.91346153846, 0.903846153846, 0.903846] \\ Randomized Rounding: [0.8846153846, 0.875, 0.91346153846, 0.903846] \\ Randomized Rounding: [0.8846153846, 0.875, 0.91346153846, 0.903846] \\ Randomized Rounding: [0.8846153846, 0.875, 0.91346] \\ Randomized Rounding: [0.884615384, 0.903846] \\ Randomized Rounding: [0$ 

Benchmarking with 224 clauses...

DPLL-32-vars/224 clauses: 841.634 ms DPLL-32-vars/224 clauses: 554.037 ms DPLL-32-vars/224 clauses: 752.386 ms DPLL-32-vars/224 clauses: 505.834 ms DPLL-32-vars/224 clauses: 1067.58 ms

 $\begin{array}{l} {\rm GSAT\text{-}32\text{-}vars/224\ clauses:\ 431.404\ ms} \\ {\rm GSAT\text{-}32\text{-}vars/224\ clauses:\ 372.976\ ms} \\ {\rm GSAT\text{-}32\text{-}vars/224\ clauses:\ 400.155\ ms} \\ {\rm GSAT\text{-}32\text{-}vars/224\ clauses:\ 494.291\ ms} \end{array}$ 

Randomized-Rounding-32-vars/224 clauses: 2.07999999999999 ms

Randomized-Rounding-32-vars/224 clauses: 2.285 ms

Randomized-Rounding-32-vars/224 clauses: 2.055 ms Randomized-Rounding-32-vars/224 clauses: 2.236 ms

Average time for 224 clauses:

DPLL: 744.2942 ms

GSAT: 430.45920000000007 ms

Randomized Rounding:2.127799999999997 ms

Average clause satisfaction:

**DPLL:** 0.0

GSAT: 0.9303571428571427

Randomized Rounding: 0.9044642857142857

Individual Problem Clause Satisfactions:

DPLL: [0.0,0.0,0.0,0.0,0.0]

GSAT: [0.9151785714285714, 0.9285714285714286, 0.9776785714285714, 0.9553571428571429, 0.875]

Benchmarking with 240 clauses...

DPLL-32-vars/240 clauses: 900.899 ms DPLL-32-vars/240 clauses: 739.272 ms

DPLL-32-vars/240 clauses: 337.792 ms DPLL-32-vars/240 clauses: 80.281 ms GSAT-32-vars/240 clauses: 431.562 ms GSAT-32-vars/240 clauses: 499.437 ms GSAT-32-vars/240 clauses: 490.631 ms GSAT-32-vars/240 clauses: 446.737 ms GSAT-32-vars/240 clauses: 449.322 ms

Randomized-Rounding-32-vars/240 clauses: 2.20099999999999 ms

Randomized-Rounding-32-vars/240 clauses: 2.536 ms

Randomized-Rounding-32-vars/240 clauses: 2.5370000000000000 ms

Randomized-Rounding-32-vars/240 clauses: 2.536 ms

Randomized-Rounding-32-vars/240 clauses: 2.308000000000000 ms

Average time for 240 clauses:

DPLL: 429.4014 ms

GSAT: 463.53780000000006 ms Randomized Rounding: 2.4236 ms

Average clause satisfaction:

**DPLL:** 0.0

GSAT: 0.9258333333333333

 $Randomized\ Rounding: 0.88666666666666667$ 

Individual Problem Clause Satisfactions:

DPLL: [0.0,0.0,0.0,0.0,0.0]

Benchmarking with 256 clauses...

DPLL-32-vars/256 clauses: 103.377 ms

DPLL-32-vars/256 clauses: 1968.0089999999998 ms

DPLL-32-vars/256 clauses: 1151.271 ms DPLL-32-vars/256 clauses: 240.445 ms

DPLL-32-vars/256 clauses: 251.1709999999999 ms

GSAT-32-vars/256 clauses: 596.701 ms

GSAT-32-vars/256 clauses: 556.8610000000001 ms

GSAT-32-vars/256 clauses: 474.779 ms GSAT-32-vars/256 clauses: 472.223 ms

GSAT-32-vars/256 clauses: 636.7230000000001 ms Randomized-Rounding-32-vars/256 clauses: 2.721 ms Randomized-Rounding-32-vars/256 clauses: 3.42 ms Randomized-Rounding-32-vars/256 clauses: 3.199 ms Randomized-Rounding-32-vars/256 clauses: 2.679 ms

Randomized-Rounding-32-vars/256 clauses: 2.837999999999999 ms

Average time for 256 clauses:

DPLL: 742.8546 ms GSAT: 547.4574 ms

Randomized Rounding:2.9714 ms

Average clause satisfaction:

DPLL: 0.0 GSAT: 0.915625

Randomized Rounding:0.89453125

Individual Problem Clause Satisfactions:

DPLL: [0.0,0.0,0.0,0.0,0.0]

GSAT: [0.89453125,0.8828125,0.94140625,0.94140625,0.91796875]

Randomized Rounding: [0.9140625, 0.88671875, 0.8984375, 0.87890625, 0.89453125]