

CAN304

Computer Systems Security

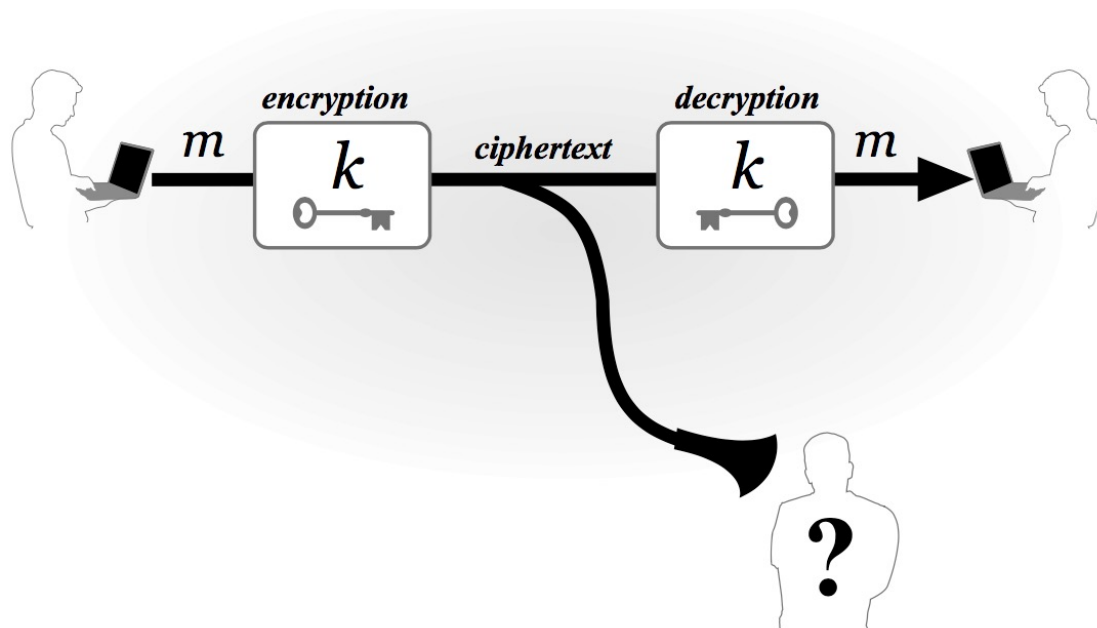
Lecture 3. Fundamentals of cryptography (2)

Week 3: 2024-03-12, 14:00-15:50, Tuesday

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Review of last week

- Classical and modern cryptography
- Symmetric encryption
 - Block ciphers
 - Cryptographic modes
 - Uses of symmetric cryptography



Learning objectives

- Discuss the use of secure hash functions for message authentication.
- List other applications of secure hash functions.
- Apply secure hash functions in security design and implementations.

Outline

- Message authentication code
- Hash functions and applications

1. Message authentication code

- Message integrity
- Fixed-length MAC
- CBC-MAC
- Secure communications

1.1 Message integrity

Confidentiality vs. integrity

- So far, we have been concerned with ensuring confidentiality of communication
- What about integrity?
 - I.e., ensuring that a received message originated from the intended party, and was not modified, even if an attacker controls the channel!



A

{transfer \$100 to Jie's account}_k



- Is the request issued by A?
- Are the details of the request exactly those intended by A?



How MAC works?



m, t

m, t



m
 $t = \text{Mac}_k(m)$

$\text{Vrfy}_k(m, t) = 1?$

Confidentiality vs. integrity

- Confidentiality and integrity are orthogonal concerns
 - Possible to have either one without the other
- Encryption can help to discover alteration.
 - If the decrypted message is meaningless, unreadable
 - But is not the purpose of encryption.

Message authentication code (MAC)

- A message authentication code is defined by three algorithms (Gen, Mac, Vrfy):
 - Gen: generates a random key k .
 - Mac: takes as input key k and message $m \in \{0,1\}^*$; outputs tag t
$$t := \text{Mac}_k(m)$$
 - Vrfy: takes key k , message m , and tag t as input; outputs 1 (“accept”) or 0 (“reject”)

For all m and all k output by Gen,
$$\text{Vrfy}_k(m, \text{Mac}_k(m)) = 1$$

1.2 Fixed-length MAC

Intuition?

- We need a keyed function Mac such that
 - Given $\text{Mac}_k(m_1), \text{Mac}_k(m_2), \dots,$
 - ...it is infeasible to predict the value $\text{Mac}_k(m)$ for any $m \notin \{m_1, \dots, \}$ without k
- Let Mac be a block cipher

Construction

- Let F be a block cipher
- Construct the following MAC Π :
 - Gen: choose a uniform key k for F
 - $\text{Mac}_k(m)$: output $t \leftarrow F_k(m)$
 - $\text{Vrfy}_k(m, t)$: output 1 iff $F_k(m) = t$

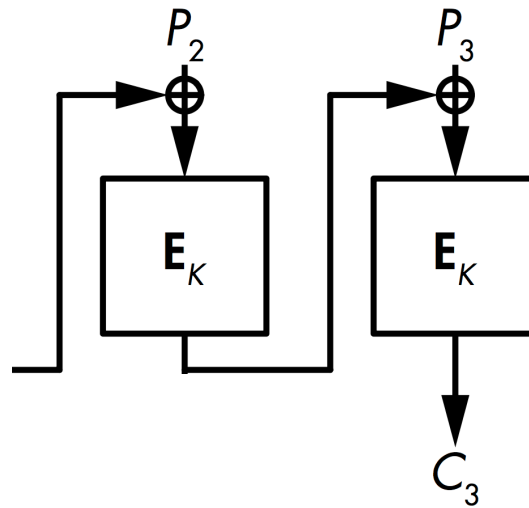
Drawbacks?

- In practice, block ciphers have short, fixed-length block size
 - E.g., AES has a 128-bit block size
 - So the previous construction is limited to authenticating short, fixed-length messages
- Next few parts: authenticating long, variable length messages

1.3 CBC-MAC

Recall CBC mode

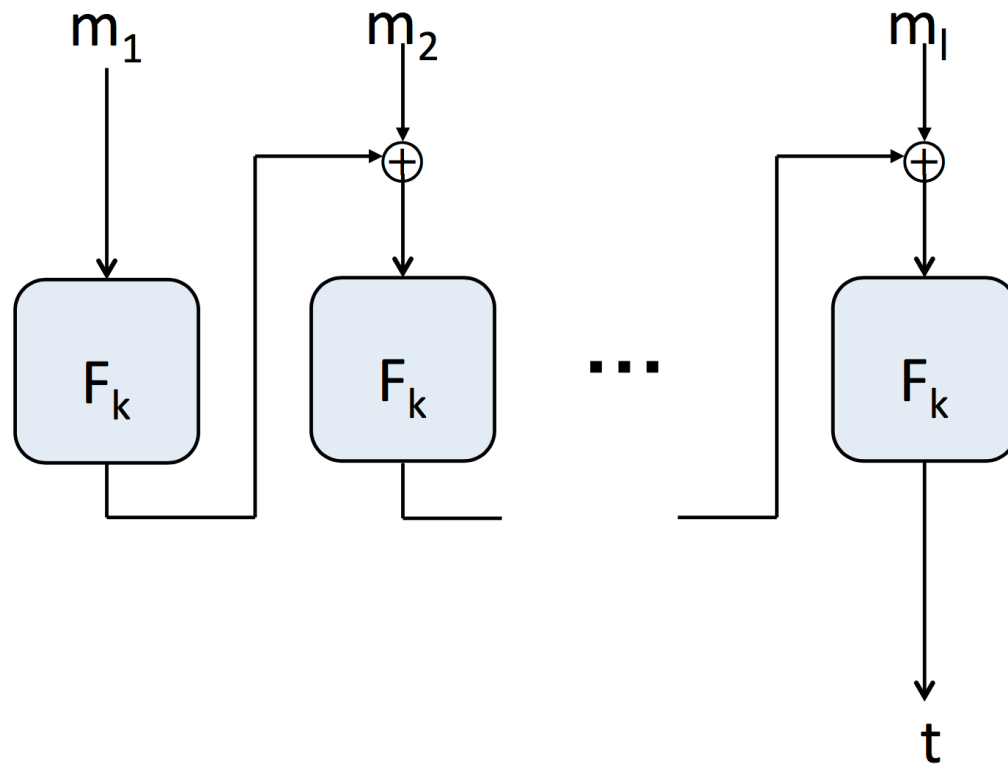
- For block $X+1$, XOR the plaintext with the ciphertext of block X
 - Then encrypt the result
- Each block's encryption depends on **all** previous blocks' contents



- What if we only output the last ciphertext block?

(Basic) CBC-MAC

- $m = m_1 m_2 \dots m_l$

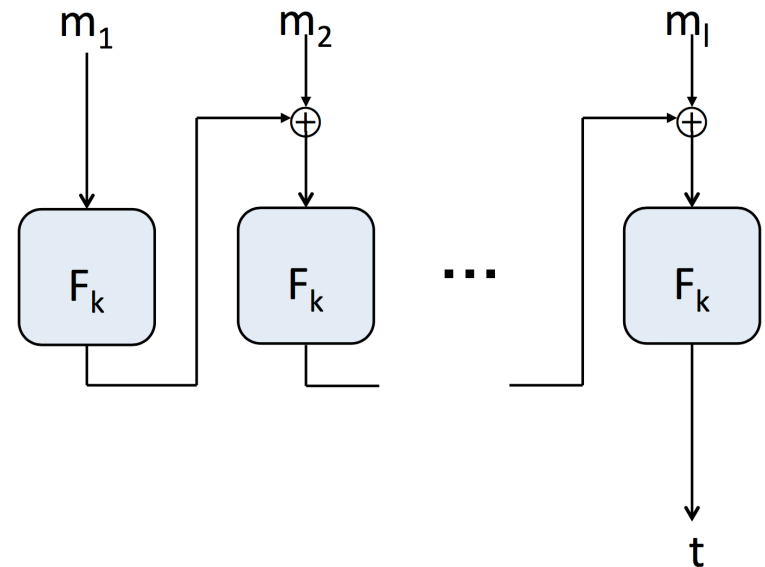
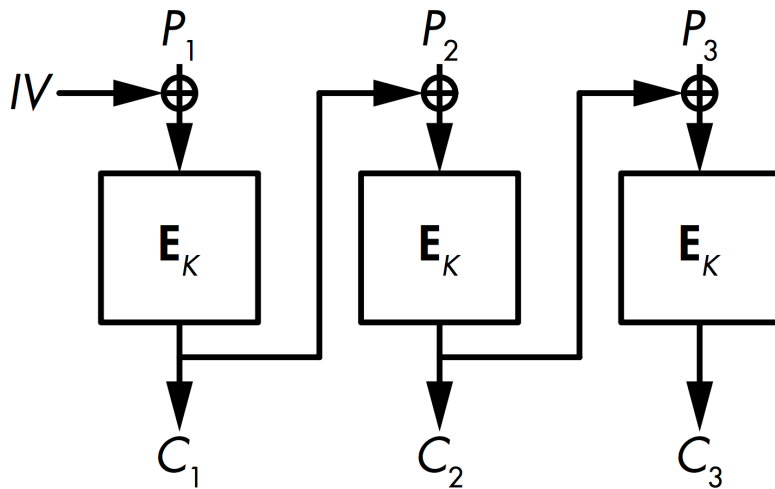


CBC-MAC vs. CBC-mode encryption

- CBC-MAC is deterministic (no IV)
- In CBC-MAC, only the final value is output
 - Verification is done by re-computing the result
- Both of these are essential for security

Can I recover the original data from its MAC tag?

- No

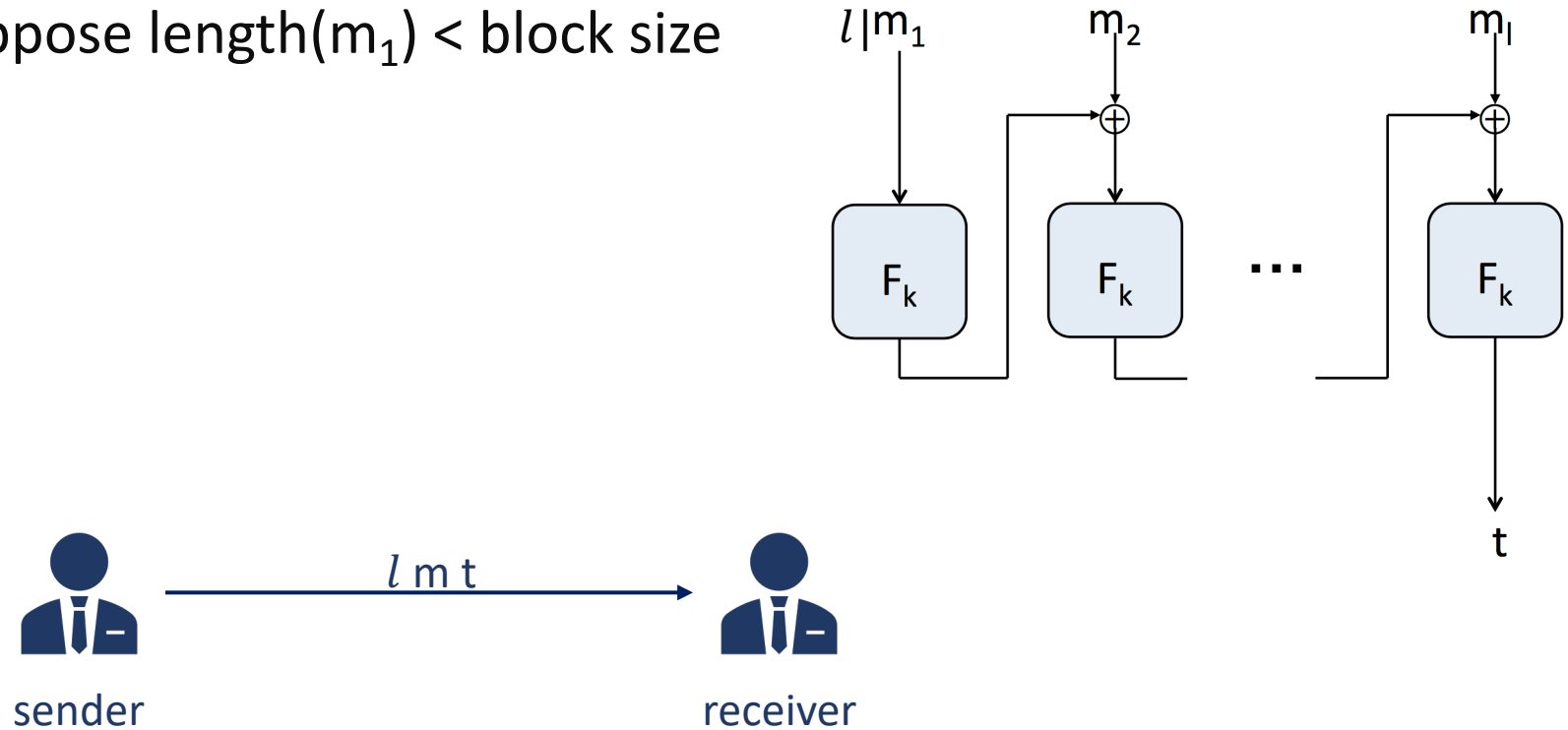


CBC-MAC extensions

- Several ways to handle variable length messages
 - Whose length is not a multiple of the block length
- One of the simplest: prepend the message length before applying (basic) CBC-MAC

CBC-MAC

- $m = m_1 m_2 \dots m_l$
- Suppose $\text{length}(m_1) < \text{block size}$



1.4 Secure communication

Confidentiality + integrity?

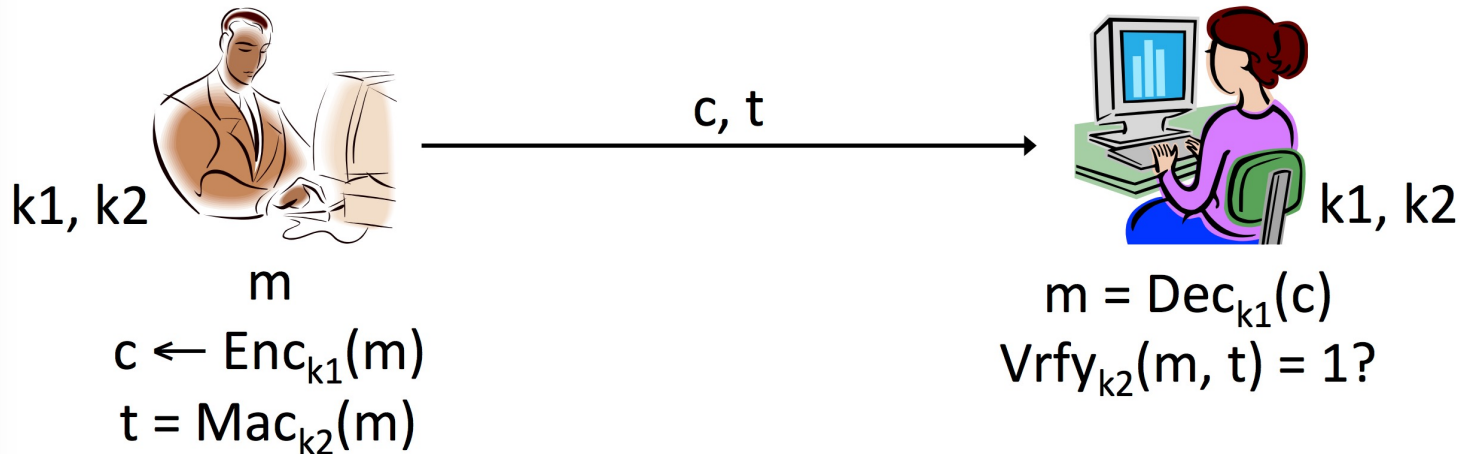
- We have shown primitives for achieving confidentiality and integrity in the private-key setting
- What if we want to achieve both?

Encrypt and authenticate

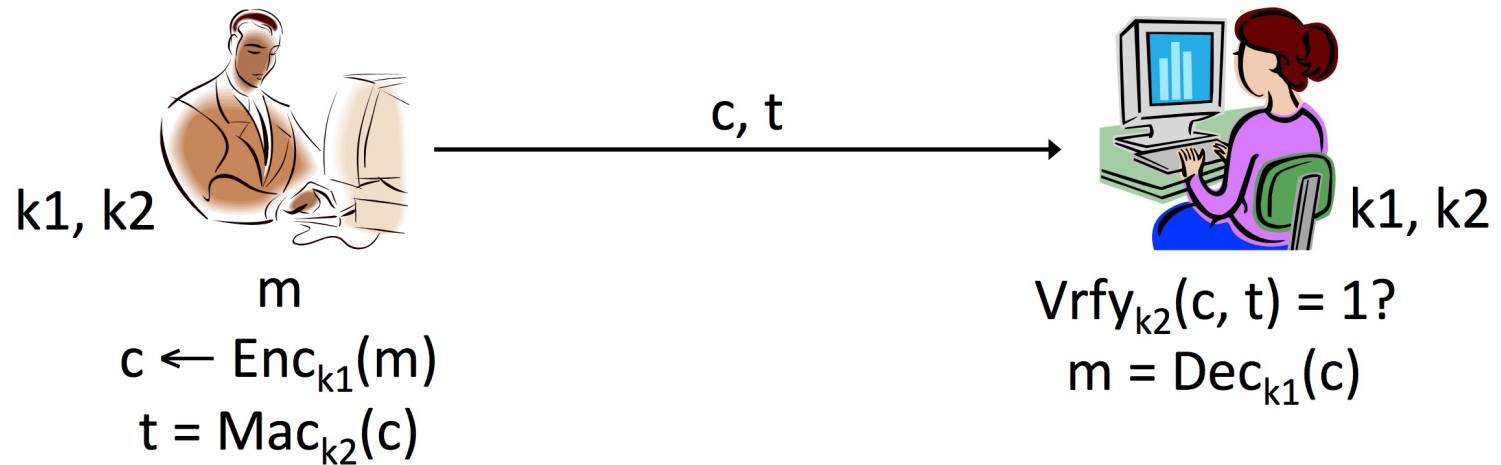


Problems

- The tag t might leak information about m !
 - Nothing in the definition of security for a MAC implies that it hides information about m
- If the MAC is deterministic (as is CBC-MAC), it leaks whether the same message is encrypted twice



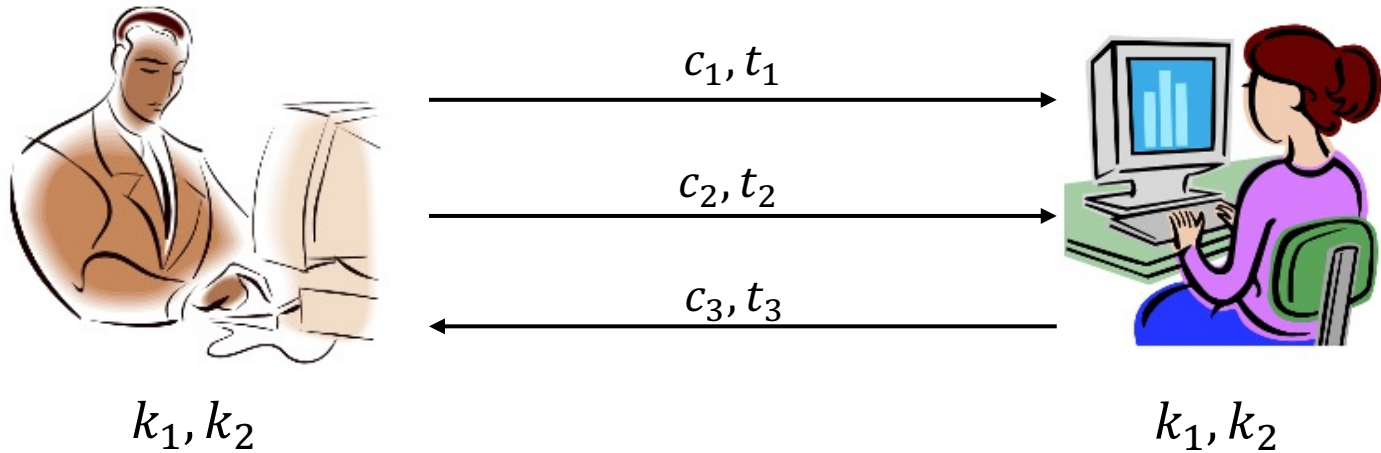
Encrypt then authenticate



Secure sessions

- Consider parties who wish to communicate securely over the course of a session
 - “Securely” = confidentiality and integrity
 - “Session” = period of time over which parties are willing to maintain state
- Can use authenticated encryption...

Any attacks?



$$c_1 = \text{Enc}_{k_1}(m_1),$$

$$t_1 = \text{MAC}_{k_2}(c_1)$$

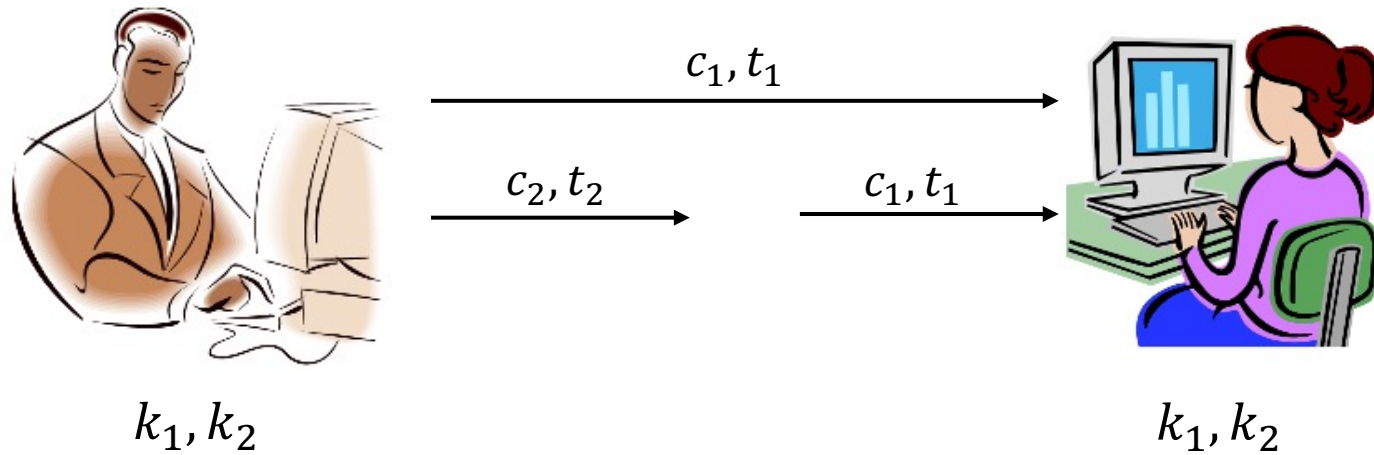
$$c_2 = \text{Enc}_{k_1}(m_2),$$

$$t_2 = \text{MAC}_{k_2}(c_2)$$

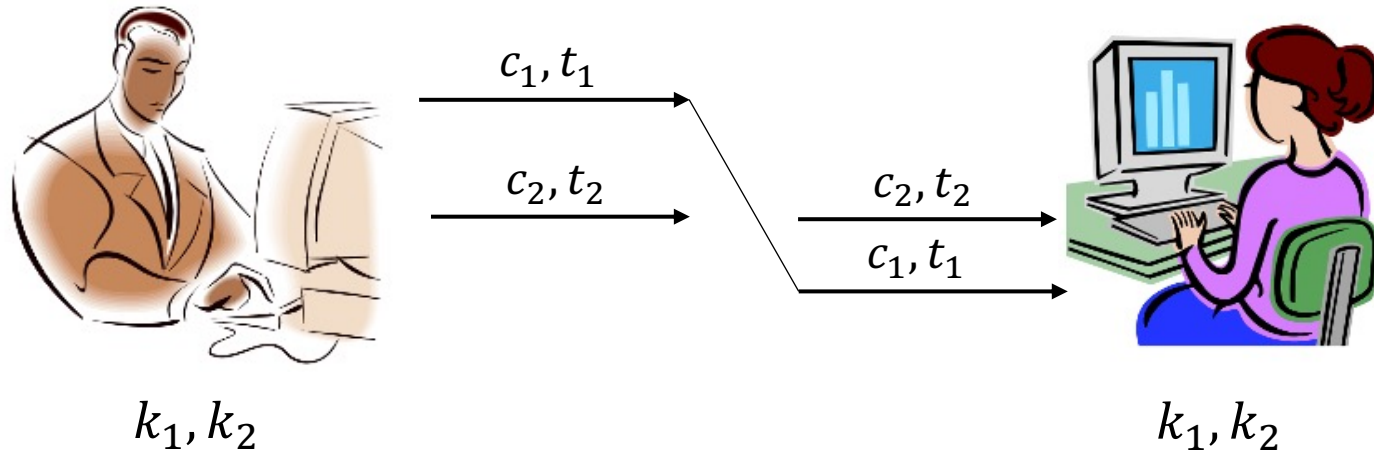
$$c_3 = \text{Enc}_{k_1}(m_3),$$

$$t_3 = \text{MAC}_{k_2}(c_3)$$

Replay attack

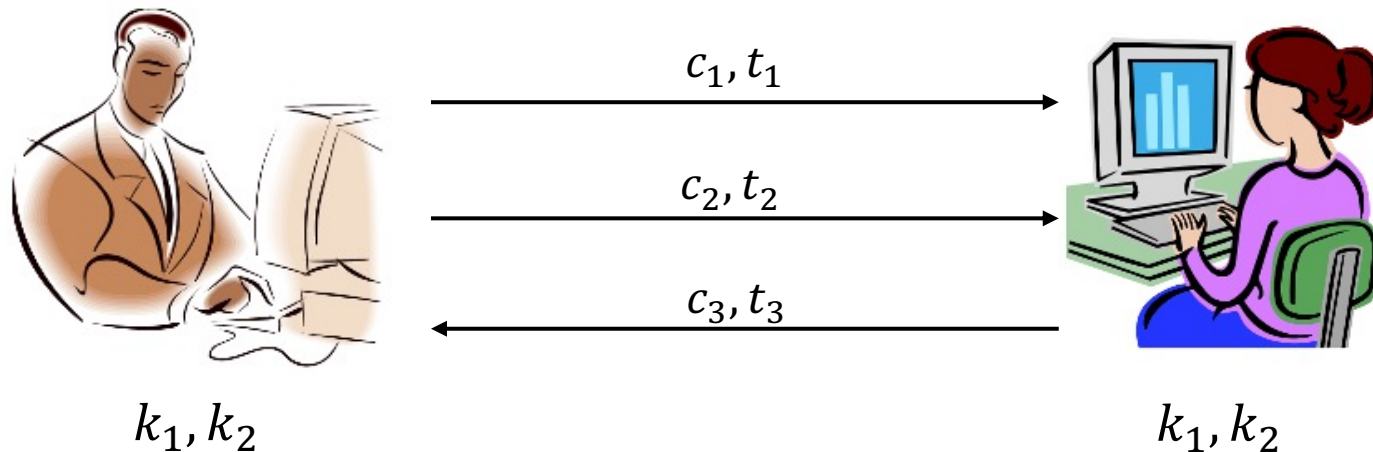


Re-ordering attack



Secure sessions

- These attacks (and others) can be prevented using counters and identities



$$c_1 = \text{Enc}_{k_1}(\text{"Bob"}|m_1|1),$$
$$t_1 = \text{MAC}_{k_2}(c_1)$$

$$c_2 = \text{Enc}_{k_1}(\text{"Bob"}|m_2|2),$$
$$t_2 = \text{MAC}_{k_2}(c_2)$$

$$c_3 = \text{Enc}_{k_1}(\text{"Alice"}|m_3|1),$$
$$t_3 = \text{MAC}_{k_2}(c_3)$$

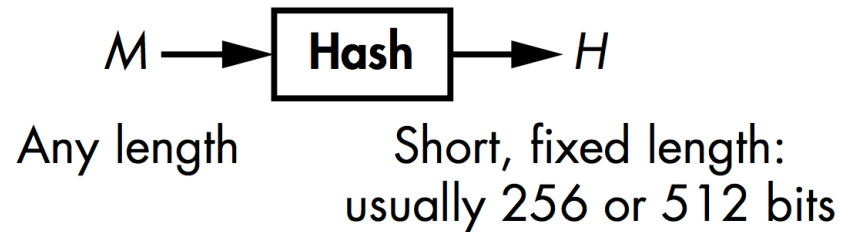
2. Hash functions and applications

- Hash functions
- HMAC
- Merkle tree
- Bitcoin

2.1 Hash functions

Hash functions

- (Cryptographic) hash function: maps arbitrary length inputs to a short, fixed-length **digest**



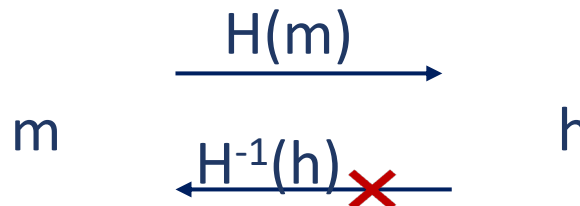
- Can define keyed or unkeyed hash functions
 - Formally, keyed hash functions are needed
 - In practice, hash functions are unkeyed
 - (We will work with unkeyed hash functions, and be less formal)

Properties of cryptographic hash functions

- Let $H: \{0,1\}^* \rightarrow \{0,1\}^n$ be a hash function
- Preimage resistance
 - one-way
- Second preimage resistance
 - weak collision resistant
- Collision resistance
 - strong collision resistance

Preimage resistance

- Let $H: \{0,1\}^* \rightarrow \{0,1\}^n$ be a hash function
- A preimage of a given hash value, h , is any message, M , such that
$$H(M) = h$$
- Preimage resistance
 - Given a random hash value, it is computationally infeasible to find a preimage of that hash value
 - One-way function



Second preimage resistance

- Let $H: \{0,1\}^* \rightarrow \{0,1\}^n$ be a hash function
- Given x , it is computationally infeasible to find $x' \neq x$ such that $H(x) = H(x')$
- Aka. weak collision resistant

Collision resistance

- Let $H: \{0,1\}^* \rightarrow \{0,1\}^n$ be a hash function
- A collision is a pair of distinct inputs x, x' such that $H(x) = H(x')$
- H is collision-resistant if it is computationally infeasible to find a collision in H .
- Aka. strong collision resistance.

Generic hash-function attacks

- What is the best “generic” collision attack on a hash function $H: \{0,1\}^* \rightarrow \{0,1\}^n$?
 - size of $\{0,1\}^*$: arbitrarily large
 - size of $\{0,1\}^n$: $2^n = 2 \times 2 \times \cdots \times 2$
- If we compute $H(x_1), \dots, H(x_{2^n+1})$, we are guaranteed to find a collision
 - Is it possible to do better?
 - guaranteed: 100%

“Birthday” attacks

- How many hashes do we need to compute to find a collision with a large probability, such as 50%?
- Related to the so-called birthday paradox
 - How many people are needed to have a 50% chance that some two people share a birthday?

Theorem

- When the number is $O(N^{1/2})$, the probability of a collision is 50%
 - Birthdays: 23 people suffice!
 - Hash functions: $O(2^{n/2})$ hash function-evaluations
 - much better than $2^n + 1$

Hash functions in practice

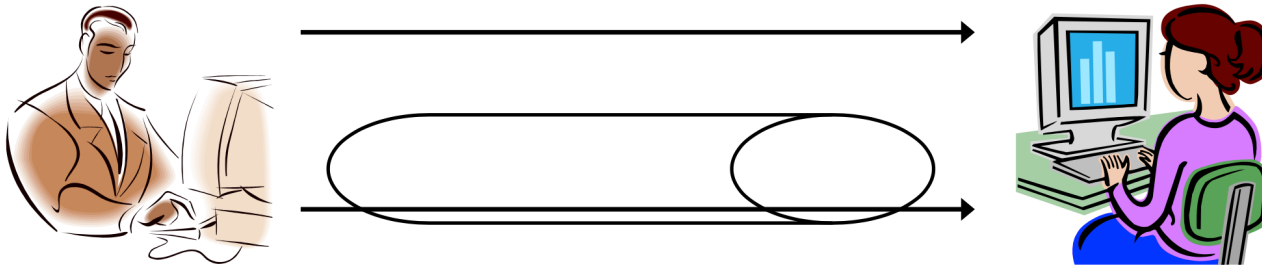
- MD5
 - Developed in 1991
 - 128-bit output length
 - Collisions found in 2004, should no longer be used
- SHA-1
 - Introduced in 1995
 - 160-bit output length
 - Theoretical analyses indicate some weaknesses
 - Very common; current trend to migrate to SHA-2

Hash functions in practice

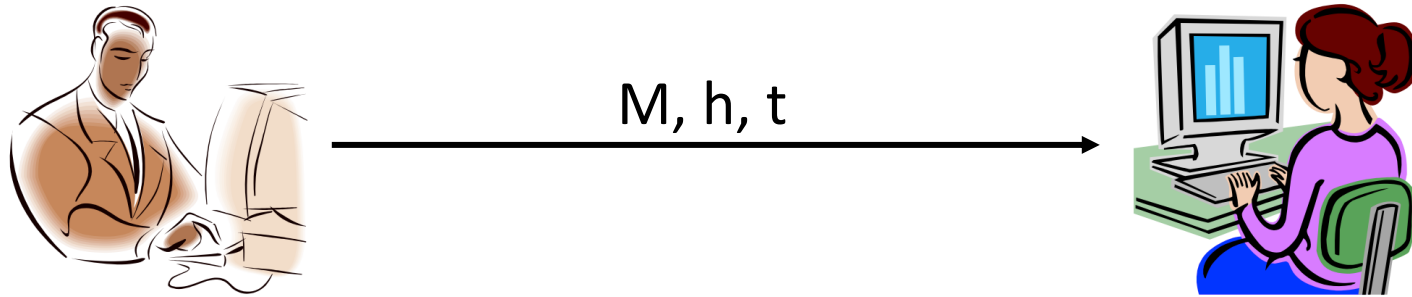
- SHA-2
 - 224-bit, 256-bit, 384-bit or 512-bit output lengths
 - No known significant weaknesses
- SHA-3/Keccak
 - Result of a public competition from 2008-2012
 - 64 submissions
 - 51 entered the first round
 - Very different design than SHA family
 - Supports 224, 256, 384, and 512-bit outputs

2.2 HMAC

Intuition...

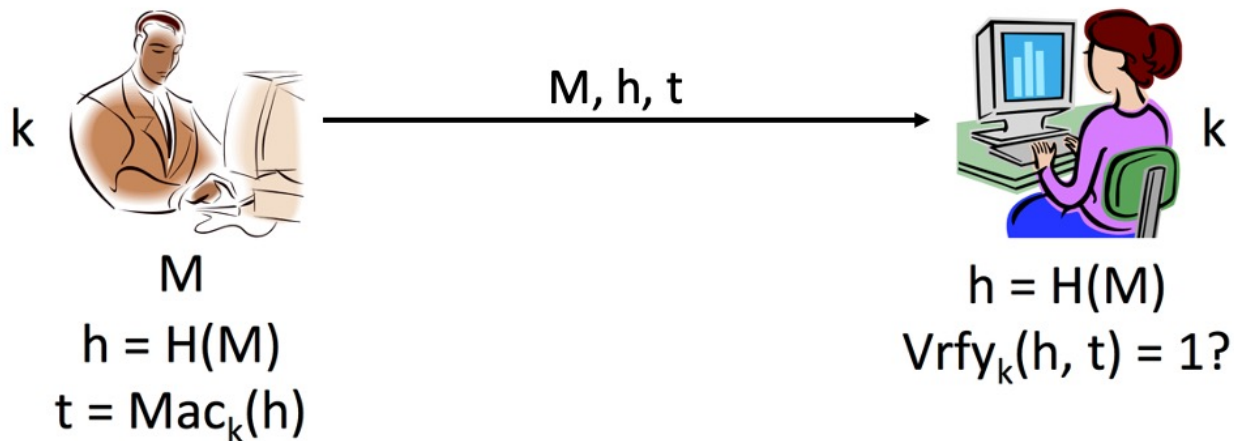


Hash-and-MAC



Instantiation?

- Hash function + block cipher-based MAC?
 - Need to implement two crypto primitives



HMAC

- Constructed entirely from (certain type of) hash functions
 - MD5, SHA-1, SHA-2
 - Not SHA-3

- Construction

$$\text{HMAC: } S(k, m) = H(k \oplus \text{opad} || H(k \oplus \text{ipad} || m))$$

- ipad: 00110110
- opad: 01011100

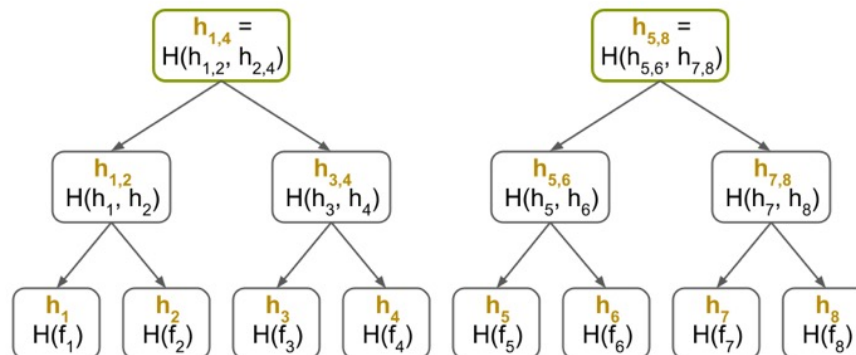
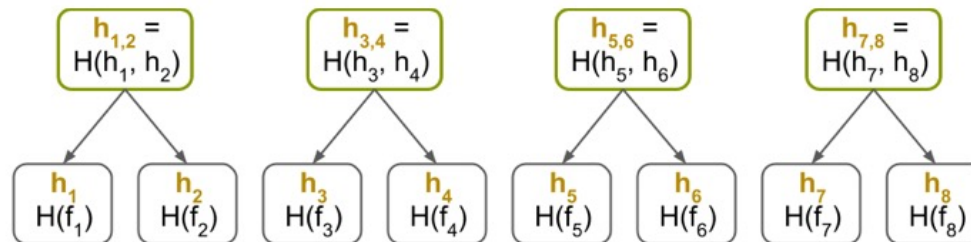
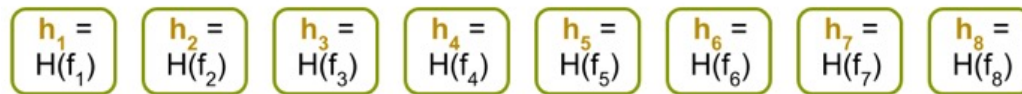
2.3 Merkle tree

Merkle tree

- Merkle tree
- $h = MHT(x_1, x_2, \dots, x_n)$
- Merkle proof

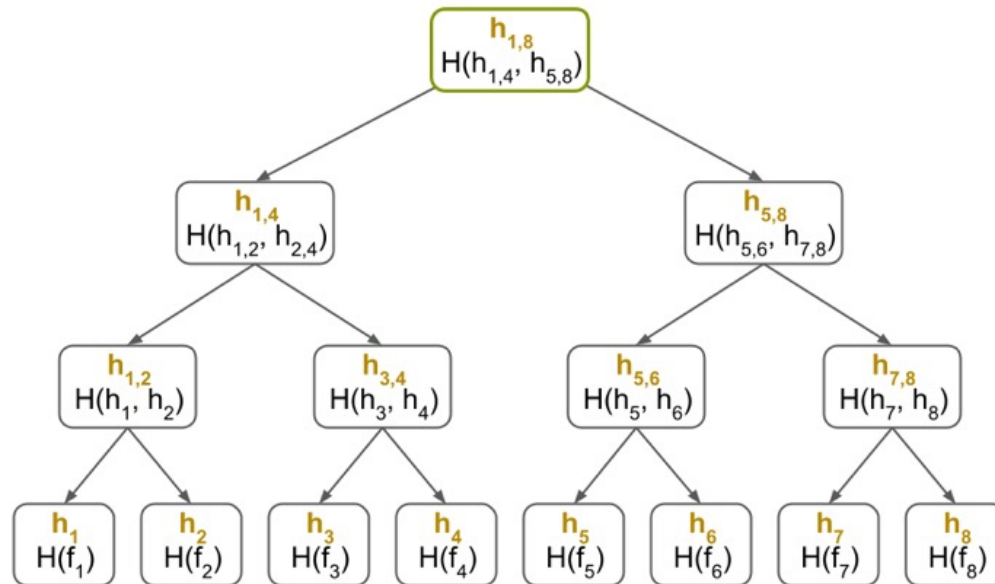
Construction of Merkle tree

- Suppose we have 8 files (f_1, \dots, f_8), H is collision resistant hash function



Construction of Merkle tree

- Suppose we have 8 files (f_1, \dots, f_8), H is collision resistant hash function

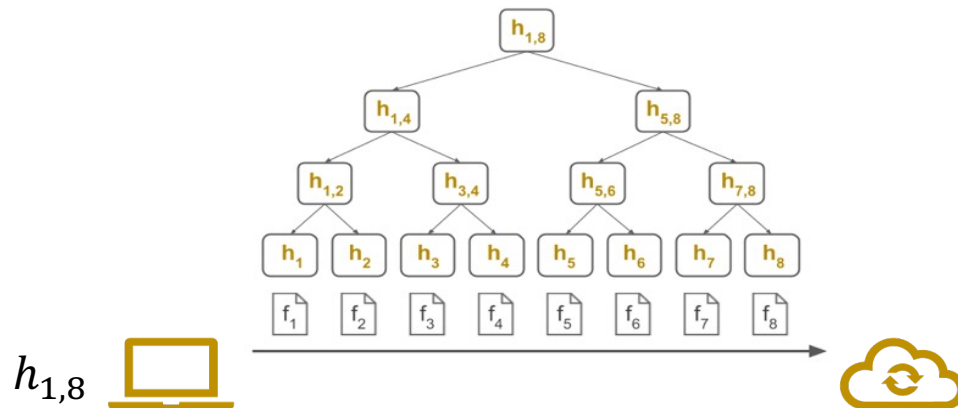


$$h_{1,8} = MHT(f_1, \dots, f_8)$$

Merkle proof

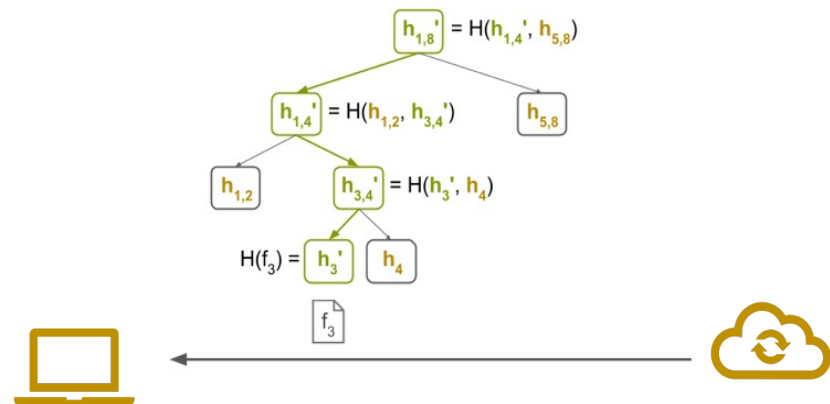
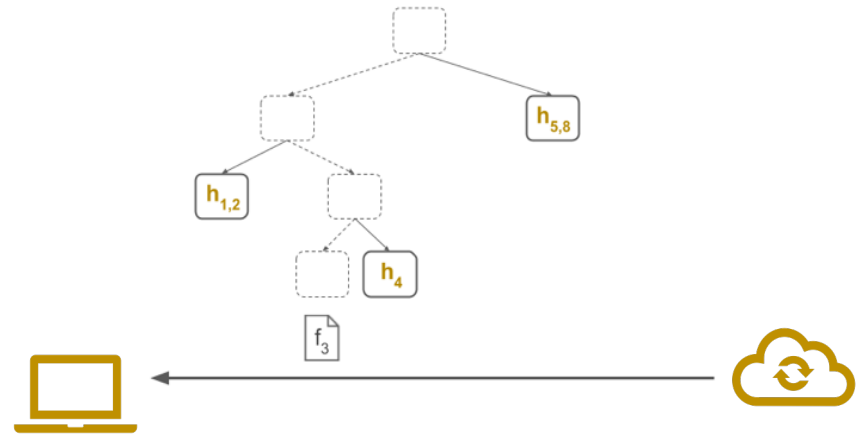
- Suppose we have 8 files (f_1, \dots, f_8), H is collision resistant hash function
- Merkle tree: $h_{1,8} = MHT(f_1, \dots, f_8)$

Whether f_3 is still stored in the cloud, and not changed?



Merkle proof

- Integrity of f_3
- download $f_3, h_4, h_{1,2}, h_{5,8}$



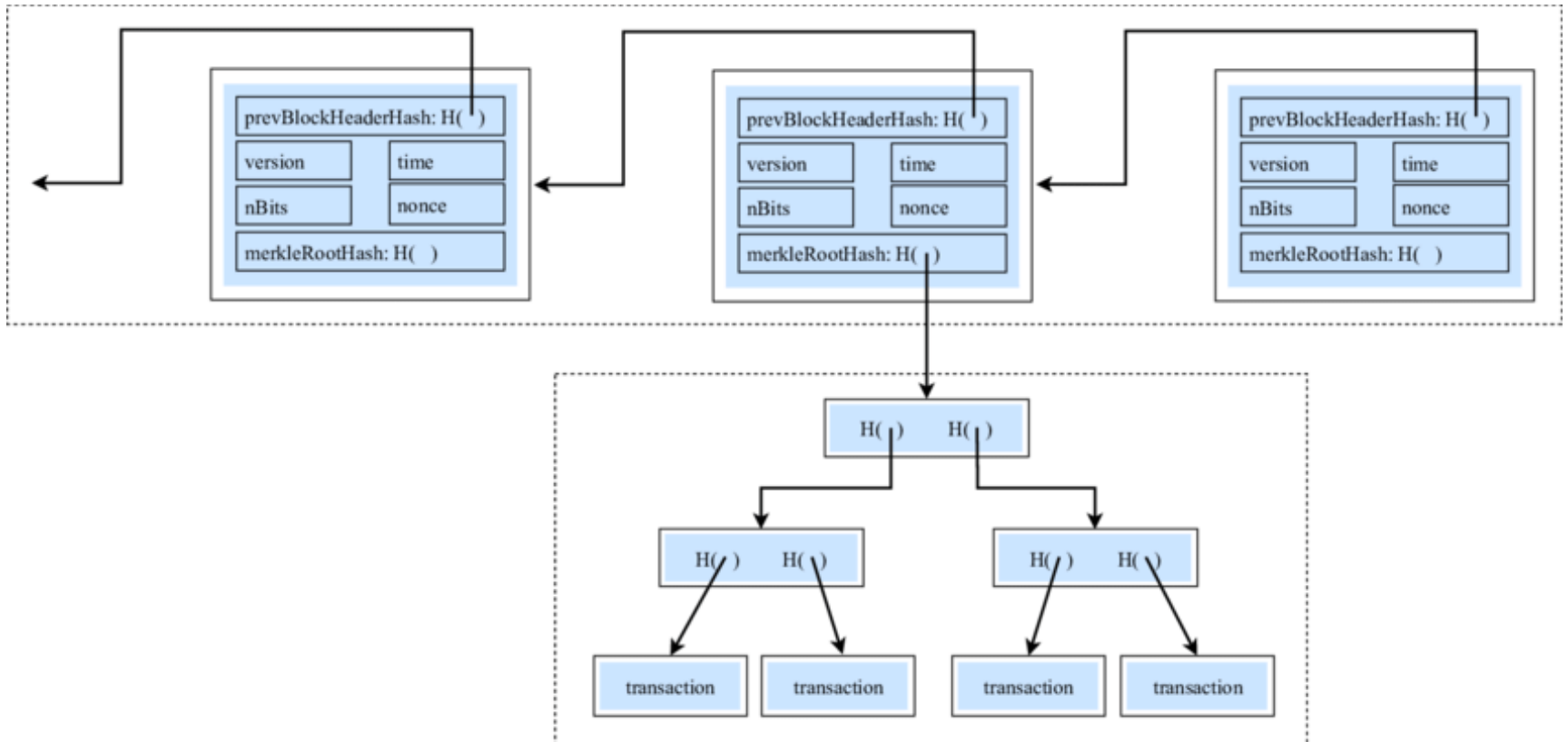
2.4 Bitcoin

Bitcoin

- Bitcoin is the first and most widely recognized cryptocurrency.
- Bitcoin is based on the ideas laid out in a 2008 whitepaper titled Bitcoin: A Peer-to-Peer Electronic Cash System.
 - Satoshi Nakamoto

Block chain

- Block chain
 - Ledger of past transactions



Mining

- Mining is the process of adding transaction records to Bitcoin's public ledger of past transactions.
- Mining is also the mechanism used to introduce Bitcoins into the system.

```
block_header = version + previous_block_hash + merkle_root + time + target_bits + nonce
for i in range(0, 2**32):
    if sha256(sha256(block_header)) < target_bits:
        break
    else:
        continue
```

Summary

- Message authentication code
 - Message integrity
 - Fixed-length MAC
 - CBC-MAC
 - Secure communications
- Hash functions and applications
 - Hash functions
 - HMAC
 - Merkle tree
 - Bitcoin