CAN304 Computer Systems Security

Lecture 2. Fundamentals of cryptography (1)

Week 2: 2024-03-05, 14:00-15:50, Tuesday

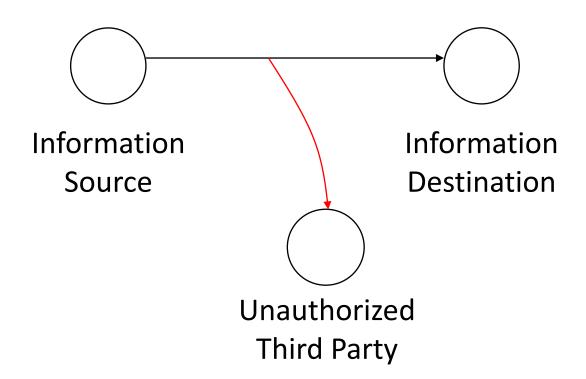
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Review of last week

- Key objectives of security: CIA
- What assets do we need to protect?
- How are those assets threatened?
- What can we do to counter those threats?



Outline

- Classical and modern cryptography
- Symmetric encryption

Learning objetives

- Learn about classical cyphers.
- Understand the basic operation of symmetric block encryption.
- Compare and contrast block encryption and stream encryption.
- Understand why CBC mode is needed.
- Apply symmetric encryption.

1. Classical and modern cryptography

Cryptography (historically)

- "...the art of writing or solving codes..."
 - Concise Oxford English Dictionary
- Historically, cryptography focused exclusively on ensuring secret communication between two parties sharing secret information in advance (aka, codes or private-key encryption)
- Which one of CIA is achieved?

- Application
 - Military organization and governments

Modern cryptography

- Much broader scope!
 - Data integrity
 - User authentication
 - Electronic auction and voting
 - Digital cash

• ...

 "Design, analysis, and implementation of mathematical techniques for securing information, systems, and computation against adversarial attack"

Classical and modern cryptography

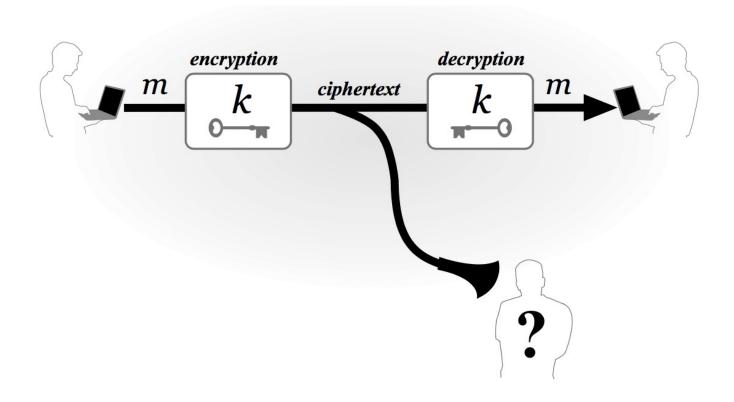
- "...the art of writing or solving codes..."
- Historically, cryptography was an art
 - Heuristic, ad hoc design and analysis
 - Schemes proposed, broken, repeat...
- Application
 - Military organization and governments
- Cryptography is now a science
 - Rigorous analysis, firm foundations, deeper understanding, rich theory
- Application
 - Everywhere

Classical cryptography

- From at least 4000 year ago, ancient Egyptians
- Until the 1970s,
- Exclusively concerned with ensuring secrecy of communication
 - Encryption
- Relied exclusively on secret information (a key) shared between the communicating parties
 - Private-key cryptography
 - AKA secret-key / shared-key / symmetric-key cryptography

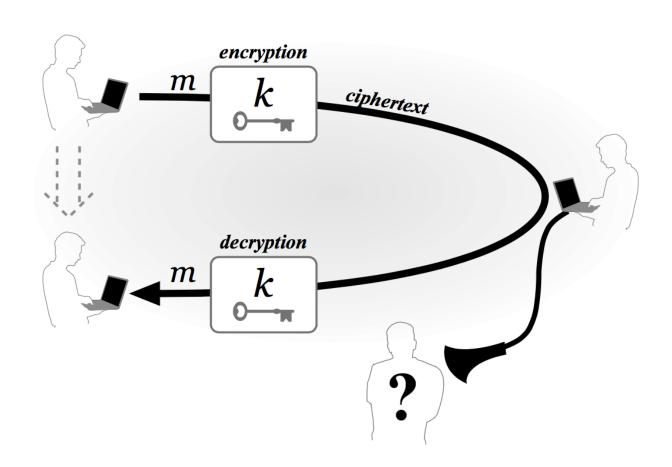
Private-key encryption

- Secure communication
 - Two parties share a key that they use to communicate securely



Private-key encryption

- Secure storage
 - A single user stores data securely over time



Private-key encryption

- A private-key encryption scheme is defined by a message space M and algorithms (Gen, Enc, Dec):
 - Gen (key-generation algorithm): generates k
 - Enc (encryption algorithm): takes key k and message $m \in M$ as input; outputs ciphertext c

$$c \leftarrow Enc_k(m)$$

• Dec (decryption algorithm): takes key k and ciphertext c as input; outputs m or "error"

$$Dec_k(c) = m$$

- For all $m \in M$ and k output by Gen,

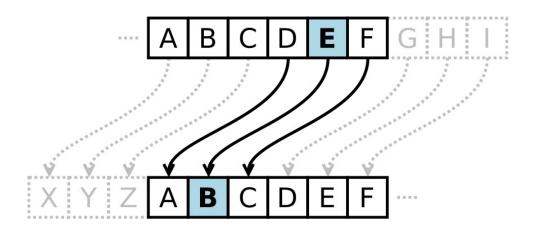
$$Dec_k(Enc_k(m)) = m$$

The shift cipher

- Caesar cipher, used by Julius Caesar
- Consider encrypting English text
- Associate a with 0; b with 1; ...; z with 25
- $k \in \{0, ..., 25\}$
- To encrypt using key k, shift every letter of the plaintext by k positions to the right (with wraparound)
- Decryption just reverses the process

The shift cipher

- Example
 - k = 23



The shift cipher, formally

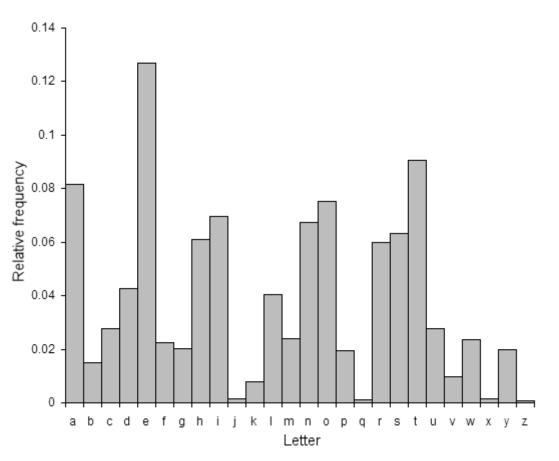
- *M* = {strings over lowercase English alphabet}
- *Gen*: choose uniform $k \in \{0, ..., 25\}$
- $Enc_k(m_1 \dots m_t)$: output $c_1 \dots c_t$, where c_i : = $[m_i + k \mod 26]$
- $Dec_k(c_1 \dots c_t)$: output $m_1 \dots m_t$, where $m_i := [c_i k \mod 26]$

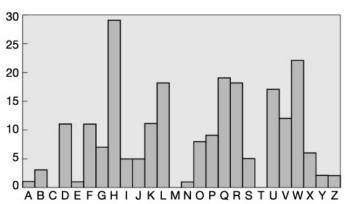
Is the shift cipher secure?

- No, only 26 possible keys!
 - Given a ciphertext, try decrypting with every possible key
 - If ciphertext is long enough (and plaintext is normal English),
 only one possibility will "make sense"
- Example
 - Ciphertext: uryybjbeyq
 - Try every possible key...
 - -k = 1: tqxxaiadxp
 - -k = 2: spwwzhzcwo
 - **...**
 - -k = 13: helloworld

Frequency analysis

• Match up the frequency distribution of the letters.





Sufficient key space principle

- The key space should be large enough to prevent "brute-force" exhaustive-search attacks
- If an encryption scheme has a key space that is too small, then it will be vulnerable to exhaustive-search attacks
- Caesar cipher is insecure
 - The key space is 26

The Vigenère cipher

- The key is now a string, not just a character
- To encrypt, shift each character in the plaintext by the amount dictated by the next character of the key
 - Wrap around in the key as needed
- Decryption just reverses the process
- Example
 - *k*='cafe'

tellhimaboutme cafecafecafeca veqpjiredozxoe

The Vigenère cipher

- Size of key space?
 - If keys are 14-character strings; then key space has size $26^{14} \approx 2^{66}$
- Brute-force search expensive/impossible
- Is the Vigenère cipher secure?
 - (Believed secure for many years...)

Attacking the Vigenère cipher

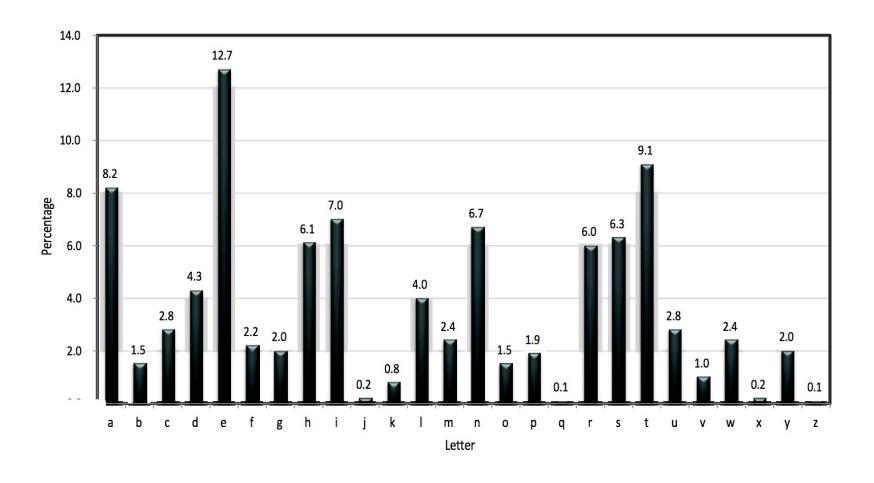
- (Assume a 14-character key)
- Observation: every 14th character is "encrypted" using the same shift

vegpjiredozxoeualpcmsdjqu
iqndnossoscdcusoakjqmxpqr
hyycjqoqqodhjcciowieii

 Looking at every 14th character is almost like looking at ciphertext encrypted with the shift cipher

Using plaintext letter frequencies

English letter frequencies



Attacking the Vigenère cipher

- Look at every 14th character of the ciphertext, starting with the first
- Let α be the most common character appearing in this portion of the ciphertext
- Most likely, this character corresponds to the most common plaintext character ('e')
- Guess the first character of the key is α e
- Repeat for all other positions

Historically...

- Cryptography was an art
 - Heuristic, ad hoc design and analysis
- In the late 1970s and early 1980s, cryptography began to develop into more of a science

2. Symmetric encryption

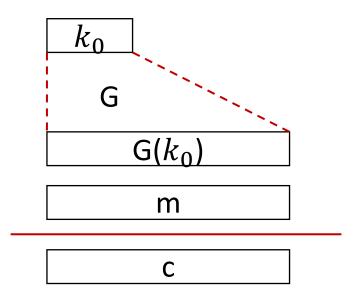
- Block ciphers
- Cryptographic modes
- Uses of symmetric cryptography

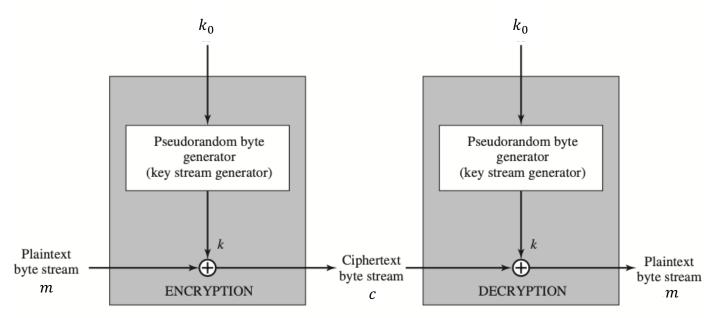
Symmetric ciphers

- Definition
 - A pair of "efficient" algorithms (E, D)
 - defined over (K, M, C)
 - where $E: K \times M \rightarrow C$, $D: K \times C \rightarrow M$
 - such that $\forall m \in M, k \in K: D(k, E(k, m)) = m$

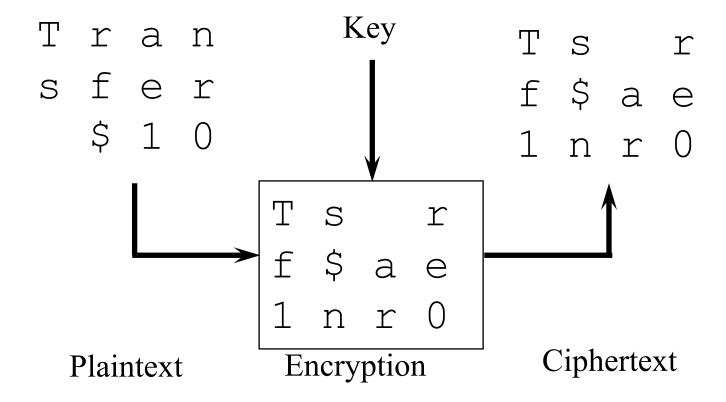
Stream ciphers

- $c \coloneqq E(k, m) = G(k_0) \oplus m$
- $m := D(k, c) = G(k_0) \oplus c$





Block ciphers



Advantages of block ciphers

- Good diffusion
 - Easier to make a set of encrypted characters depend on each other
- Immunity to insertions
 - Encrypted text arrives in known lengths
- Most common Internet crypto are done with block ciphers

Disadvantages of block ciphers

- Slower
 - Need to wait for block of data before encryption/decryption starts
- Worse error propagation
 - Errors affect entire blocks

2.1 Block ciphers

Sample block ciphers

- The Data Encryption Standard
- The Advanced Encryption Standard
- There are many others

The Data Encryption Standard

- Well known symmetric cipher
- Developed in 1977, still much used
 - Shouldn't be, for anything serious
- Block encryption, using substitutions, permutations, table lookups
 - With multiple rounds
 - Each round is repeated application of operations
- Only serious problem based on short key

The Advanced Encryption Standard

- A relatively new cryptographic algorithm
- Intended to be the replacement for DES
- Chosen by NIST
 - Through an open competition
- Chosen cipher was originally called Rijndael
 - Developed by Dutch researchers
 - Uses combination of permutation and substitution

AES Internals

- Process blocks of 128 bits using a secret key of 128, 192, or 256 bits
- View 16-byte plaintext as a two-dimensional array of bytes: s

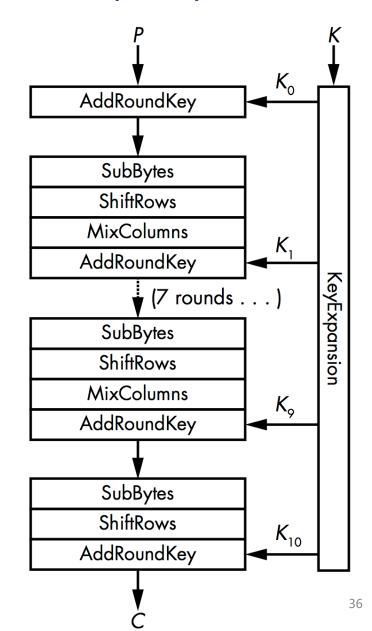
S ₀₀	S ₀₁	S ₀₂	S ₀₃
S ₁₀	S ₁₁	S ₁₂	S ₁₃
S ₂₀	S ₂₁	S ₂₂	S ₂₃
S ₃₀	S ₃₁	S ₃₂	S_{33}

The internal state of AES viewed as a 4 × 4 array of 16 bytes.

- This array is called the internal state
- AES transforms the bytes, columns, and rows of this array to produce a final value that is the ciphertext.

Substitution-permutation network (SPN)

- In order to transform its state,
 AES uses an SPN structure, with
 10 rounds for 128-bit keys, 12 for
 192-bit keys, and 14 for 256-bit
 keys.
- Four building blocks
 - AddRoundKey
 - SubBytes
 - ShiftRows
 - MixColumns



Substitution—permutation network (SPN)

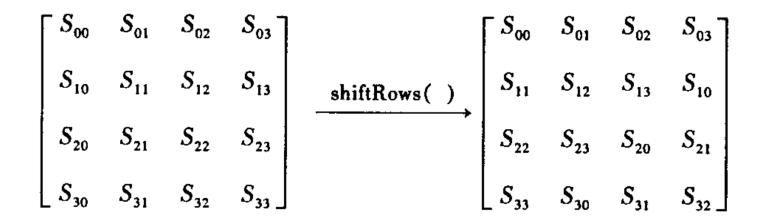
- AddRoundKey
 - XORs a round key to the internal state
- SubBytes
 - Replaces each byte $(s_{00}, s_{01}, \dots, s_{33})$ with another byte according to an S-box (next slides).

S-box

										7				57.87			
		0	1	2	3	4 .	5	6	7	8	9	A	В	С	D	E	F
	0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
	1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	CO
	2	В7	FD	93	26	36	3F	F7	CC	34	A5	E5	F1	71	D8	31	15
	3	04	C7	23	СЗ	18	96	05	9A	07	12	80	E2	EB	27	B2	75
x	4	09	83	2C	1 A	1B	6E	5 A	A0	52	3B	D6	В3	29	Е3	2F	84
	5	53	D1	00	ED	20	FC	В1	5B	6A	СВ	BE	39	4A	4C	58	CF
	6	DO	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
	7	51	A3	40	8F	92	9D	38	F5	ВС	В6	DA	21	10	FF	F3	D2
	8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3 D	64	5 D	19	73
	9	60	81	4F	DC	22	2 A	90	88	46	EE	В9	14	DE	5E	ОВ	DB
	A	EO	32	3 A	0 A	49	06	24	5C	C2	D3	AC	62	91	95	E4	79
	В	E7	C8	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7 A	AE	08
	С	BA	78	25	2E	1C	A6	B4	C6	E8	DD	74	1F	4B	BD	8B	8 A
	D	70	3E	В5	66	48	03	F6	0E	61	35	57	В9	86	C1	1D	9E
	Е	E1	F8	98	11	69	D9	8E	94	9B	1E	87	Е9	CE	55	28	DF
	F	8C	A1	89	0D	BF	Е6	42	68	41	99	2D	0F	ВО	54	ВВ	16

Substitution-permutation network (SPN)

- ShiftRows
 - Shifts the *i*th row of *i* positions to the left, for *i* ranging from 0 to
 3



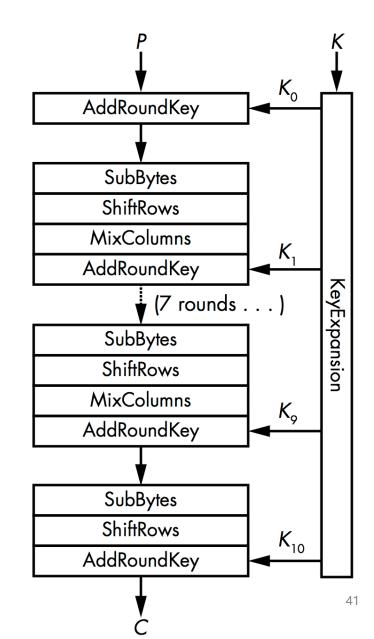
Substitution—permutation network (SPN)

- MixColumns
 - Each column of four bytes is now transformed using a special mathematical function.
 - This function takes as input the four bytes of one column and outputs four completely new bytes, which replace the original column.
 - The result is another new matrix consisting of 16 new bytes.

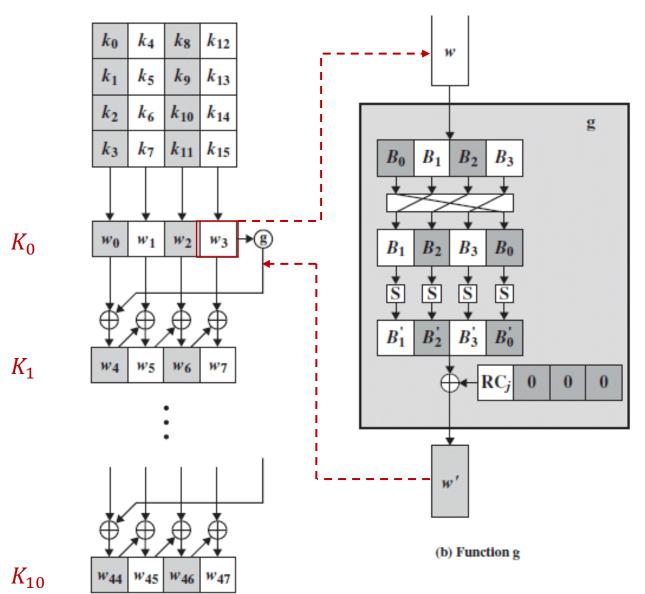
$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \begin{bmatrix} s_{00} & s_{01} & s_{02} & s_{03} \\ s_{10} & s_{11} & s_{12} & s_{13} \\ s_{20} & s_{21} & s_{22} & s_{23} \\ s_{30} & s_{31} & s_{32} & s_{33} \end{bmatrix} = \begin{bmatrix} s'_{00} & s'_{01} & s'_{02} & s'_{03} \\ s_{10} & s'_{11} & s_{12} & s'_{13} \\ s'_{20} & s'_{21} & s'_{22} & s'_{23} \\ s'_{30} & s'_{31} & s'_{32} & s'_{33} \end{bmatrix}$$

Key schedule function

- KeyExpansion
 - Create 11 round keys (K0, K1, . . . , K10) of 16 bytes each from the 16-byte initial key, using the same S-box as SubBytes and a combination of XORs



Key schedule function



 $RC_1 = 01$ $RC_2 = 02$ $RC_3 = 04$ $RC_4 = 08$ $RC_5 = 10$ $RC_6 = 20$ $RC_7 = 40$ $RC_8 = 80$ $RC_9 = 18$ $RC_{10} = 36$

Is AES secure?

- AES is as secure as a block cipher can be
 - All output bits depend on all input bits in some complex, pseudorandom way.
- But there's no proof that AES is immune to all possible attacks.
 - e.g., the new side-channel attacks

2.2 Cryptographic modes

The basic situation

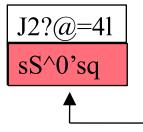
 Let's say our block cipher has a block size of 7 characters and we use the same key for all

1840326 \$100.00

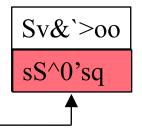
\$550.00

3370259 \$100.00 \$225.00

Now let's encrypt



Dor72m/ 2ci;aE9



Xl3lu*m #rdL04,

- There's something odd here . . .
 - Why did it happen?
 - Is this good?

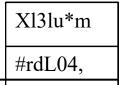
Problem with this approach

 What if these are transmissions representing deposits into bank accounts?

1840326	5610993	3370259	6840924	5610993
\$100.00	\$550.00	\$100.00	\$225.00	\$100.00

J2?@=41	Dor72m/	Sv&'>o	Xl3lu*m	Dor72m/
sS^0'sq	2ci;aE9	sS^0'sq	#rdL04,	sS^0'sq





Dor72m/ 2ci;aE9



What if account 5610993 belongs to him?

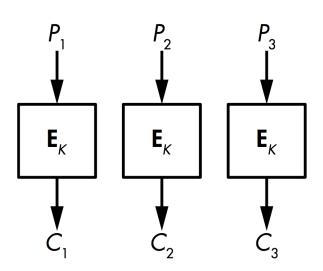


So far, so good . . .

1840326	450
2201568	5000
3370259	8900
5610993	1579
6840924	2725
8436018	10

What caused the problem?

- Each block of data was independently encrypted
 - With the same key
- So two blocks with identical plaintext encrypt to the same ciphertext
- Not usually a good thing
- We used the wrong cryptographic mode
 - Electronic Codebook (ECB) Mode



Cryptographic modes

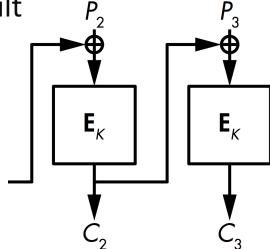
- A cryptographic mode is a way of applying a particular cipher
 - Block or stream
- The same cipher can be used in different modes

So, what mode should we have used?

- Cipher Block Chaining (CBC) mode might be better
- Ties together a group of related encrypted blocks
- Hides that two blocks are identical

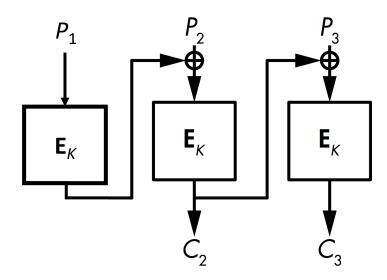
Cipher block chaining mode

- Adds feedback into encryption process
- The encrypted version of the previous block is used to encrypt this block
- For block X+1, XOR the plaintext with the ciphertext of block X
 - Then encrypt the result



- Each block's encryption depends on all previous blocks' contents
- Decryption is similar

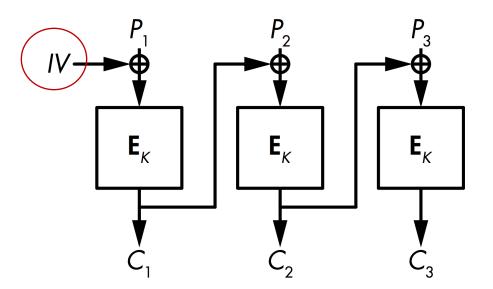
What about the first block?



- If we send the same first block in two messages with the same key,
 - Won't it be encrypted the same way?
- Might easily happen with message headers or standardized file formats
- CBC as described would encrypt the first block of the same message sent twice the same way both times

Initialization vectors

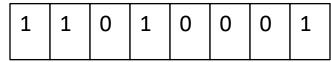
- A technique used with CBC
 - And other crypto modes
 - Abbreviated IV



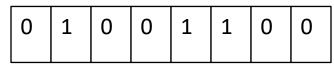
- Ensures that encryption results are always unique
 - Even for duplicate message using the same key
- XOR a random string with the first block
 - $\cdot P_1 \oplus IV$
 - Then do CBC for subsequent blocks

Encrypting with an IV





Initialization vector



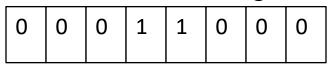
XOR IV and message

1	0	0	1	1	1	0	1

Encrypt message and send IV plus message

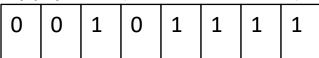
0	0	1	1	0	1	1	1
							l

Second block of message



Use previous msg for CBC

Apply CBC (XOR P2 with C1)



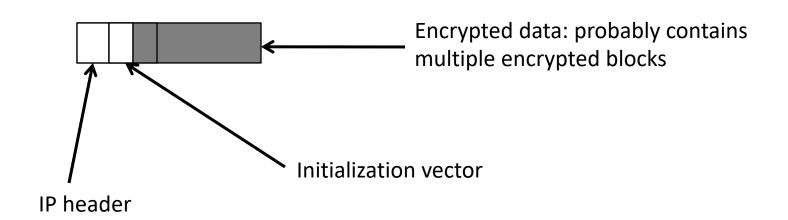
Encrypt and send second block of message

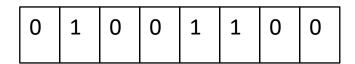
1	0	0	1	1	1	1	0
l		l	l			l	

How to decrypt with initialization vectors?

- First block received decrypts to
 - P = Dec(k, message)
 - plaintext = $P \oplus IV$
- No problem if receiver knows IV
 - Typically, IV is sent in the message
- Subsequent blocks use standard CBC
 - So can be decrypted that way

An example of IV decryption





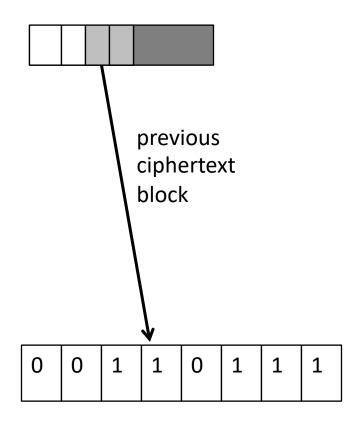
Now decrypt the message

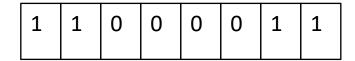
|--|

And XOR with the plaintext IV

1	1	0	1	0	0	0	1

For subsequent blocks





Now decrypt the message

0	0	1	0	1	1	1	1

And XOR with the previous ciphertext block

0	0	0	1	1	0	0	0

2.3 Uses of symmetric cryptography

Uses of symmetric cryptography

- What can we use symmetric cryptography for?
- Lots of things
 - Secrecy (confidentiality)
 - Authentication
 - Prevention of alteration (integrity)

Symmetric cryptography and secrecy

- Pretty obvious
- Only those knowing the proper keys can decrypt the message
 - Thus preserving secrecy

Symmetric cryptography and authentication

- How can I prove to you that I created a piece of data?
- I give you the data in encrypted form?
 - Using a key only you and I know
- Then only you or I could have created it
 - Unless one of us told someone else the key . . .

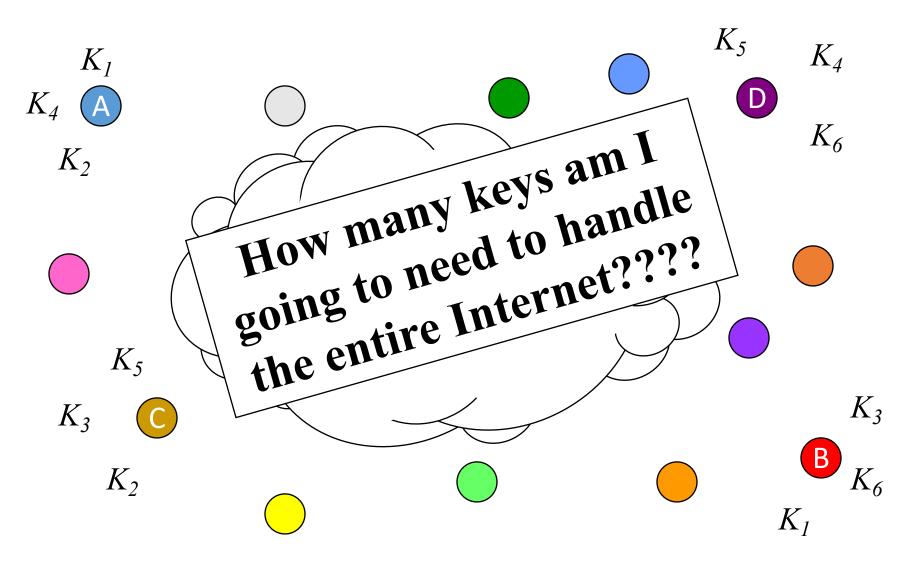
Using symmetric cryptography for authentication

- Problems with non-repudiation
 - e.g., I create a data and encrypt it using a secret key known only by you and me; later, I deny that the data is created by me.
- What if three parties want to share a key?
 - No longer certain who created anything
 - Public key cryptography can solve this problem
- What if I want to prove authenticity without secrecy?
 - Encryption is not necessary.

Symmetric cryptography and non-alterability

- Changing one bit of an encrypted message completely garbles it
 - For many forms of cryptography
 - ciphertext → plaintext (meaningless, unreadable)

Key management problem



Summary

- Classical and modern cryptography
- Symmetric encryption
 - Block ciphers
 - Cryptographic modes
 - Uses of symmetric cryptography