作業

武國寧

1 試作出下列函數的圖像

- (1) $y = \operatorname{sgn}(\sin(x))$
- (2) $y = 1 (x+1)^2$
- $(3) y = \sin(x^2)$

2 解答題

函
$$f(x) = \frac{1}{1+x}$$
,求 $f(2+x)$, $f(2x)$, $f(x^2)$, $f(f(x))$, $f(\frac{1}{f(x)})$

3 用區間表示下列不等式的解

- $(1) |1 x| x \ge 0$
- $(2) \left| x + \frac{1}{x} \right| \le 6$
- $(3) \sin x \ge \frac{\sqrt{2}}{2}$

4 求下列數集的上下確界,並依據定義加以驗證

- $(1) S = \{x | x^2 < 2\}$
- (2) $S = \{x | x = n!, n \in \mathbb{N}\}$
- (3) $S = \{x | x \in (0,1) and x is irrational number\}$

(4)
$$S = \left\{ x | x = 1 - \frac{1}{2^n}, n \in \mathbb{N} \right\}$$